

SUPERSYMMETRY IN COHERENT ILC/LHC ANALYSES

LHC/LC SUSY [WG]:

G.Blair, A.Freitas, G.Polesello, W.Porod, P.M.Zerwas

1. INTRODUCTION

- Physics scenario
- LHC/ILC characteristics

2. EXTRACTING SUSY PARAMETERS

- LHC/ILC observables and Lagrangian parameters / elw scale

3. EXTRAPOLATION TO HIGH SCALES

- minimal SUGRA: gauge couplings and mass parameters
- Intermediate scales: LR extension
- Determining superstring effective parameters

4. CONCLUSIONS

1. INTRODUCTION

Scenario: Standard Model / $v \sim 100$ GeV



Supersymmetry / $\tilde{M} \sim 1$ TeV



GUT theory / $M_{gut} \sim 10^{16}$ GeV

Question: ■ to what extent can theory / parameters be reconstructed in bottom-up approach?

- symmetries
- impact of high-scale parameters

parallel: P decay
 ν physics
cosmology

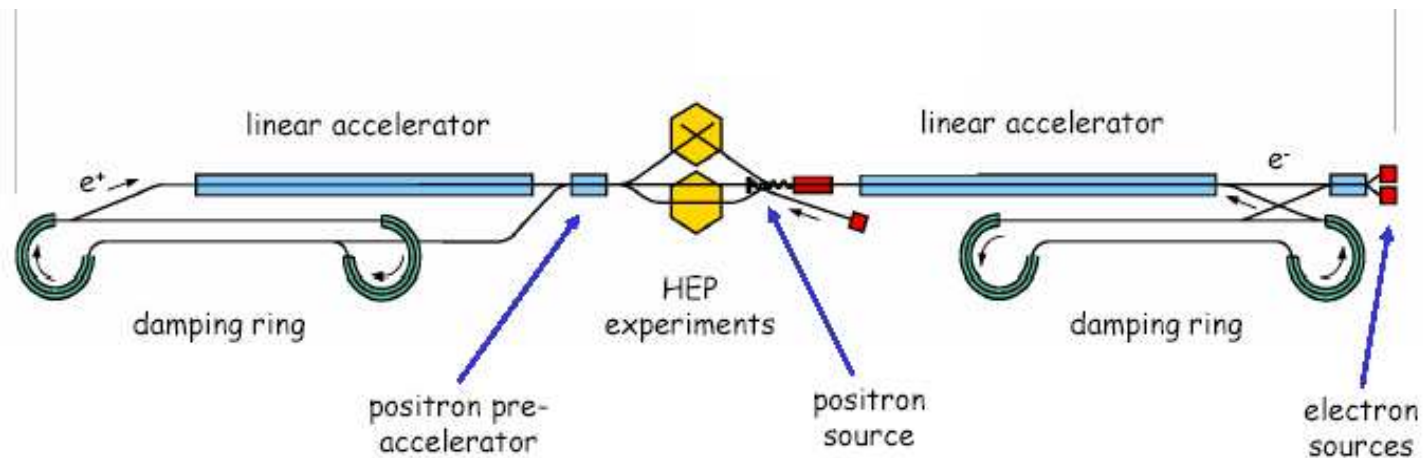
■ what precision can be reached in the alternative top-down approach?

Experimental Approach

Machines : PP collider LHC : $\sqrt{s}_{eff} \sim 4$ to 5 TeV for SUSY sector

e^+e^- linear collider : ★ ILC : $\sqrt{s} = 1$ TeV polarized e^\pm beams |
 $e^-e^- | e\gamma | \gamma\gamma |$ GigaZ

★ CLIC : $\sqrt{s} = 3$ to 5 TeV



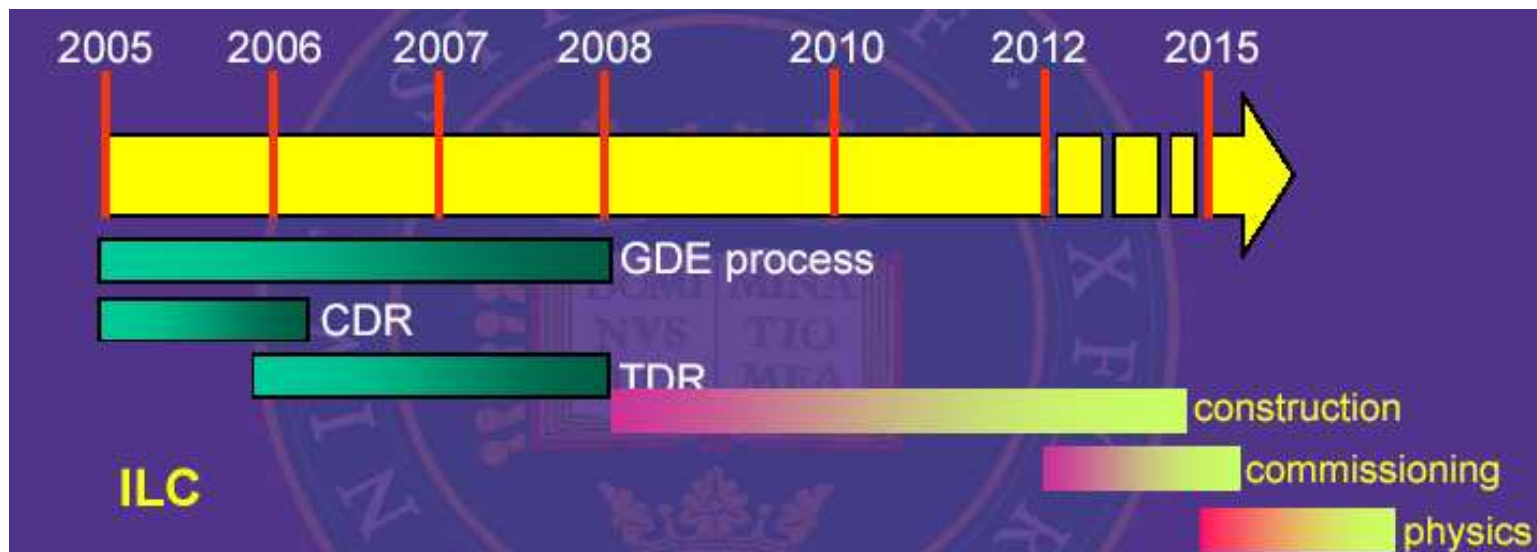
ILC LAYOUT

Experimental Approach

Machines : **PP collider LHC** : $\sqrt{s}_{eff} \sim 4 \text{ to } 5 \text{ TeV}$ for SUSY sector

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 $e^-e^- | e\gamma | \gamma\gamma | \text{GigaZ}$

technical road map:



Experimental Approach

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e^+e^- linear collider : ★ ILC : $\sqrt{s} = 1$ TeV polarized e^\pm beams |
 $e^-e^-|e\gamma|\gamma\gamma|$ GigaZ

★ CLIC : $\sqrt{s} = 3$ to 5 TeV

PROGRAM: comprehensive and high-precision picture at elw scale

platform for high-scale extrapolations \Rightarrow

- fundamental SUSY theory
- SUSY breaking mechanism

2. EXPERIMENTAL PARAMETER ANALYSIS

LHC : direct production : $pp \rightarrow Higgs$

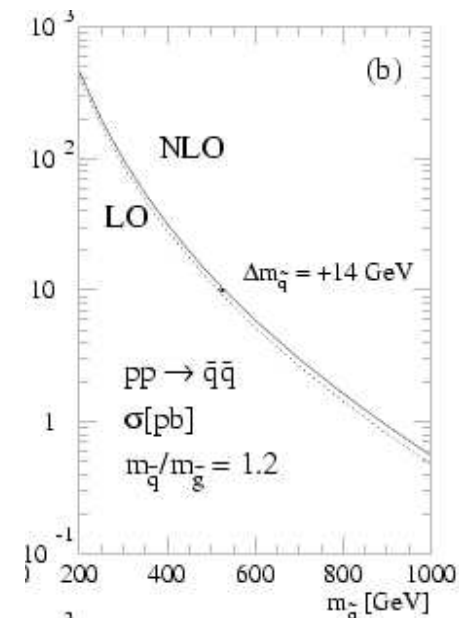
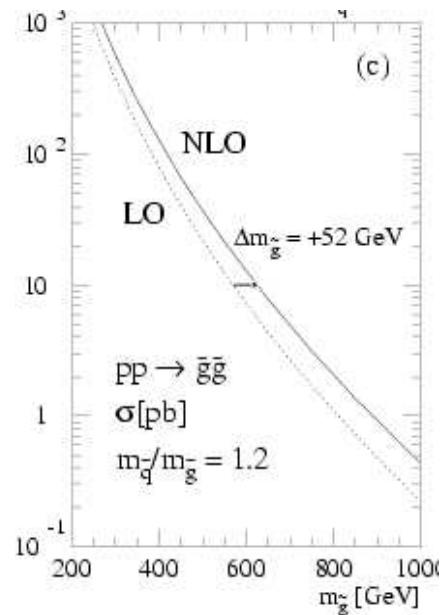
$\rightarrow \tilde{q}\tilde{q}, \tilde{g}\tilde{g}, \tilde{q}\tilde{g}$

Spira ea

Beenakker ea

cross sections theoretically under good control

$m_{\tilde{q}/\tilde{g}} \sim 1 \text{ TeV} \Rightarrow \sim 10^6$ particles



2. EXPERIMENTAL PARAMETER ANALYSIS

LHC : direct production : $pp \rightarrow Higgs$

Spira ea

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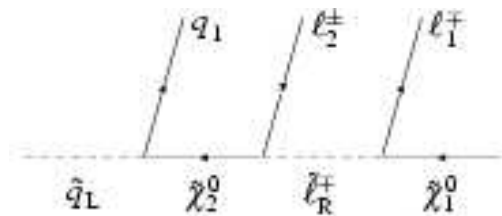
Beenakker ea

cross sections theoretically under good control

$m_{\tilde{q}/\tilde{g}} \sim 1 \text{ TeV} \Rightarrow \sim 10^6$ particles

cascade decays : $\tilde{q} \rightarrow q \tilde{\chi}_2^0 \rightarrow q (\tilde{\ell}\ell) \rightarrow q (\ell\ell) \tilde{\chi}_1^0$

Hinchliffe ea



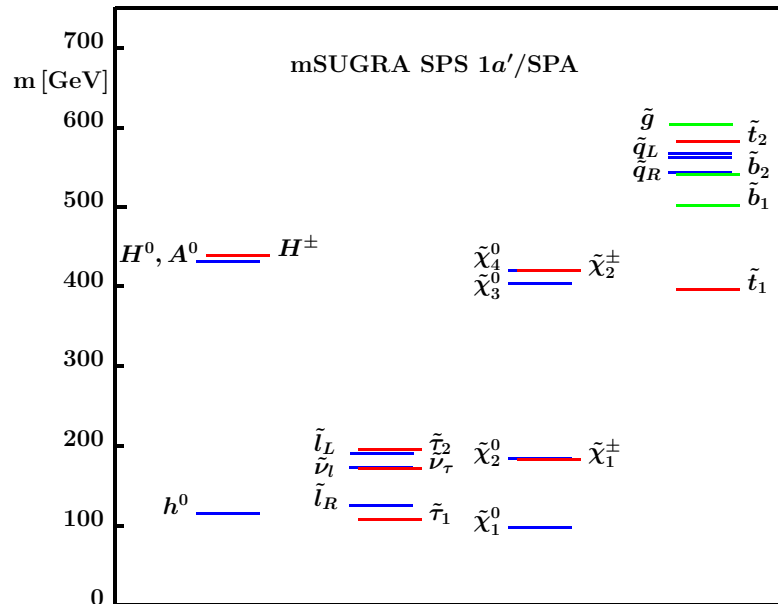
primary source of non-colored SUSY particles

SPECIFIC SUSY POINT

Spectrum SPS1a/a' :

compatible with all LE
and cosmology data **

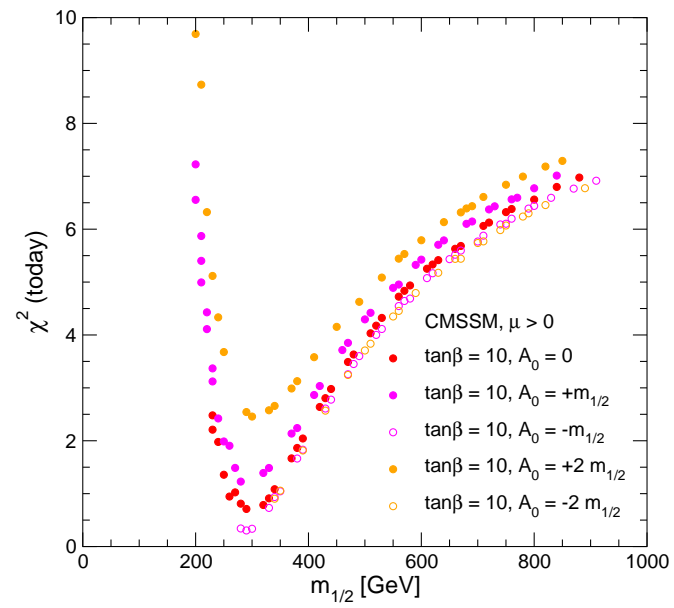
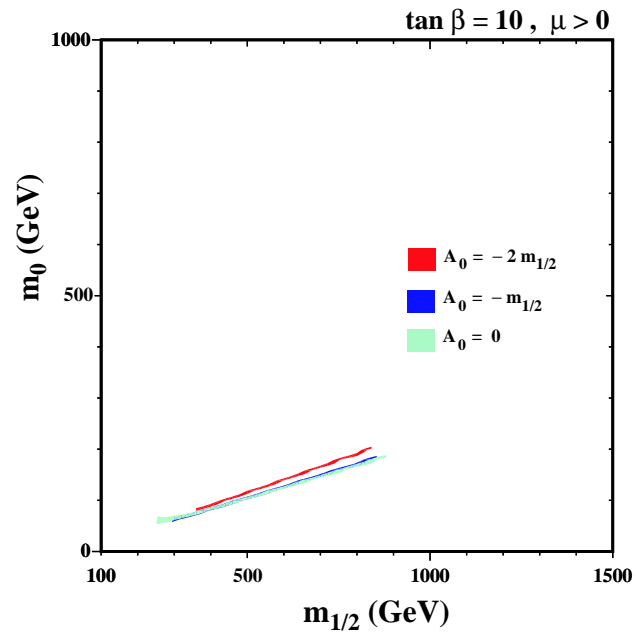
favorable mass range
for ILC and LHC



SPS1a/a' cascade : $\tilde{q} \rightarrow q \tilde{\chi}_2^0 \rightarrow q (\tilde{\ell}\ell) \rightarrow q (\ell\ell) \tilde{\chi}_1^0$

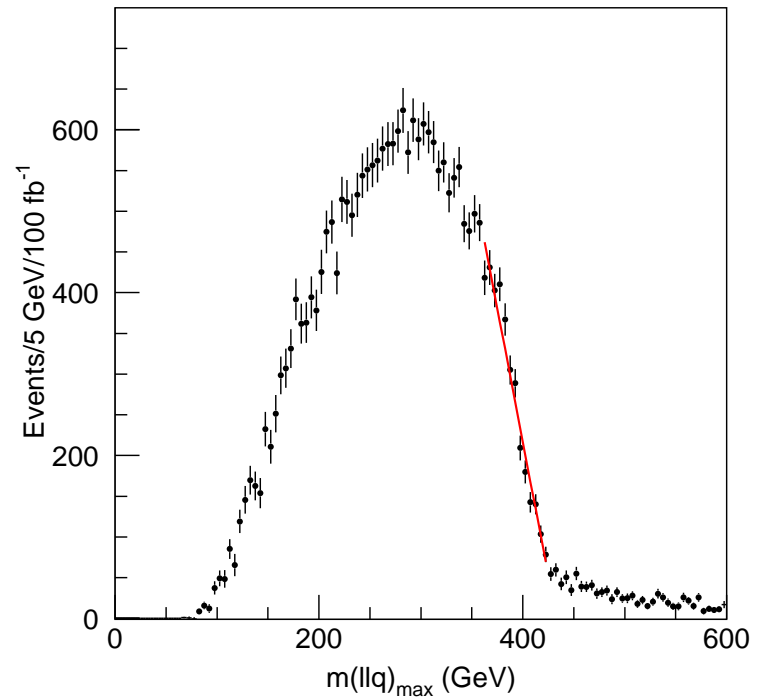
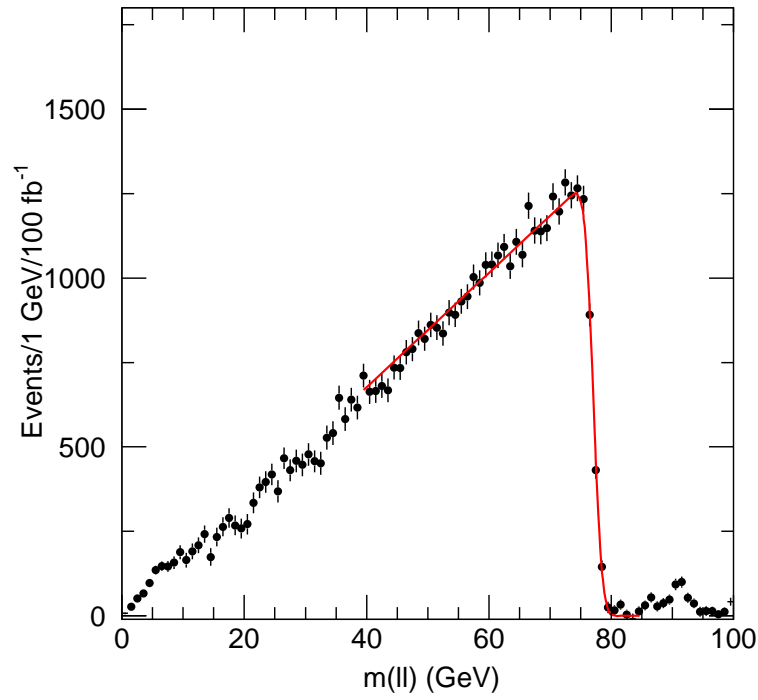


mSUGRA in WMAP and electroweak precision data:



Ellis, Heinemeyer, Olive, Weiglein

SPS1a/a' cascade at LHC : $\tilde{q} \rightarrow q \tilde{\chi}_2^0 \rightarrow q(\tilde{\ell}\ell) \rightarrow q(\ell\ell)\tilde{\chi}_1^0$



SPS1a/a' cascade : $\tilde{q} \rightarrow q \tilde{\chi}_2^0 \rightarrow q (\tilde{\ell}\ell) \rightarrow q (\ell\ell) \tilde{\chi}_1^0$

$$(m_{\tilde{\chi}_1^0}^2)^{\text{edge}} = \frac{(m_{\tilde{\chi}_2^0}^2 - m_{\tilde{\ell}}^2)(m_{\tilde{\ell}}^2 - m_{\tilde{\chi}_1^0}^2)}{m_{\tilde{\ell}}^2}$$

$$(m_{\tilde{\chi}_1^0}^2)^{\text{edge}} = \frac{(m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2^0}^2)(m_{\tilde{\chi}_2^0}^2 - m_{\tilde{\chi}_1^0}^2)}{m_{\tilde{\chi}_2^0}^2}$$

$$(m_{\tilde{q}_L}^2)^{\text{edge min}} = \frac{(m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2^0}^2)(m_{\tilde{\chi}_2^0}^2 - m_{\tilde{\ell}}^2)}{m_{\tilde{\chi}_2^0}^2}$$

$$(m_{\tilde{q}_L}^2)^{\text{edge max}} = \frac{(m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2^0}^2)(m_{\tilde{\ell}}^2 - m_{\tilde{\chi}_1^0}^2)}{m_{\tilde{\ell}}^2}$$

$$(m_{\tilde{q}_L}^2)^{\text{thres}} = \frac{[(m_{\tilde{q}_L}^2 + m_{\tilde{\chi}_2^0}^2)(m_{\tilde{\chi}_2^0}^2 - m_{\tilde{\ell}}^2)(m_{\tilde{\ell}}^2 - m_{\tilde{\chi}_1^0}^2) - (m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2^0}^2) \sqrt{(m_{\tilde{\chi}_2^0}^2 + m_{\tilde{\ell}}^2)^2 (m_{\tilde{\ell}}^2 + m_{\tilde{\chi}_1^0}^2)^2 - 16 m_{\tilde{\chi}_2^0}^2 m_{\tilde{\ell}}^4 m_{\tilde{\chi}_1^0}^2} + 2 m_{\tilde{\ell}}^2 (m_{\tilde{q}_L}^2 - m_{\tilde{\chi}_2^0}^2)(m_{\tilde{\chi}_2^0}^2 - m_{\tilde{\chi}_1^0}^2)] / (4 m_{\tilde{\ell}}^2 m_{\tilde{\chi}_2^0}^2)}$$

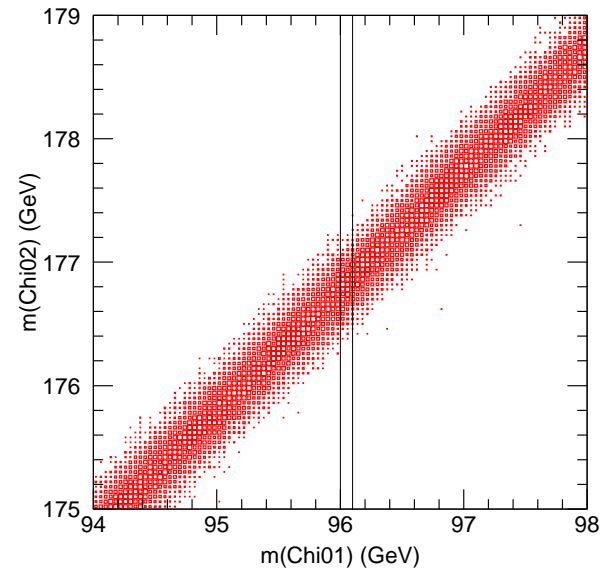
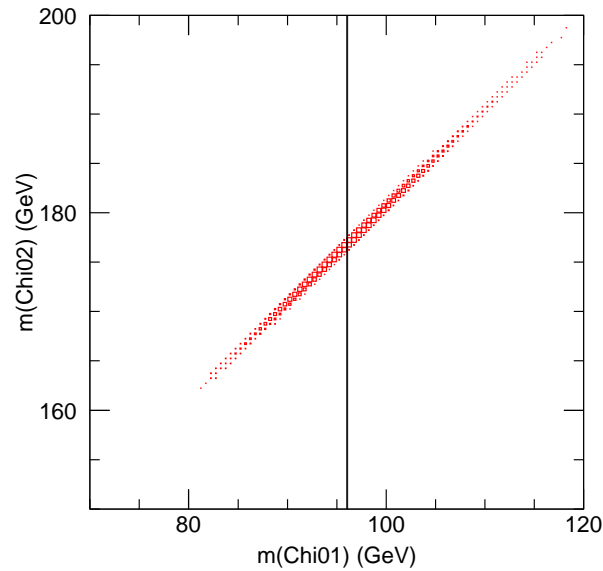
\Rightarrow mass differences with high precision

\Rightarrow absolute values less: escaping light $\tilde{\chi}_1^0 \Rightarrow$

LHC

	Mass, ideal	“LHC”	“LC”	“LHC+LC”
$\tilde{\chi}_1^\pm$	179.7			
$\tilde{\chi}_2^\pm$	382.3	–		
$\tilde{\chi}_1^0$	97.2	4.8		
$\tilde{\chi}_2^0$	180.7	4.7		
\tilde{e}_R	143.9	4.8		
\tilde{e}_L	207.1	5.0		
$\tilde{\nu}_e$	191.3	–		
$\tilde{\mu}_R$	143.9	4.8		
$\tilde{\tau}_1$	134.8	5-8		
$\tilde{\tau}_2$	210.7	–		
\tilde{q}_L	570.6	8.7		
\tilde{t}_1	399.5			
\tilde{t}_2	586.3			
\tilde{g}	604.0	8.0		
h^0	110.8	0.25		
A^0	399.4			

SPS1a/a' cascade : $\tilde{q} \rightarrow q \tilde{\chi}_2^0 \rightarrow q (\tilde{\ell}\ell) \rightarrow q (\ell\ell) \tilde{\chi}_1^0$



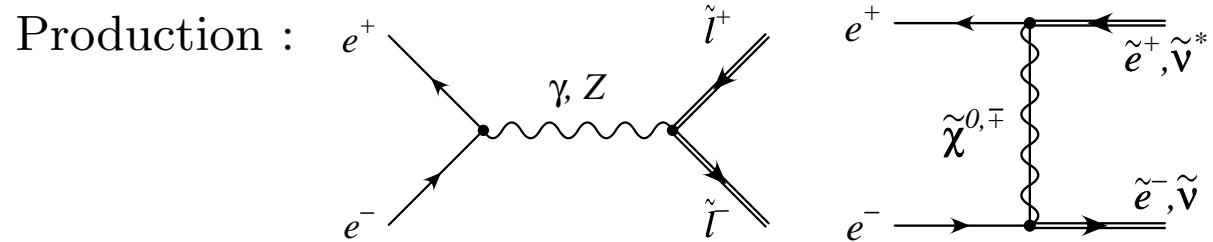
LHC : residual ambiguities

strong correlations with χ_1^0 : both problems resolved by LC

LC

charginos, neutralinos : $e^+e^- \rightarrow \tilde{\chi}\tilde{\chi}$ Fritzsche ea

sleptons, sneutrinos : $e^\pm e^\mp \rightarrow \tilde{\ell}\tilde{\ell}$ Freitas ea

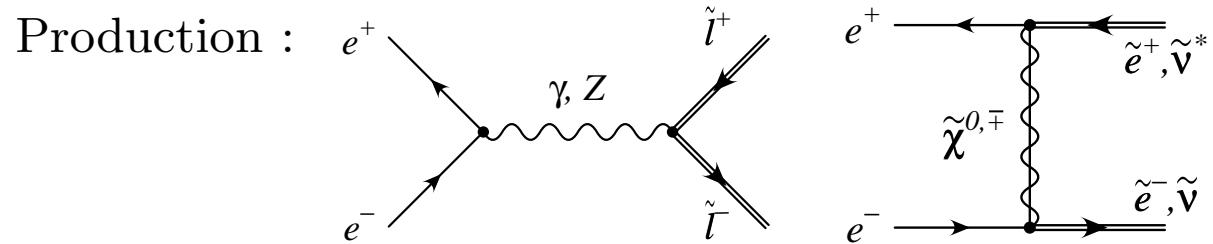


wonderful th laboratory : non-zero width and gauge invariance
Sommerfeld rescattering
analyticity : anomalous thresholds

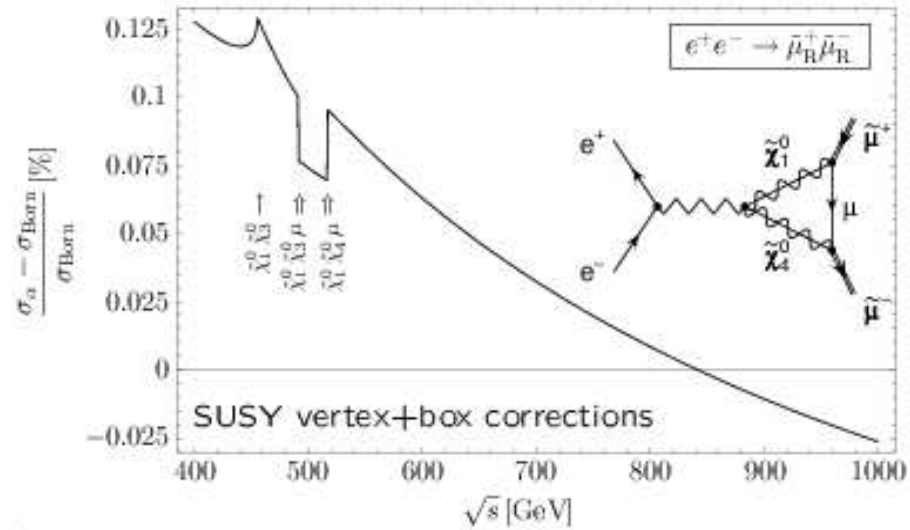
LC

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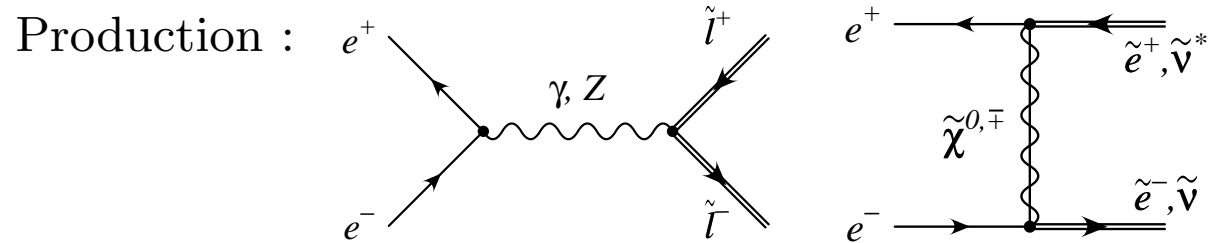
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wonderful th laboratory : non-zero width and gauge invariance

Sommerfeld rescattering

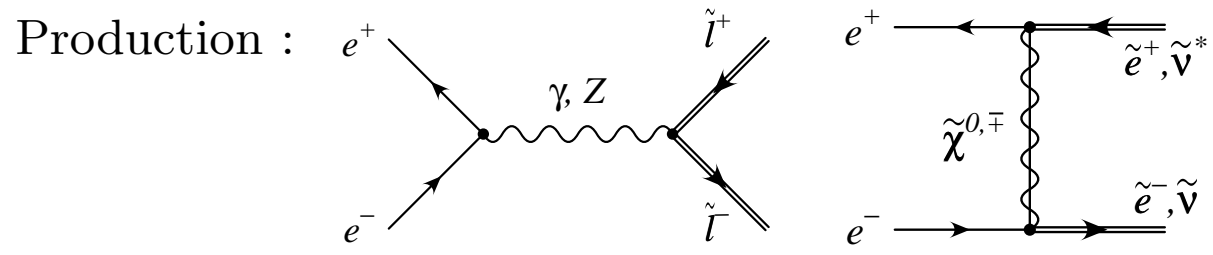
analyticity : anomalous thresholds

complete to 1-loop: exp relevant at 1% level

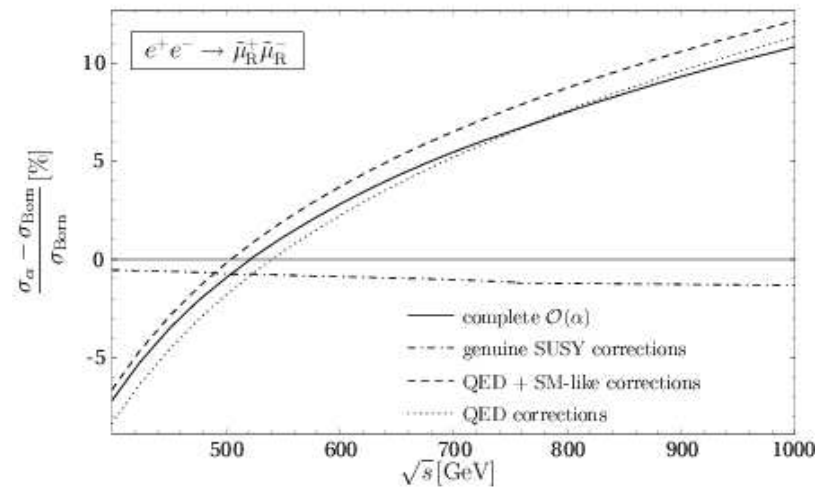
LC

charginos, neutralinos : $e^+e^- \rightarrow \tilde{\chi}\tilde{\chi}$ Fritzsche ea

sleptons, sneutrinos : $e^\pm e^- \rightarrow \tilde{l}\tilde{l}$ Freitas ea



wonderful th laboratory :



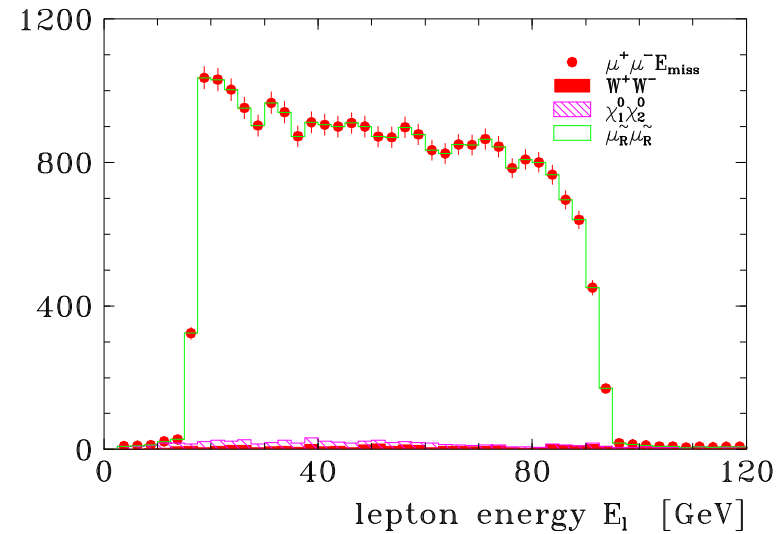
MASSES at LC

a) edge effects: $\tilde{\mu}_R \rightarrow \mu + \tilde{\chi}_1^0$

$$m_{\tilde{\ell}} = \sqrt{s} \sqrt{E_+ E_-} / (E_+ + E_-)$$

$$m_{\tilde{\chi}_1^0} = m_{\tilde{\ell}} \sqrt{1 - 2(E_+ + E_-) / \sqrt{s}}$$

precision on χ_1^0 increased by $\sim 10^2$



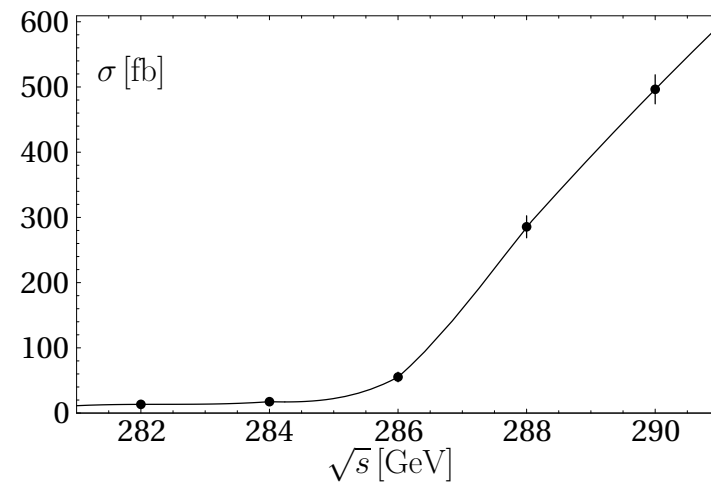
b) threshold excitations:

$$e^+ e^- \rightarrow \tilde{\mu}_R^+ + \tilde{\mu}_R^- \rightarrow \mu^+ \mu^- + E_{miss}$$

P-wave: slow β^3 rise

$$e^- e^- \rightarrow \tilde{e}_R^- + \tilde{e}_R^- \rightarrow e^- e^- + E_{miss}$$

S-wave: fast β rise



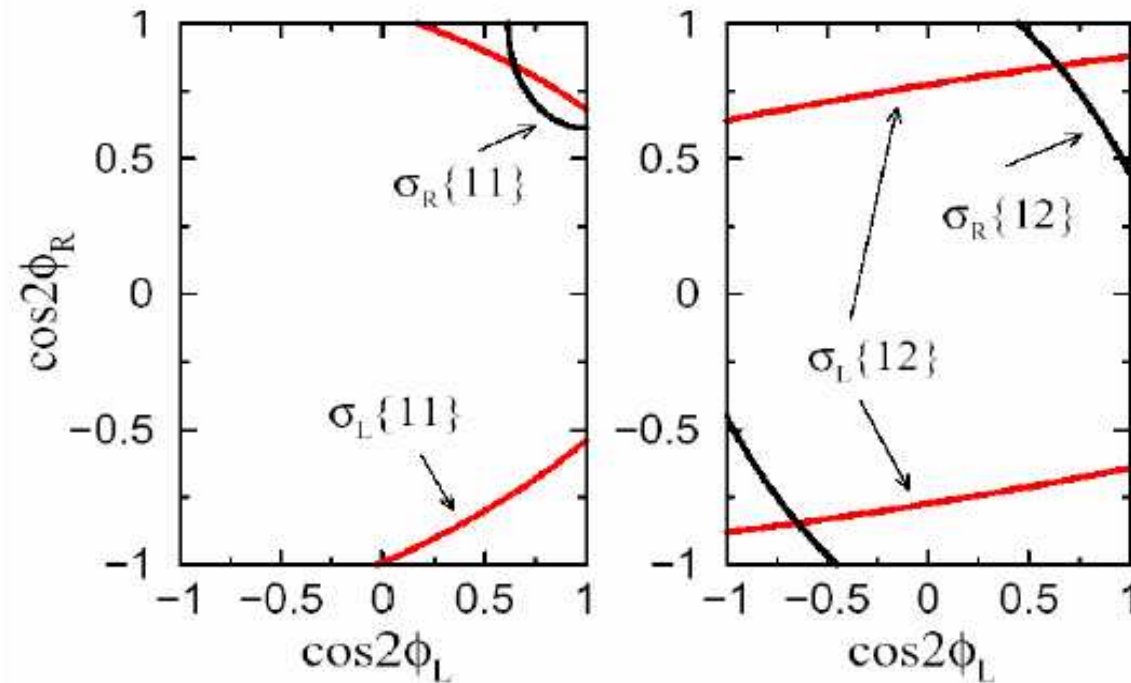
SUMMARY:

LHC+LC

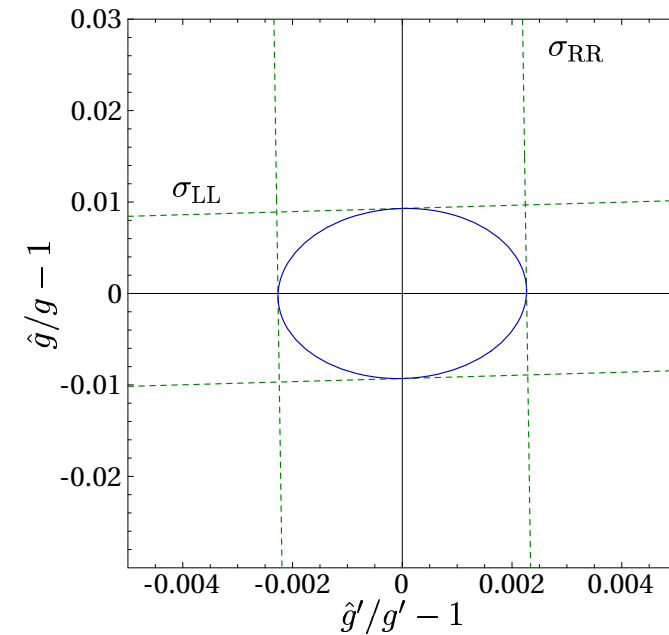
Coherent LHC+LC analyses complete and increase resolution of SUSY picture significantly

	Mass, ideal	“LHC”	“LC”	“LHC+LC”
$\tilde{\chi}_1^\pm$	179.7		0.55	0.55
$\tilde{\chi}_2^\pm$	382.3	–	3.0	3.0
$\tilde{\chi}_1^0$	97.2	4.8	0.05	0.05
$\tilde{\chi}_2^0$	180.7	4.7	1.2	0.08
\tilde{e}_R	143.9	4.8	0.05	0.05
\tilde{e}_L	207.1	5.0	0.2	0.2
$\tilde{\nu}_e$	191.3	–	1.2	1.2
$\tilde{\mu}_R$	143.9	4.8	0.2	0.2
$\tilde{\tau}_1$	134.8	5-8	0.3	0.3
$\tilde{\tau}_2$	210.7	–	1.1	1.1
\tilde{q}_L	570.6	8.7	–	4.9
\tilde{t}_1	399.5		2.0	2.0
\tilde{t}_2	586.3		–	
\tilde{g}	604.0	8.0	–	6.5
h^0	110.8	0.25	0.05	0.05
A^0	399.4		1.5	1.5

Mixing in $\tilde{\chi}^{\pm,0}$ sector* :



Yukawa = gauge identity* :



⇐ Crucial elements of basic Lagrangian at electroweak scale can be reconstructed

* Choi ea

input : particle masses $\tilde{\chi}^{\pm,0}, \tilde{g}, \tilde{\ell}, \tilde{q}, \text{Higgs}$
 polarized cross-sections $e^+e^- \rightarrow \tilde{\chi}\tilde{\chi}, \tilde{\ell}\tilde{\ell}$

Born analysis: analytical

Choi ea

$$|\mu| = M_W \left[M_{\chi^+} + M_{\chi^-} (\cos 2\phi_R + \cos 2\phi_L) \right]^{1/2}$$

$$M_2 = M_W \left[M_{\chi^+} - M_{\chi^-} (\cos 2\phi_R + \cos 2\phi_L) \right]^{1/2}$$

$$|M_1| = \left[\sum_i m_{\tilde{\chi}_i^0}^2 - M_2^2 - \mu^2 - 2M_Z^2 \right]^{1/2}$$

$$|M_3| = m_{\tilde{g}}$$

$$\tan \beta = \left[\frac{1 + M_{\chi^-} (\cos 2\phi_R - \cos 2\phi_L)}{1 - M_{\chi^-} (\cos 2\phi_R - \cos 2\phi_L)} \right]^{1/2}$$

\Rightarrow LHC not sufficient for complete parameter set:
 $[\tilde{\chi}_{1,2,4}^0] : / [M_{1,2}, \mu, \tan \beta]$

\Rightarrow ILC not sufficient:
 $/ [\tilde{g}] \sim [M_3]$

Gaugino, higgsino, scalar mass paramters, trilinear coupling, etc:

integral LHC/LC analysis \oplus loops: $\mathcal{O} = \mathcal{O}[\mathcal{MSSM}]$

[\Leftarrow light Higgs h]

Martin[1+2], Vaughn, Pierce ea

Carena, Haber; Heinemeyer ea

EXC	LHC	LC	LHC+LC	SPS1a
M_1	102.5 ± 5.3	102.3 ± 0.1	102.2 ± 0.1	102.2
M_2	191.8 ± 7.3	192.5 ± 0.7	191.8 ± 0.2	191.8
M_3	$578. \pm 15.$	\rightarrow	$588. \pm 11.$	589.4
$M_{\tilde{e}_L}$	198.7 ± 5.1	198.7 ± 0.2	198.7 ± 0.2	198.7
$M_{\tilde{e}_R}$	138.2 ± 5.0	138.2 ± 0.05	138.2 ± 0.05	138.2
$M_{\tilde{q}_L}$	$550. \pm 13.$	\rightarrow	553.3 ± 6.5	553.7
$M_{\tilde{u}_R}$	$529. \pm 20.$	\rightarrow	$532. \pm 15.$	532.1
$M_{\tilde{d}_R}$	$526. \pm 20.$	\rightarrow	$529. \pm 15.$	529.3
A_t	$-507. \pm 91.$	-501.9 ± 2.7	-505.2 ± 3.3	-504.9
μ	345.2 ± 7.3	344.3 ± 2.3	344.4 ± 1.0	344.3
$\tan \beta$	10.2 ± 9.1	10.3 ± 0.3	10.06 ± 0.2	10

SFitter: Lafaye, Plehn, Zerwas.D

3. EXTRAPOLATION TO GUT SCALE

high-precision measurements of LE Lagrangian parameters

- ⇒ extrapolate to high scale:
- symmetries/universal behavior?
 - impact of high-scale physics?

transport: RG Equations [← up to 3 loops : Jack ea]

minimal SUGRA

universal GUT scale parameters

SPS1a/a':

$b \rightarrow s\gamma$	$3.0 \cdot 10^{-4}$	3.70 ± 0.30
m_h	115.4 GeV	≥ 114 GeV
Δa_μ	$34 \cdot 10^{-10}$	25.2 ± 9.2
$\Omega_{cdm} h^2$	0.10	0.112 ± 0.017
<i>LE data</i>	EHOW	<i>max.prob.</i>

gaugino mass	$M_{1/2}$	250 GeV
scalar mass	M_0	100/70 GeV
trilin cplg	A_0	-100/-300 GeV
signum μ	$sgn[\mu]$	+
higgs mix	$\tan \beta$	10

RGE's:

$$\begin{aligned} \text{gauge couplings} & : \alpha_i = Z_i \alpha_U \\ \text{gaugino mass parameters} & : M_i = Z_i M_{1/2} \\ \text{scalar mass parameters} & : M_{\tilde{j}}^2 = M_0^2 + c_j M_{1/2}^2 + \sum_{\beta=1}^2 c'_{j\beta} \Delta M_{\beta}^2 \\ \text{trilinear couplings} & : A_k = d_k A_0 + d'_k M_{1/2} \\ Z \text{ transporters} & : Z_i^{-1} = 1 + b_i \frac{\alpha_U}{4\pi} \log \left(\frac{M_U}{M_Z} \right)^2 \\ & \text{for } i = \text{U}(1), \text{SU}(2), \text{SU}(3) \end{aligned}$$

couplings, M_i : explicit linear connections

$M_{\tilde{j},H}^2$ implicit connections :

$$M_{\tilde{L}_1}^2 = M_0^2 + 0.5 M_{1/2}^2$$

$$M_{\tilde{Q}_1}^2 = M_0^2 + 5.0 M_{1/2}^2$$

$$M_{H_2}^2 = -0.03 M_0^2 - 1.3 M_{1/2}^2 + \dots$$

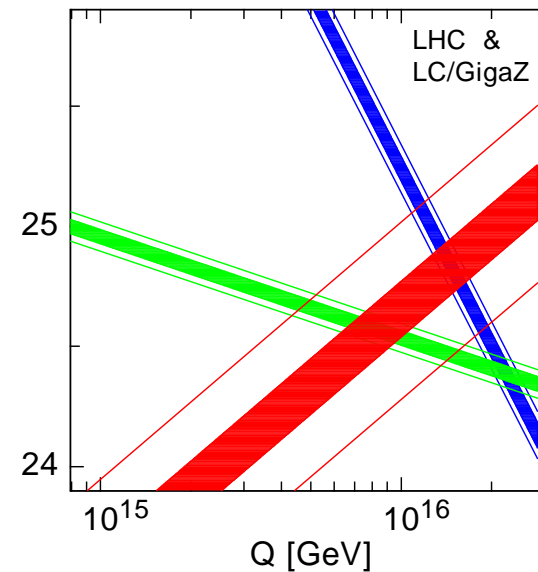
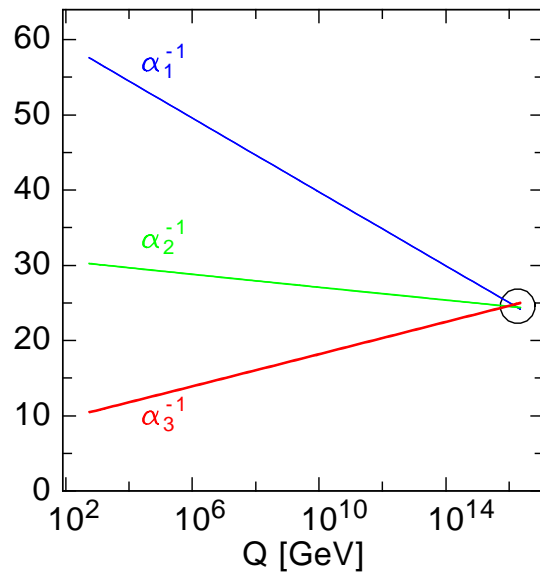
$$A_t = A_0 \text{ insensitive } [IR - fp]$$

GAUGE COUPLINGS

Evolution: 1. present electroweak/strong gauge couplings

⊕ SUSY threshold corrections \sim LHC

\Rightarrow Grand Unification at $\sim 2\sigma$ / $g : 2\%$



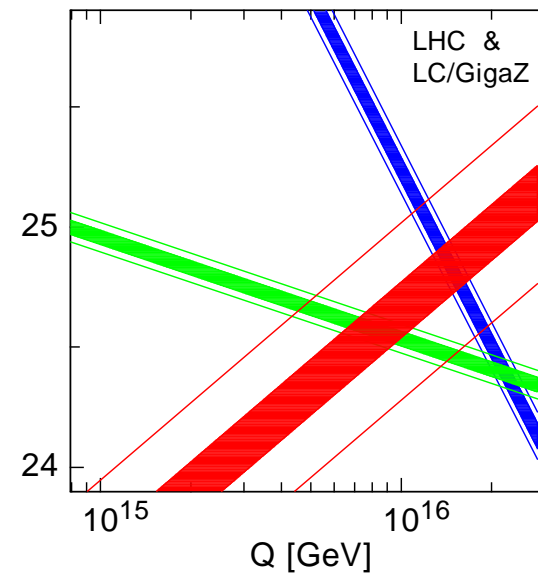
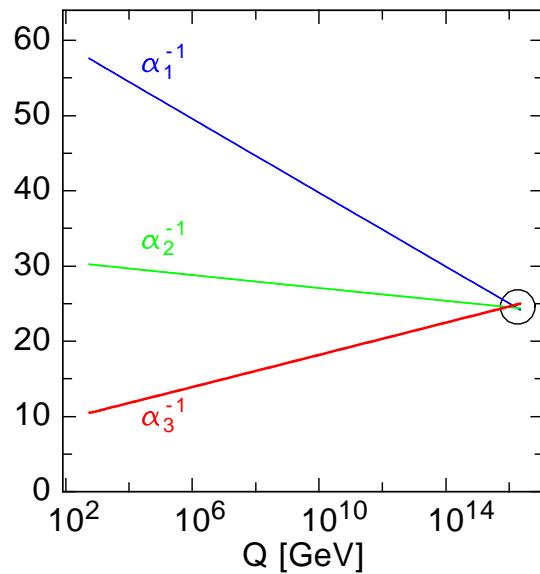
	Present/"LHC"	GigaZ/"LHC+LC"
M_U	$(2.36 \pm 0.06) \cdot 10^{16}$ GeV	$(2.360 \pm 0.016) \cdot 10^{16}$ GeV
α_U^{-1}	24.19 ± 0.10	24.19 ± 0.05
$\alpha_3^{-1} - \alpha_U^{-1}$	0.97 ± 0.45	0.95 ± 0.12

GAUGE COUPLINGS

Evolution: 2. GigaZ improved gauge couplings $\Delta \sin^2 \theta_W \simeq 10^{-5}$, $\Delta \alpha_s \simeq 10^{-3}$

⊕ “LHC+LC” completed SUSY threshold corrections

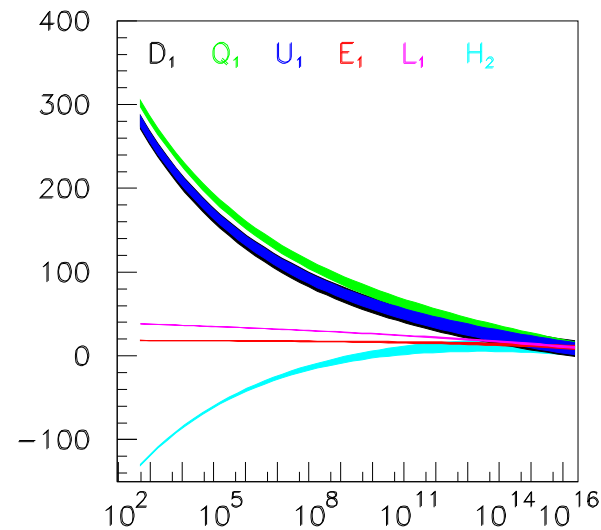
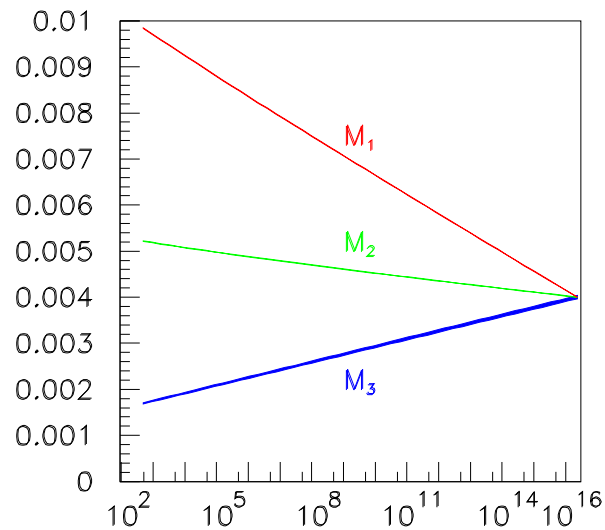
⇒ GUT scale parameters at $\sim 8\sigma$ level



	Present/"LHC"	GigaZ/"LHC+LC"
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α_U^{-1}	24.19 ± 0.10	24.19 ± 0.05
$\alpha_3^{-1} - \alpha_U^{-1}$	0.97 ± 0.45	0.95 ± 0.12

UNIVERSALITY OF MASS PARAMETERS

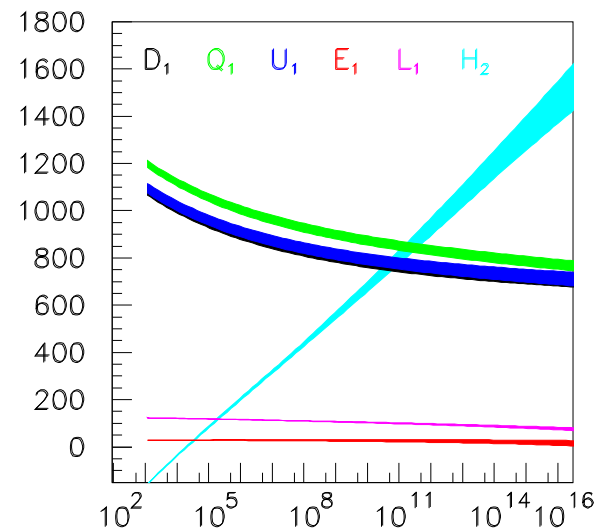
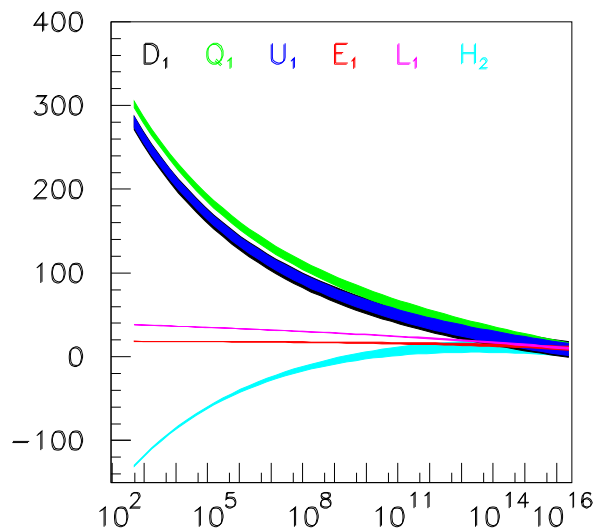
Evolution : Gaugino and scalar mass parameters



$M_i \rightarrow M_{1/2}$	excellent	$\sim 10^{-3}/10^{-2}$
$M_{\tilde{\ell}}^2 \rightarrow M_0^2$	very good	a few 10^{-2}
$M_{\tilde{Q}}^2 \rightarrow M_0^2$	abs:good / rel:improve	a few 10^{-1}

Evolution : Scalar mass parameters

mSUGRA *vs.* GMSB



⇒ evolution distinctly different for mSUGRA *vs.* GMSB

⇒ testing microscopic parameters of SUSY breaking schemes

UNIVERSALITY OF MASS PARAMETERS

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Evolution : Gaugino and scalar mass parameters \Rightarrow top-down evaluation

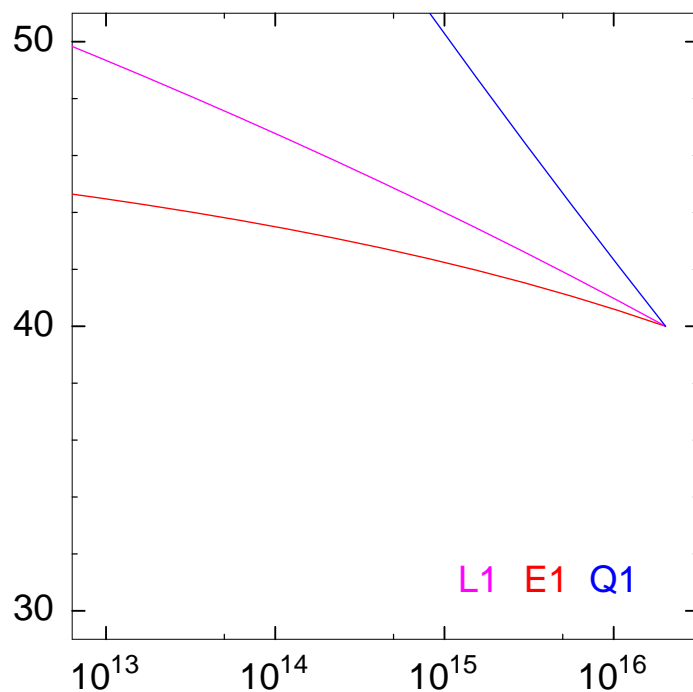
	Parameter, ideal	Experimental error
M_U	$2.36 \cdot 10^{16}$ GeV	$2.2 \cdot 10^{14}$ GeV
α_U^{-1}	24.19	0.05
$M_{1/2}$	250. GeV	0.2 GeV
M_0	100. GeV	0.2 GeV
A_0	-100. GeV	14 GeV
μ	357.4 GeV	0.4 GeV
$\tan \beta$	10.	0.4

\Rightarrow excellent parametric analysis: physics scenario near GUT scale
can be reconstructed at LHC+LC

INTERMEDIATE SCALE

$m_\nu \neq 0$: neutrino mass generated by seesaw mechanism \Rightarrow

intermediate seesaw scale $M[\nu_R]$ measurable [in-directly] ?



ν_R fields affect running through
Yukawa couplings \Rightarrow
only 3rd generation + Higgs

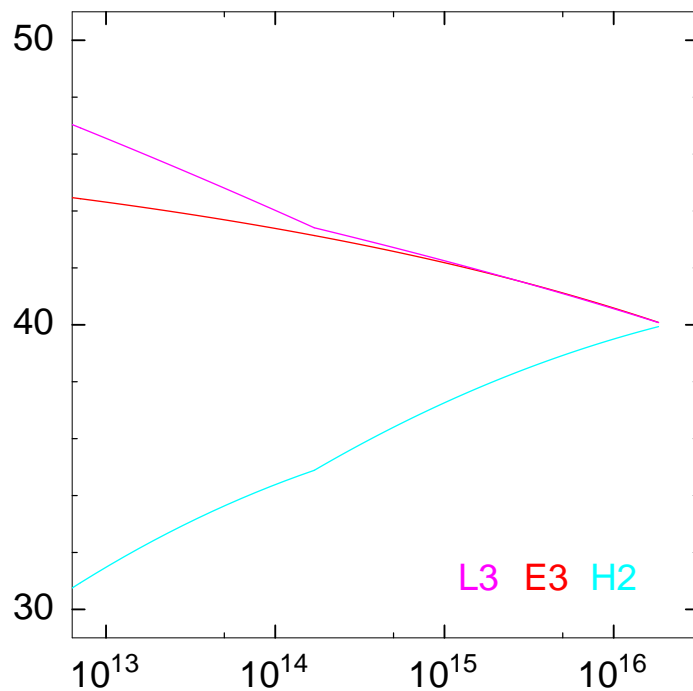
if parameters of GUT theory universal

\Rightarrow universality in 1st/2nd generation
directly observable: M_U, M_0

INTERMEDIATE SCALE

$m_\nu \neq 0$: neutrino mass generated by seesaw mechanism \Rightarrow

intermediate seesaw scale $M[\nu_R]$ measurable? \Rightarrow "qualified yes"



ν_R fields affect running through
Yukawa couplings \Rightarrow
only 3rd generation + Higgs

if parameters of GUT theory universal

\Rightarrow universality in 1st/2nd generation
directly observable: M_U, M_0

\Rightarrow in 3rd generation realized only if kink
due to seesaw ν_R mass built in

STRING EFFECTIVE THEORY

Ibanez ea; Brignole ea

Binétruy ea

scenario : heterotic string theory with orbifold compactification

LE limit: dilaton field S

moduli fields T

vev's of scalar fields determine soft SUSY breaking parameters

M_i and M_j^2 etc

Goldstino \tilde{G}

▷ SUSY breaking | S/T mixture:

$\tilde{G} = \sin \theta \tilde{S} + \cos \theta \tilde{T}$: $\sin \theta$ leading \rightarrow dilaton-type/universal

$\cos \theta$ leading \rightarrow moduli-type/non-universal

$$\text{gaugino masses} \quad : \quad M_i = \frac{\alpha_i}{4\pi} m_{3/2} \langle S \rangle \sqrt{3} \sin \theta + \mathcal{O}\{\langle T \rangle, \delta_{GS}, \dots\}$$

$$\text{scalar masses} \quad : \quad M_j^2 = m_{3/2}^2 [1 + n_j \cos^2 \theta] + \mathcal{O}\{\langle T \rangle \dots\}$$

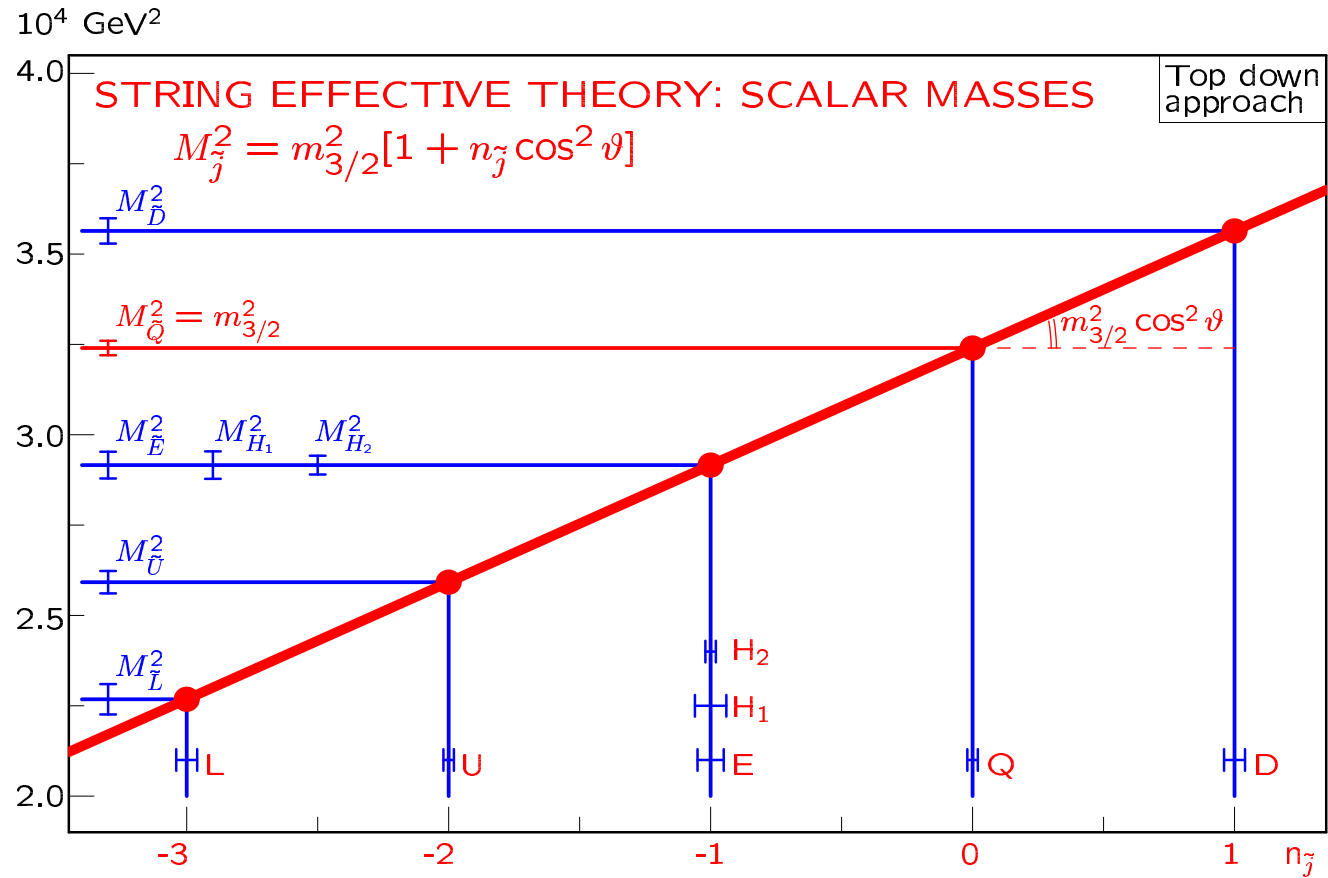
↑ integer modular weights

Model analysis :

Parameter	Ideal	Reconstructed		
$m_{3/2}$	180	179.9	\pm	0.4
$\langle S \rangle$	2	1.998	\pm	0.006
$\langle T \rangle$	14	14.6	\pm	0.2
$\sin^2 \theta$	0.9	0.899	\pm	0.002
g_s^2	0.5	0.501	\pm	0.002
δ_{GS}	0	0.1	\pm	0.4
n_L	-3	-2.94	\pm	0.04
n_E	-1	-1.00	\pm	0.05
n_Q	0	0.02	\pm	0.02
n_U	-2	-2.01	\pm	0.02
n_D	+1	0.80	\pm	0.04
n_{H_1}	-1	-0.96	\pm	0.06
n_{H_2}	-1	-1.00	\pm	0.02

\Leftarrow precision at per-cent level for integer modular weights testing stringently string-theoretical approach

“SUSY Chew-Frautschi Plot”



4. CONCLUSIONS

1. Coherent “LHC+LC” analyses establish SUSY scenario, if accessible, at electroweak scale comprehensively and with high precision:
 non-colored \Leftarrow per-mille level
 colored \Leftarrow per-cent level
2. Fundamental SUSY theory at GUT/Planck scale can be reconstructed / intermediate scales detected: universal mSUGRA, LR-extended, ...
3. String-effective parameters can be measured through gauge couplings and gaugino/scalar SUSY breaking parameters

[*P* decay / ν physics / cosmology / \oplus]

high-precision high-energy experiments \Rightarrow

LHC+ILC may be interpreted as “Telescope to Planck-scale physics”
 – if supersymmetry realized in Nature and mass domain favorable