

$$\boxed{8-2} \text{ (a) } \langle E \rangle = \frac{3}{2} kT \Rightarrow 13.6 \text{ eV} = \frac{3}{2} (8.617 \cdot 10^{-5} \text{ eV/K}) T$$

$$\text{SOLVE FOR } T = \frac{2}{3} \frac{(13.6 \text{ eV}) K}{(8.617 \cdot 10^{-5} \text{ eV})} = 105,000 \text{ K}$$

$$\text{(b) } T = 10^7 \text{ K} \quad \langle E \rangle = \frac{3}{2} (8.617 \cdot 10^{-5} \text{ eV/K}) (10^7 \text{ K}) = \boxed{1.3 \text{ keV}}$$

$$\boxed{8-5} \text{ (a) } E_{\text{TOT}} = \int_0^{\infty} E n(E) dE = N \langle E \rangle = \frac{3}{2} N kT$$

(N = NUMBER OF MOLECULES)

$$Nk = nR \quad \text{WHERE } n = \text{NUMBER OF MOLES}$$

$$\Rightarrow E_{\text{TOT}} = \frac{3}{2} (1 \text{ mol}) R (273 \text{ K}) = \boxed{3.4 \cdot 10^3 \text{ J}}$$

↑
R = 8.31 J/mol·K

(b) THE MOLAR MASS DID NOT ENTER THE CALCULATION, SO AS LONG AS YOU HAVE THE SAME NUMBER OF MOLES YOU GET THE SAME RESULT.

$$\boxed{8-8} \text{ (a) EQN (8-20) } f(v_x) = \left(\frac{m}{2\pi kT} \right)^{1/2} e^{-mv_x^2/2kT}$$

$$= \frac{1}{\sqrt{2\pi}} \left(\frac{m}{kT} \right)^{1/2} e^{-v_x^2/2(kT/m)} = \frac{1}{\sqrt{2\pi}} \frac{1}{v_0} e^{-v_x^2/2v_0^2}$$

(b) FRACTION OF MOLECULES IN $\Delta v_x = f(v_x) \Delta v_x$

$$\Delta v_x = .01 v_0$$

$$\text{TOTAL NUMBER OF MOLECULES} = N f(v_x) \Delta v_x$$

$$\frac{v_x = 0}{v_0} = \frac{N}{\sqrt{2\pi}} \frac{1}{v_0} e^0 (.01 v_0) = N \cdot 3.9 \cdot 10^{-3} = \boxed{2.3 \cdot 10^{21}}$$

$$\text{(c) } \frac{v_x = v_0}{v_0} = \frac{N}{\sqrt{2\pi}} \frac{1}{v_0} e^{-v_x^2/2v_0^2} (v_0 \cdot .01) = \frac{.01 N}{\sqrt{2\pi}} e^{-1/2} = \boxed{1.5 \cdot 10^{21}}$$

$$\text{(d) } \frac{v_x = 2v_0}{v_0} = \frac{N}{\sqrt{2\pi}} \frac{1}{v_0} e^{-4/2} (.01 v_0) = \boxed{3.3 \cdot 10^{20}}$$

$$\text{(e) } \frac{v_x = 8v_0}{v_0} = \frac{N}{\sqrt{2\pi}} (.01) e^{-64/2} = \boxed{3.0 \cdot 10^7}$$

$$\boxed{8-11} \quad n(E) = A g(E) e^{-E/kT}$$

$$\frac{n_2}{n_1} = \frac{1}{10^6} = \frac{g(E_2) e^{-E_2/kT}}{g(E_1) e^{-E_1/kT}} = \frac{g(E_2)}{g(E_1)} e^{-(E_2-E_1)/kT}$$

$$\text{ASSUME } \frac{g_2}{g_1} = 4 \Rightarrow \frac{1}{10^6} = 4 e^{-(10.2\text{eV})/kT}$$

$$\Rightarrow 4 \cdot 10^6 = e^{1.18 \cdot 10^5/T}$$

$$\Rightarrow T = \boxed{7.76 \cdot 10^3 \text{ K}}$$

$$\ln(4 \cdot 10^6) = 15.2 = 1.18 \cdot 10^5/T$$

$$\boxed{8-17} \quad \text{FIND } n_2/n_1, n_3/n_1, n_4/n_1 \text{ AT } T = 5800 \text{ K:}$$

$$\frac{n_2}{n_1} = \frac{g_2}{g_1} e^{-(E_2-E_1)/kT}$$

FOR $n=1$, $l=0$ so $g_1 = 2$ ($m_l=0, m_s=\pm 1/2$)

FOR $n=2$, $l=0$ OR 1 (8 STATES TOTAL) so $g_2 = 8$

FOR $n=3$, $l=2, 1$ OR 0 (18 STATES) so $g_3 = 18$

FOR $n=4$, $l=3, 2, 1$ OR 0 so $g_4 = 32$.

$$E_2 = \frac{1}{4} E_1, \quad E_3 = \frac{1}{9} E_1, \quad \text{AND } E_4 = \frac{1}{16} E_1, \quad E_1 = -13.6 \text{ eV}$$

$$\Rightarrow \frac{n_2}{n_1} = \frac{8}{2} e^{+(\frac{1}{4}-1)13.6\text{eV}/(8.62 \cdot 10^{-5}\text{eV/K}) 5800\text{K}} = 5.5 \cdot 10^{-9}$$

$$\text{SIMILARLY, } \frac{n_3}{n_1} = \frac{g_3}{g_1} e^{+(\frac{1}{9}-1)E_1/kT} = 2.8 \cdot 10^{-10}$$

$$\frac{n_4}{n_1} = \frac{g_4}{g_1} e^{+(\frac{1}{16}-1)E_1/kT} = 1.3 \cdot 10^{-10}$$