

# Research on the Theory of the TeV energy scale (Terascale)

Howard Haber  
SCIPP Theory  
January 9, 2019

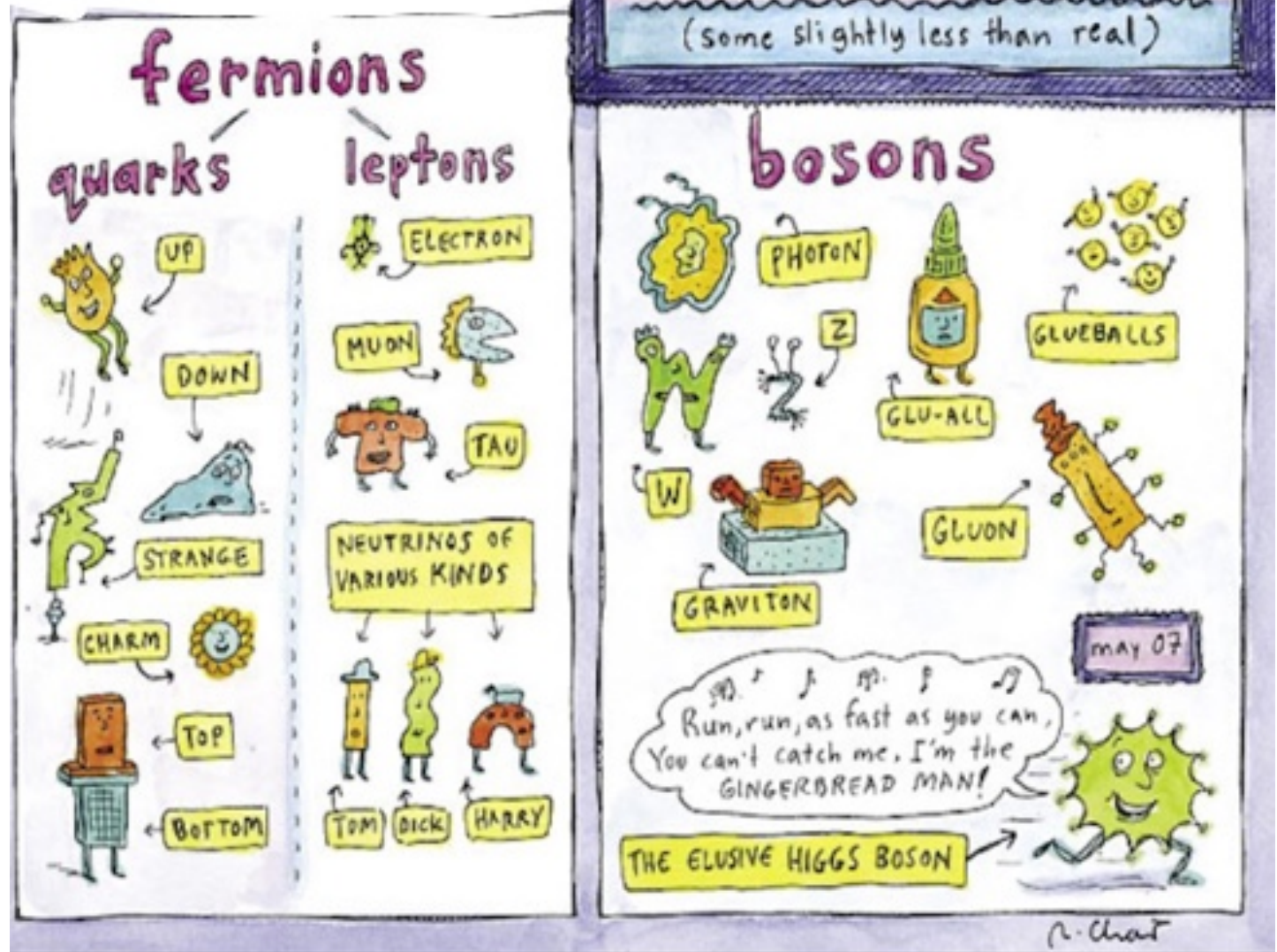
For further details, check out my webpage:  
<http://scipp.ucsc.edu/~haber/>

# SCIPP Particle Theory Group

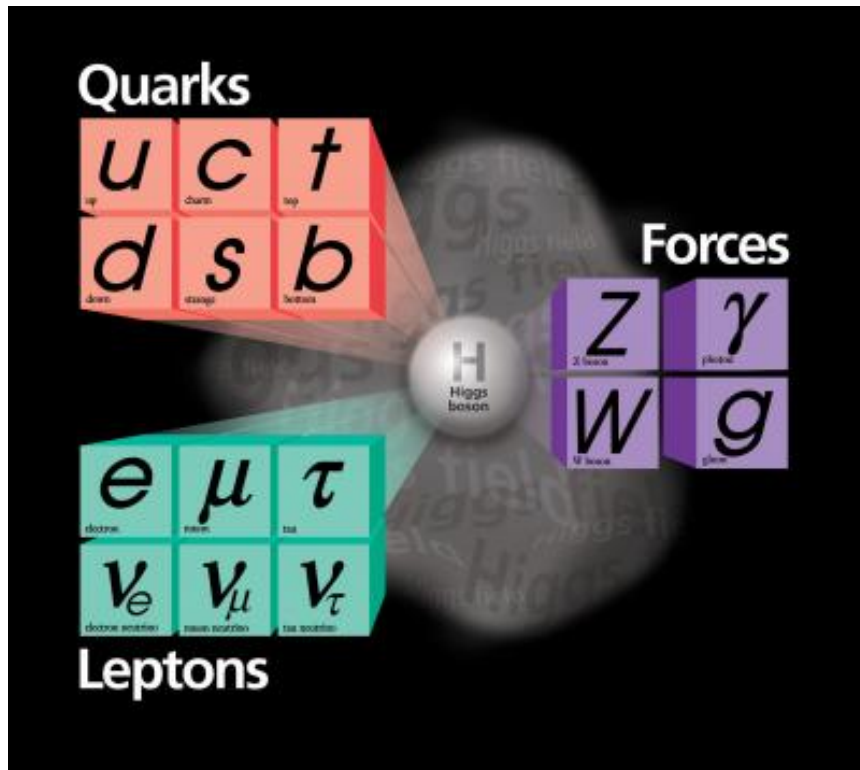
- **Michael Dine:** supersymmetry, string theory, instantons, axions, inflation and the early universe
- **Stefania Gori:** phenomenology of new physics beyond the Standard model, dark matter and dark sectors, Higgs physics
- **Howard Haber:** Higgs bosons, collider physics, new physics beyond the Standard Model at the terascale (including supersymmetry)
- **Stefano Profumo:** Theories of particle dark matter and their implications for astrophysics and collider phenomenology
- **Wolfgang Altmannshofer:** Flavor physics theory and phenomenology, CP violation, neutrino physics, Higgs physics

In addition, Anthony Aguirre and Joel Primack work on a variety of topics overlapping particle theory and astroparticle theory, including dark matter, early universe cosmology, inflation, ...

# Fundamental particles: the view in May 2007



# The Standard Model (SM) of Particle Physics



The elementary particles consists of three generations of spin-1/2 quarks and leptons and the gauge bosons of  $SU(3) \times SU(2) \times U(1)$ .

Technically, massive neutrinos require an extension of the Standard Model, but most likely the relevant scale of the new physics lies way beyond the terascale.



# Origin of mass for elementary particles

Naively, an  $SU(3) \times SU(2) \times U(1)$  gauge theory yields massless gauge bosons and massless quarks and leptons, in conflict with observation. The Standard Model employs the Higgs mechanism for mass generation. The  $SU(2) \times U(1)$  electroweak gauge invariance is spontaneously broken down to  $U(1)_{EM}$ , which yield the massive  $W$  and  $Z$  gauge bosons. In the simplest implementation, one spinless physical Higgs scalar is predicted.

## explain it in 60 seconds

**The Higgs boson**, a fundamental particle predicted by theorist Peter Higgs, may be the key to understanding why elementary particles have mass. Explaining the connection, I am reminded of the puzzler, "If sound cannot travel in a vacuum, why are vacuum cleaners so noisy?" This riddle actually touches on a profound insight of modern physics: the vacuum—or empty space—is far from empty. It is indeed "noisy" and full of virtual particles and force fields. The origin of mass seems to be related to this phenomenon.

In Einstein's theory of relativity, there is a crucial difference between massless and massive particles: All massless particles must travel at the speed of light, whereas massive particles can never attain this ultimate speed. But, how do massive particles arise? Higgs proposed that the vacuum contains an omnipresent field that can slow down some (otherwise massless) elementary particles—like a vat of molasses slowing down a high-speed bullet. Such particles would behave like massive particles traveling at less than light speed. Other particles—such as the photons of light—are immune to the field: they do not slow down and remain massless.

Although the Higgs field is not directly measurable, accelerators can excite this field and "shake loose" detectable particles called Higgs bosons. So far, experiments using the world's most powerful accelerators have not observed any Higgs bosons, but indirect experimental evidence suggests that particle physicists are poised for a profound discovery.

**Howard E. Haber, University of California, Santa Cruz**



From Symmetry Magazine, volume 3, issue 6, August 2006

On July 4, 2012, the discovery of a new boson is announced which may be the long sought after Higgs boson.

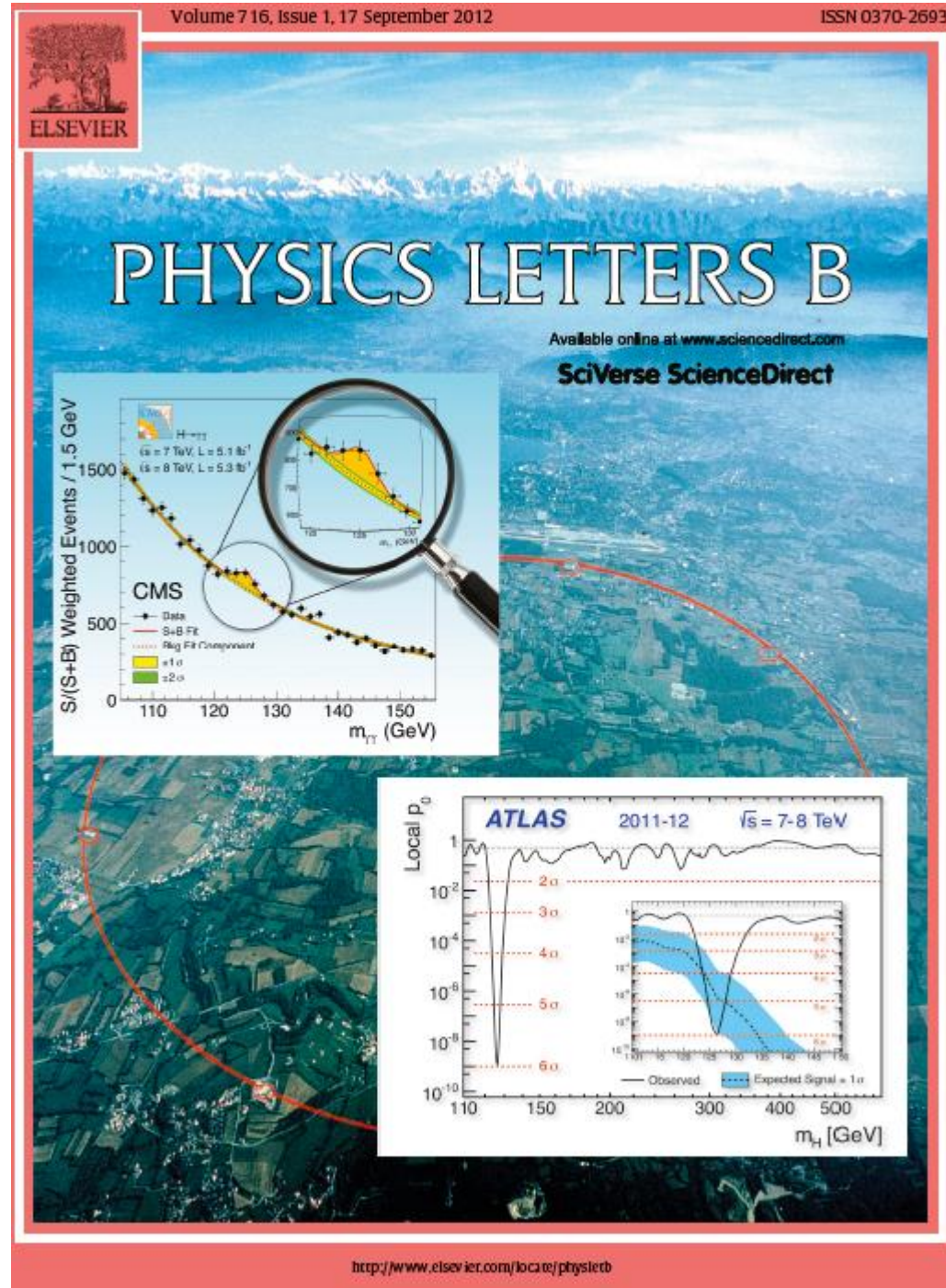
The discovery papers are published two months later In Physics Letters B.

ATLAS Collaboration:

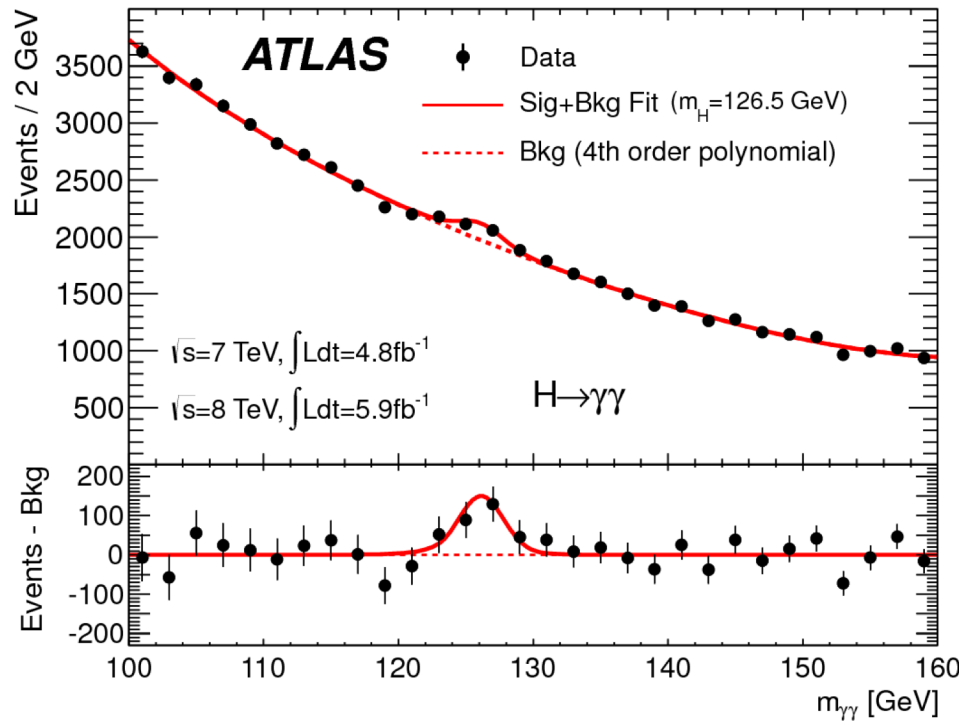
**Physics Letters B716 (2012) 1—29**

CMS Collaboration:

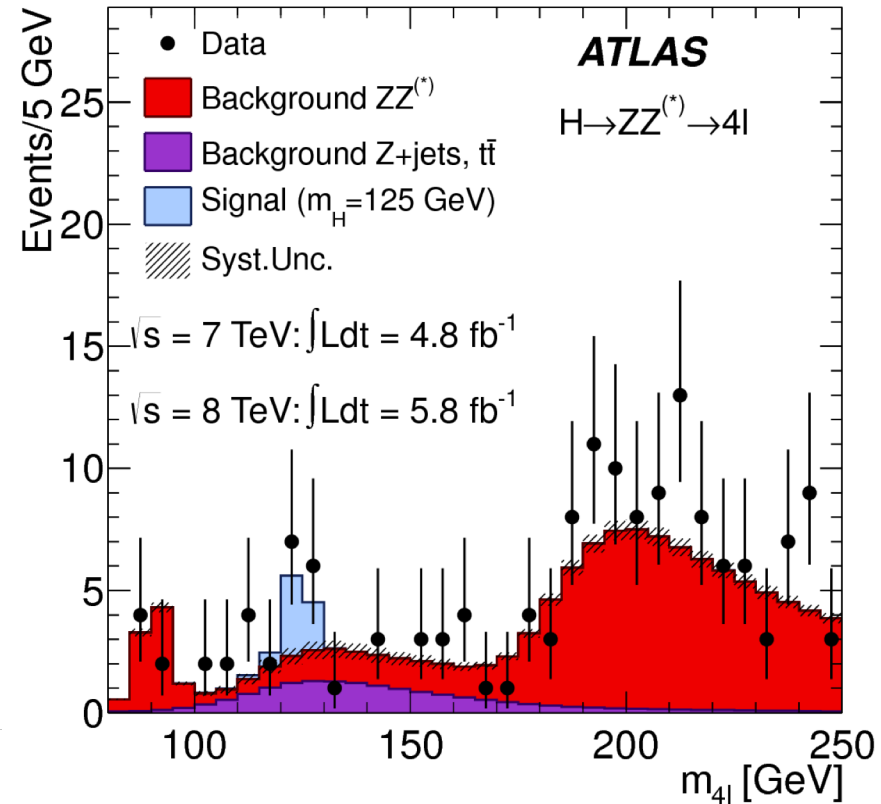
**Physics Letters B716 (2012) 30—61**



# A boson is discovered at the LHC by the ATLAS Collaboration



Invariant mass distribution of diphoton candidates for the combined 7 TeV and 8 TeV data samples. The result of a fit to the data of the sum of a signal component fixed to  $m_H = 126.5$  GeV and a background component described by a fourth-order Bernstein polynomial is superimposed. The bottom inset displays the residuals of the data with respect to the fitted background component.

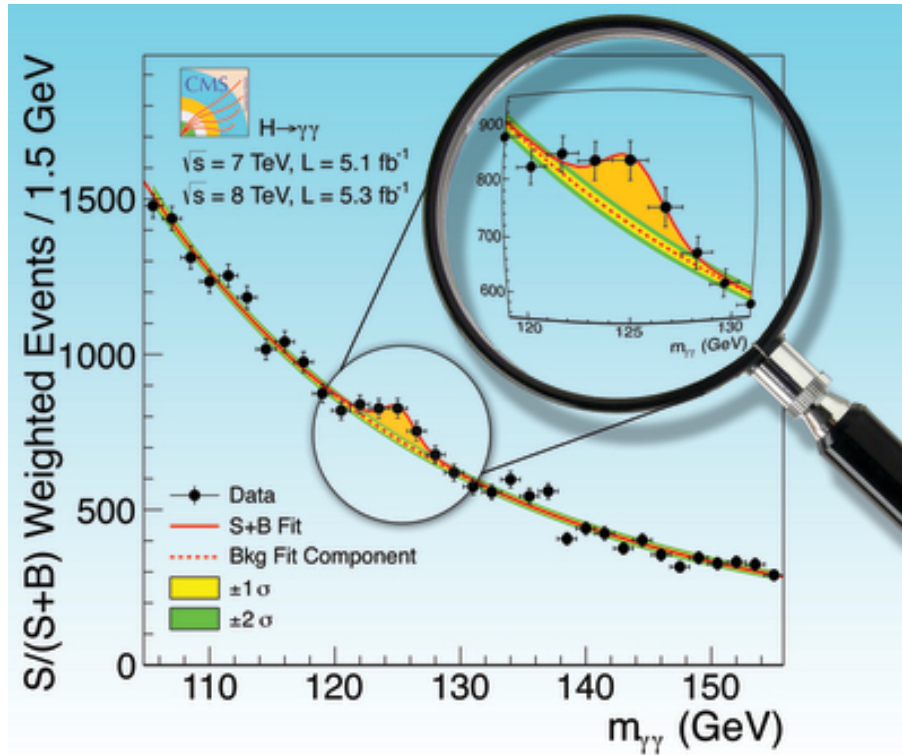


The distribution of the four-lepton invariant mass,  $m_{4l}$ , for the selected candidates, compared to the background expectation in the 80 to 250 GeV mass range, for the combination of the 7 TeV 8 TeV data. The signal expectation for a Higgs boson with  $m_H = 125$  GeV is also shown.

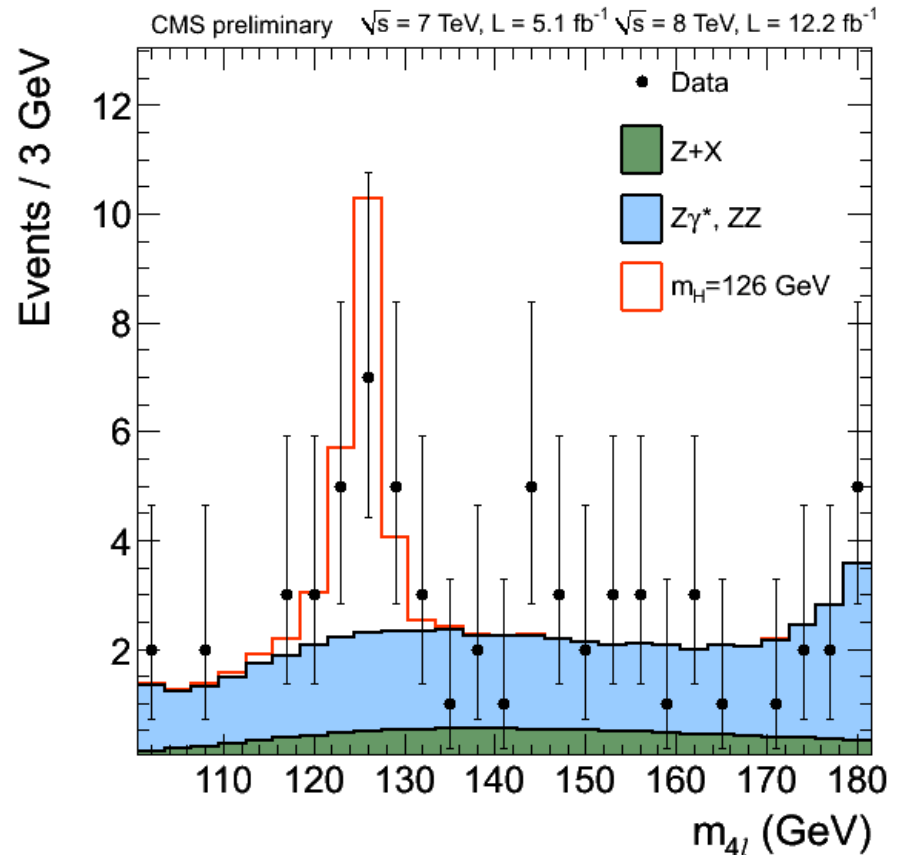
(Taken from Physics Letters B716 (2012) 1-29.)



# A boson is discovered at the LHC by the CMS Collaboration

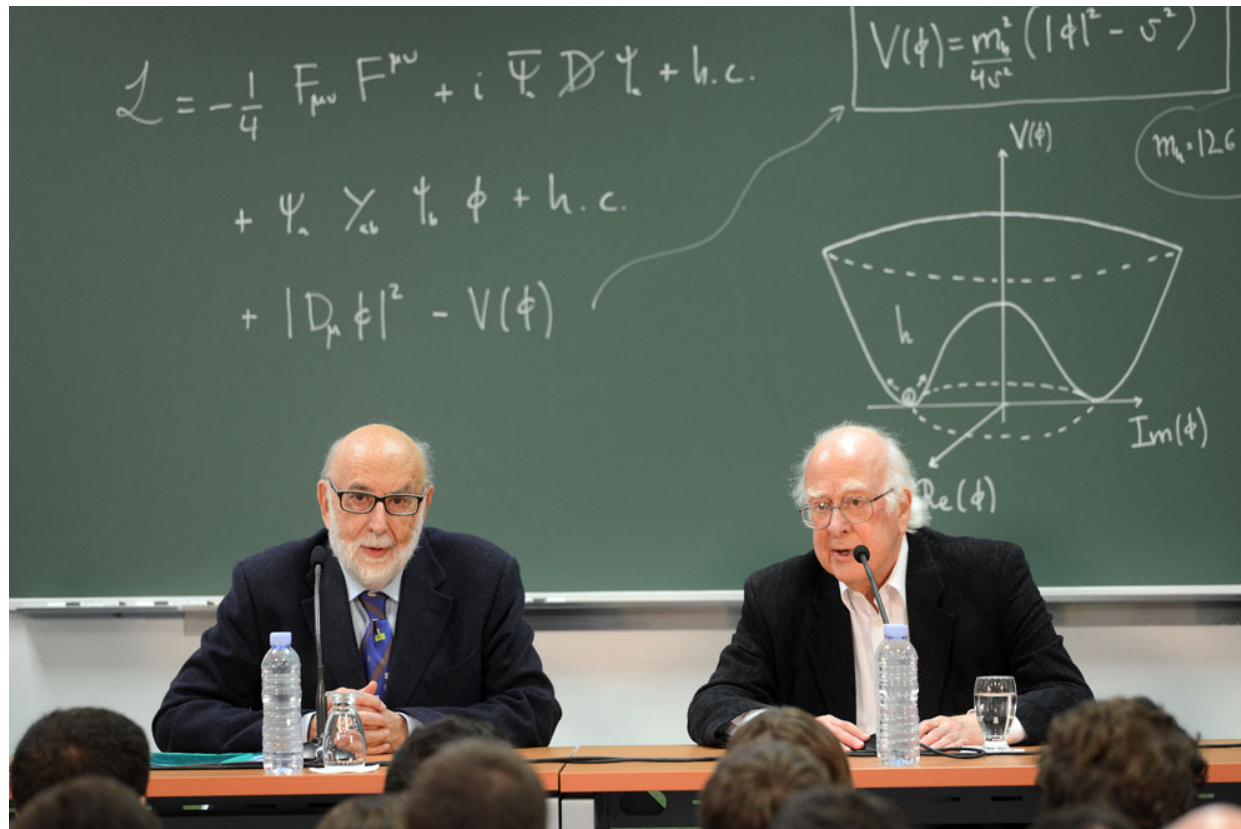


The diphoton invariant mass distribution with each event weighted by the  $S/(S+B)$  value of its category. The lines represent the fitted background and signal, and the colored bands represent the  $\pm 1$  and  $\pm 2$  standard deviation uncertainties in the background estimate. The inset shows the central part of the unweighted invariant mass distribution. Taken from Physics Letters **B716** (2012) 30—61.



Distribution of the four-lepton invariant mass for the  $ZZ \rightarrow 4$  leptons analysis. The points represent the data, the filled histograms represent the background, and the open histogram shows the signal expectation for a Higgs boson of mass  $m_H = 126$  GeV, added to the background expectation. Taken from <https://twiki.cern.ch/twiki/bin/view/CMSPublic/Hig12041TWiki>.

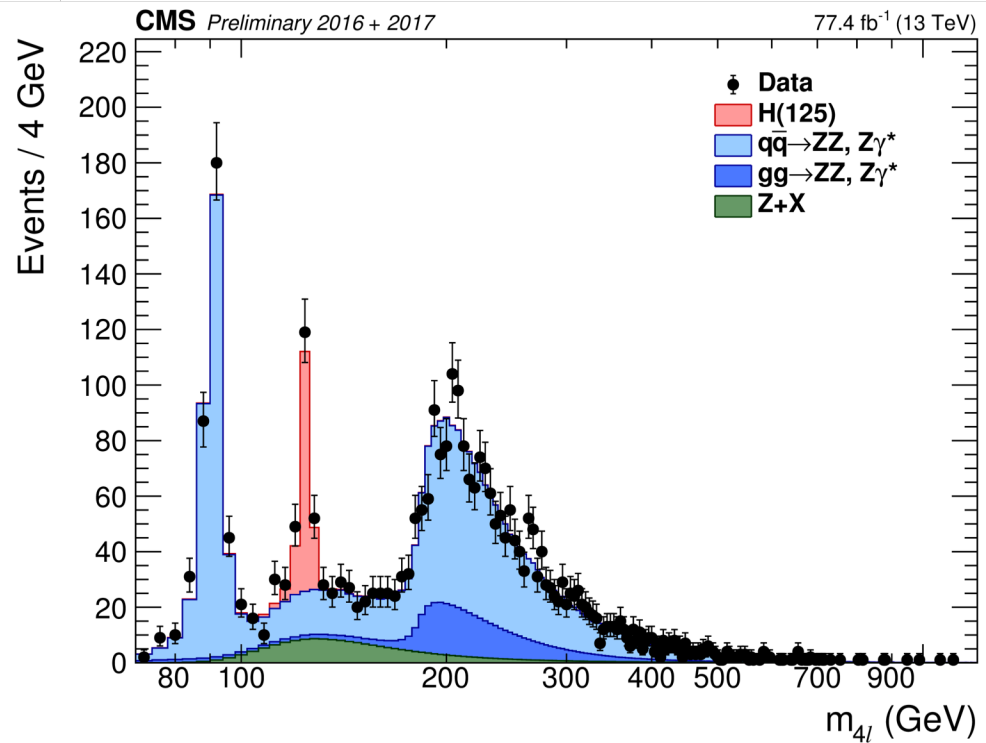
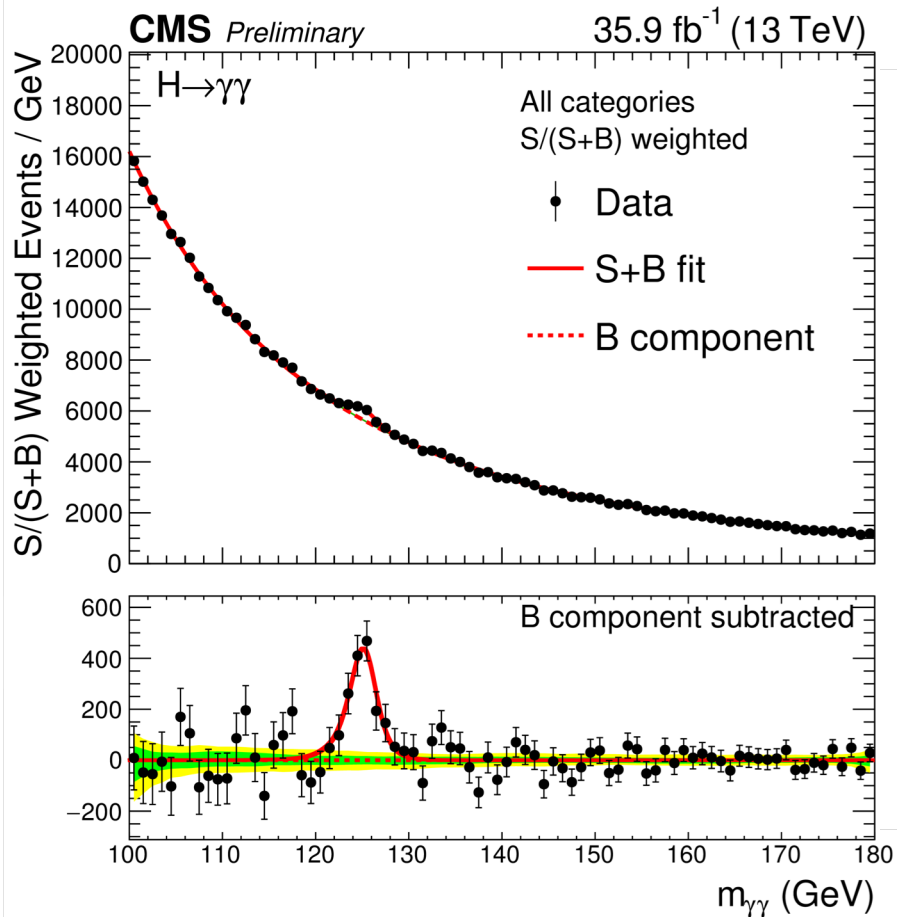
# Winners of the 2013 Nobel Prize in Physics



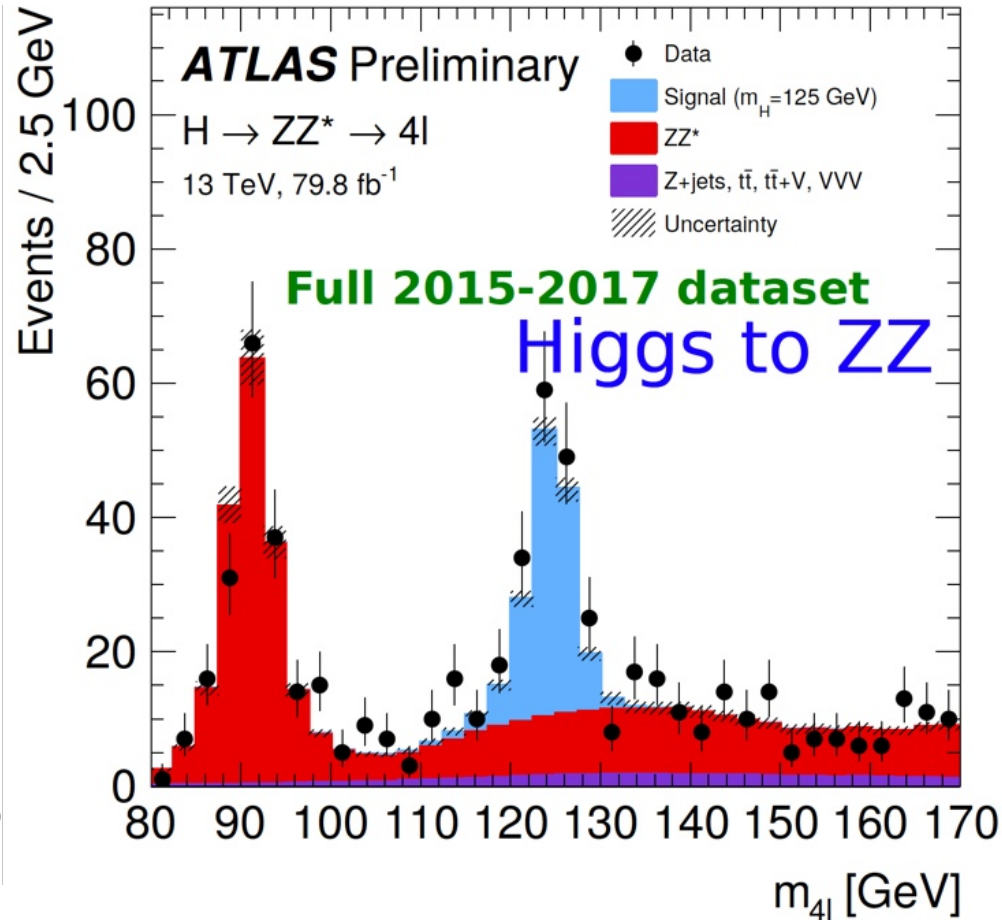
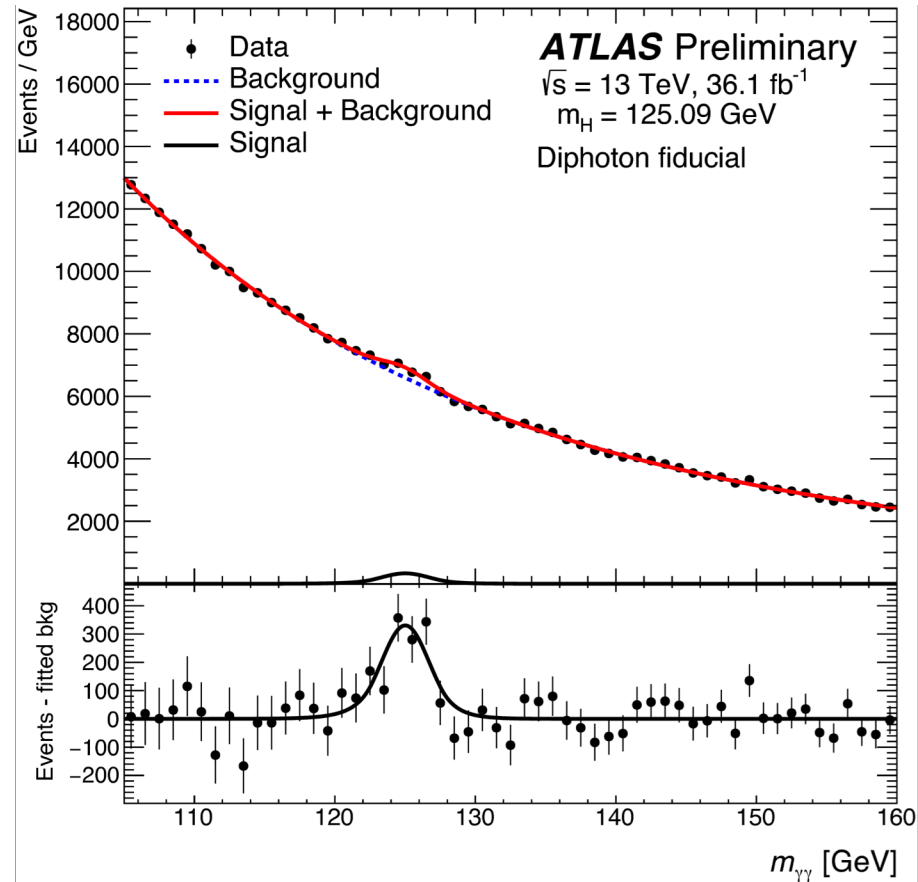
**François Englert**  
**and**  
**Peter Higgs**



# CMS Run-2 observations of the Higgs boson



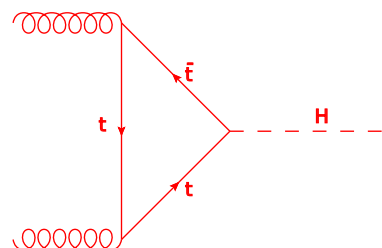
# ATLAS Run-2 observations of the Higgs boson



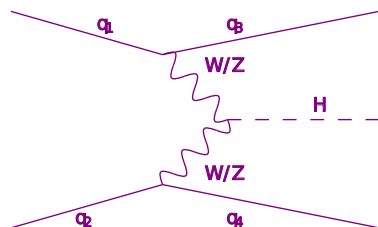
# ATLAS observed Higgs boson interactions



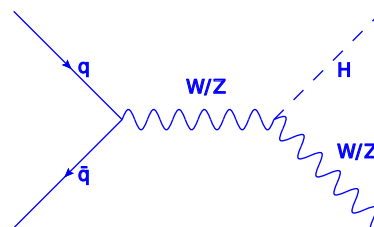
## Higgs production mechanisms



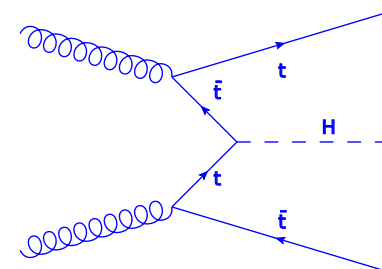
ggF  
Run 1



VBF  
Run 1 (ATLAS+CMS)  
Run 2 (ATLAS alone)

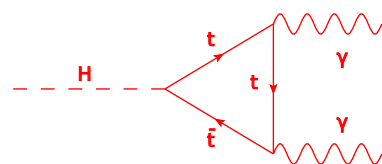


VH  
2018

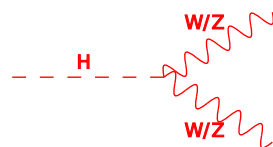


ttH  
2018

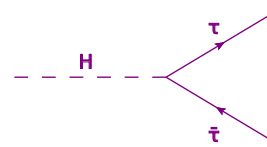
## Higgs decay modes



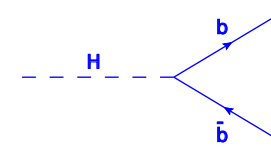
Hγγ  
Run 1



HWW/HZZ  
Run 1

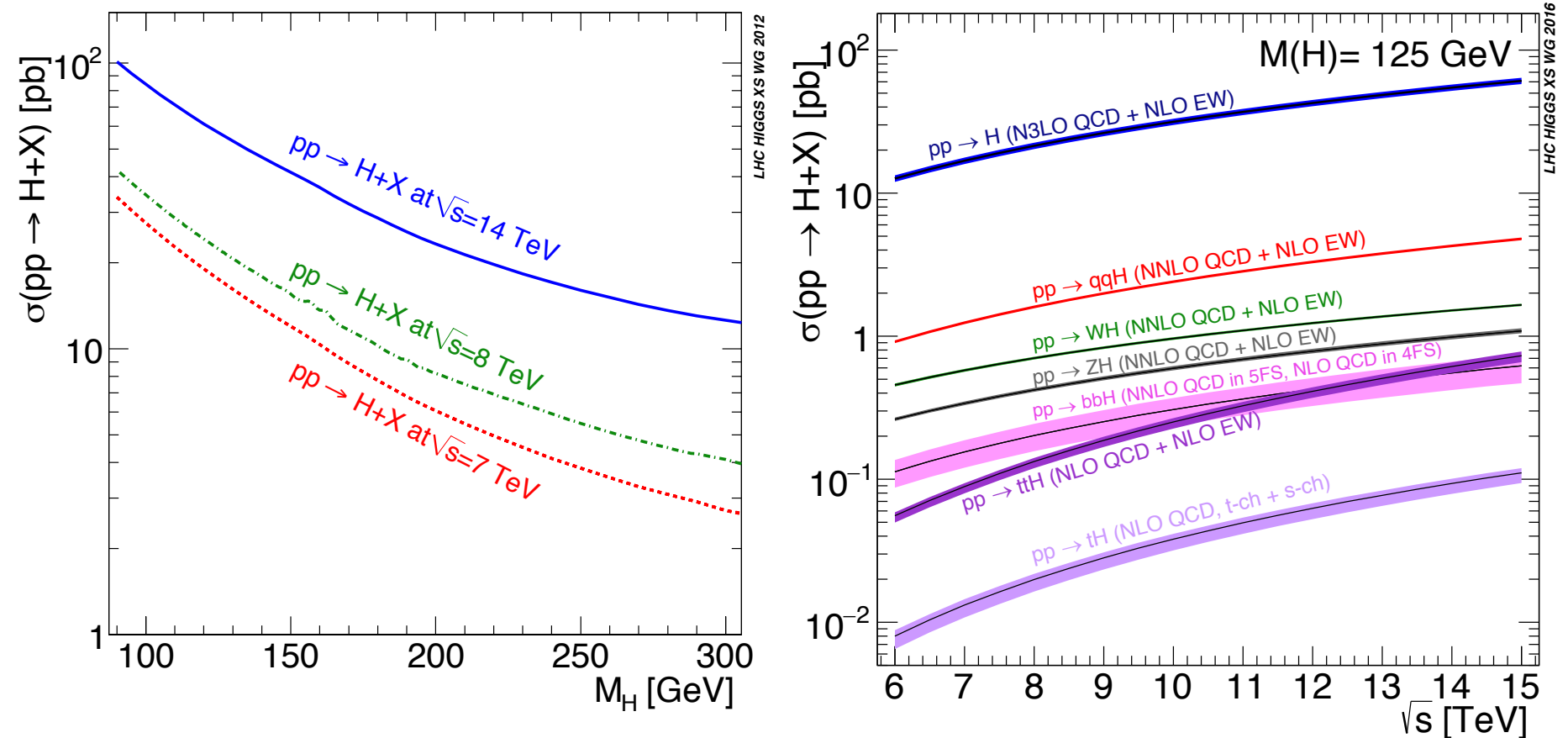


Hττ  
Run 1 (ATLAS+CMS)  
2018 (ATLAS alone)



Hbb  
2018

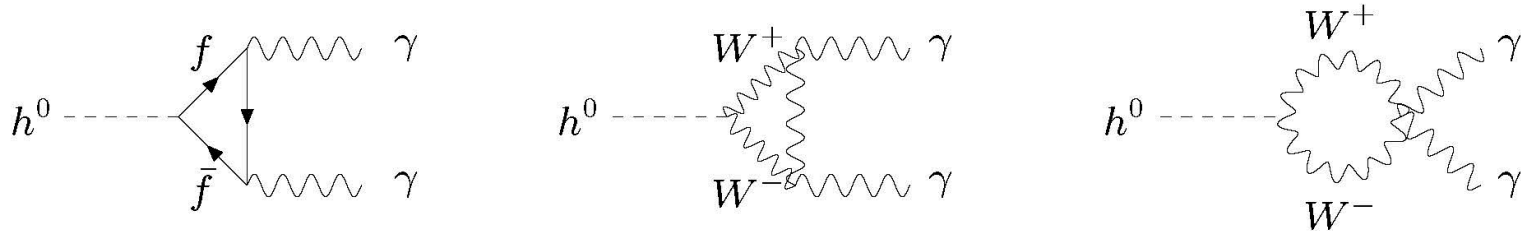
# Higgs boson production cross sections at a pp collider



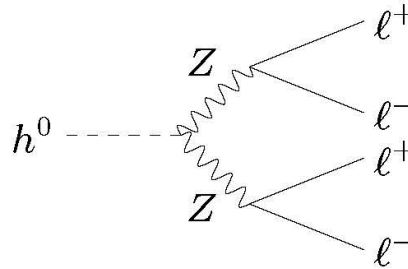
With  $40 \text{ fb}^{-1}$  of data delivered by the LHC to both ATLAS and CMS in 2015—2016 at a center of mass energy of 13 TeV, roughly 2 million Higgs bosons per experiment were produced, assuming the Higgs mass is 125 GeV. Still to be analyzed:  $50 \text{ fb}^{-1}$  of 2017 data and  $65 \text{ fb}^{-1}$  of data in 2018.

# SM Higgs decays at the LHC for $m_h \sim 125$ GeV

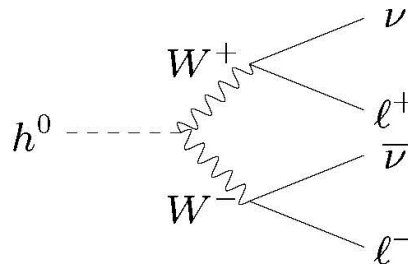
1. The rare decay  $h^0 \rightarrow \gamma\gamma$  is the most promising signal.



2. The so-called golden channel,  $h^0 \rightarrow ZZ \rightarrow \ell^+\ell^-\ell^+\ell^-$  (where one or both  $Z$  bosons are off-shell) is a rare decay for  $m_h \sim 125$  GeV, but is nevertheless visible.



3. The channel,  $h \rightarrow WW^* \rightarrow \ell^+\nu\ell^-\bar{\nu}$  is also useful, although it does not provide a good Higgs mass determination.



# Higgs boson decay channels observed at the LHC

Higgs boson decay mode	Branching ratio (for $m_h = 125 \text{ GeV}$ )
$H^0 \rightarrow b\bar{b}$	0.582
$H^0 \rightarrow \tau^+ \tau^-$	$6.27 \times 10^{-2}$
$h^0 \rightarrow \ell^+ \ell^- \nu \nu$ ( $\ell = e$ or $\mu$ )	$1.06 \times 10^{-2}$
$h^0 \rightarrow \gamma \gamma$	$2.27 \times 10^{-3}$
$h^0 \rightarrow \ell^+ \ell^- \ell^+ \ell^-$ ( $\ell = e$ or $\mu$ )	$1.24 \times 10^{-4}$

Taken from [https://twiki.cern.ch/twiki/bin/view/LHCPhysics/CERNYellowReportPageBR#Branching\\_Ratios](https://twiki.cern.ch/twiki/bin/view/LHCPhysics/CERNYellowReportPageBR#Branching_Ratios)

## Remarks:

1.  $h^0 \rightarrow WW^*$  is observed primarily via the  $\ell^+ \nu \ell^- \nu$  ( $\ell = e$  or  $\mu$ ) final state.
2.  $h^0 \rightarrow ZZ^*$  is observed primarily via the  $\ell^+ \ell^- \ell^+ \ell^-$  ( $\ell = e$  or  $\mu$ ) final state.

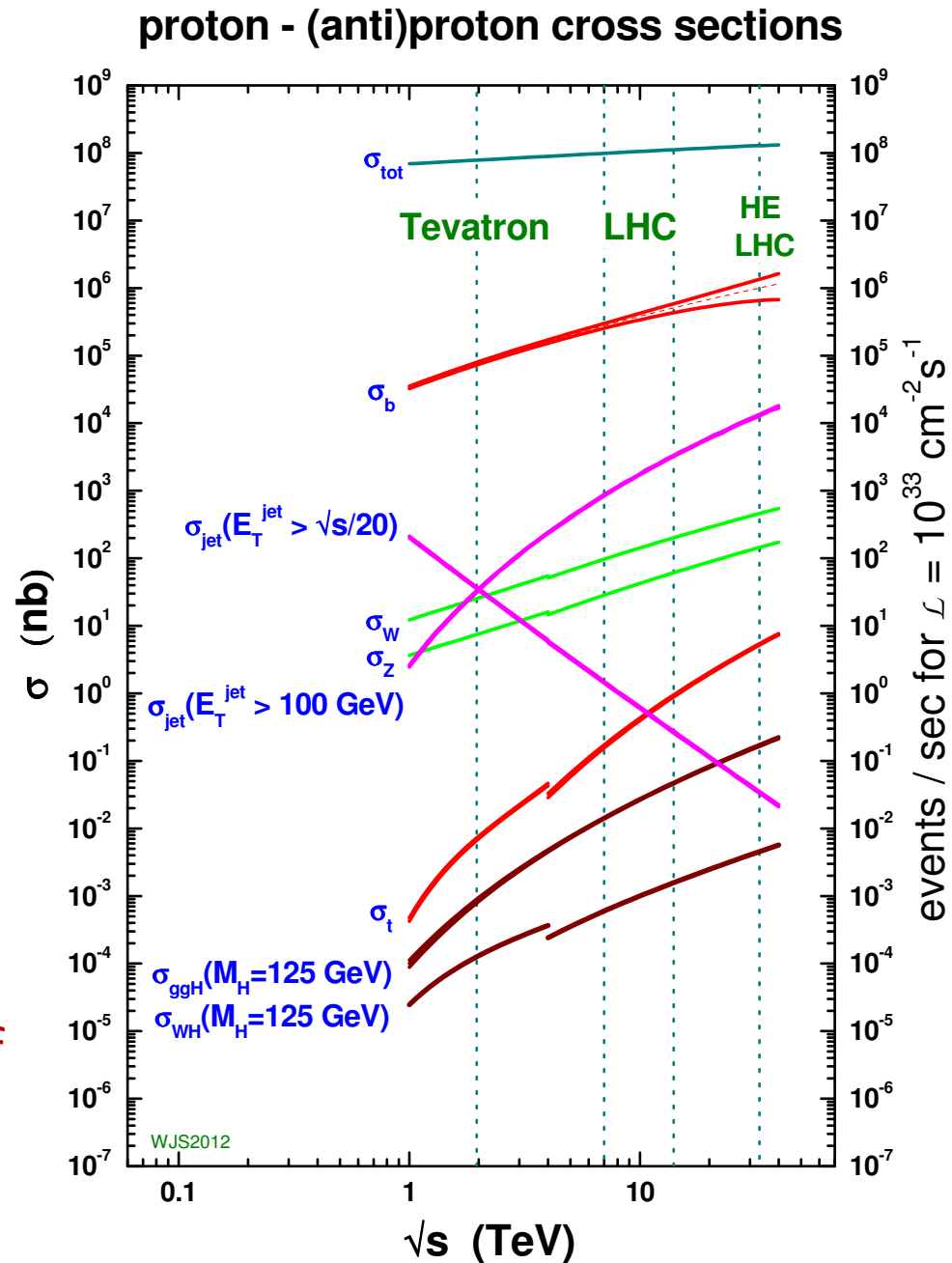
In the decays to the diboson final state, kinematics dictates that one of the vector bosons is off-shell (i.e., “virtual”) and is thus indicated by a superscript star.



Question: why not search inclusively for Higgs bosons that decay into a pair of b-quarks?

Answer: The Standard Model background is overwhelming. There are more than  $10^7$  times as many b-quark pairs produced in proton-proton collisions as compared to b-quark pairs that arise from a decaying Higgs boson.

Nevertheless, the observation of  $H \rightarrow b\bar{b}$  in the VH channel was confirmed by ATLAS and CMS in 2018!

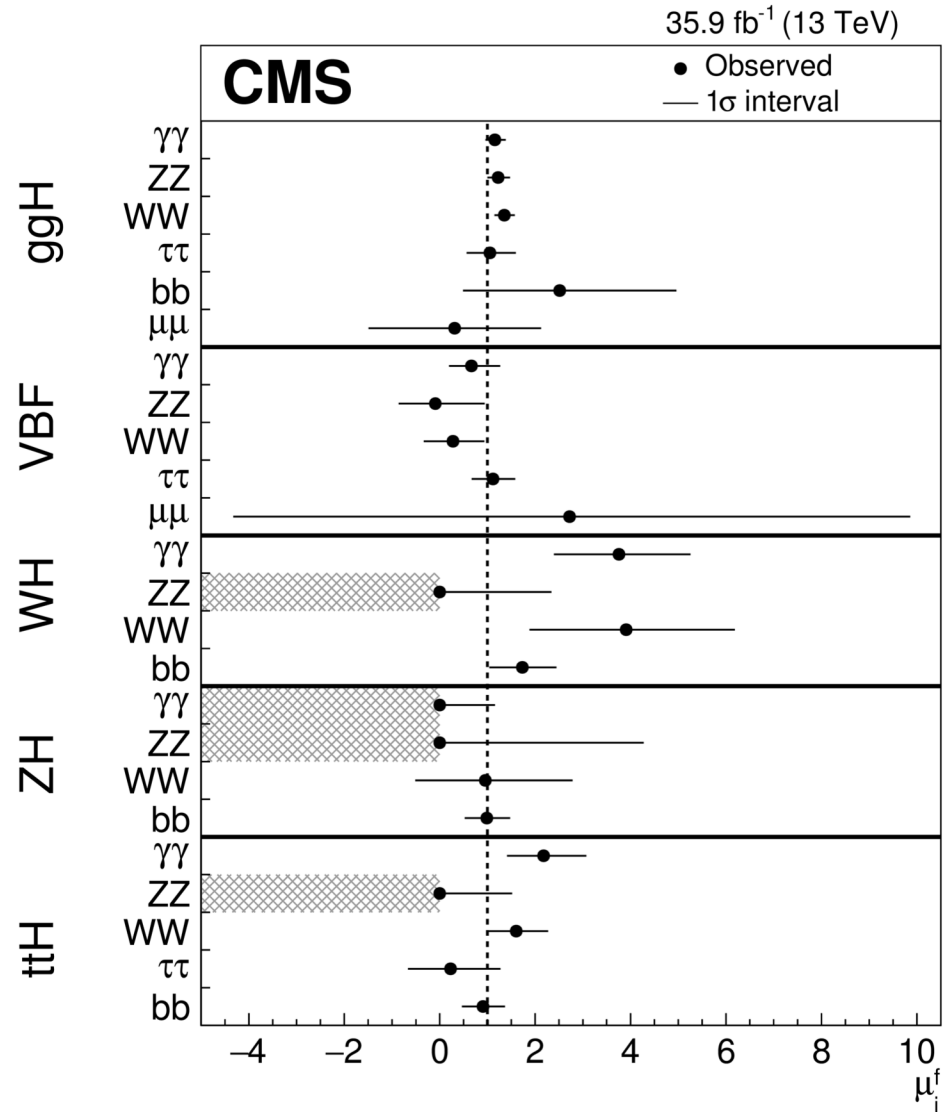


# Is the observed 125 GeV scalar the SM Higgs boson?

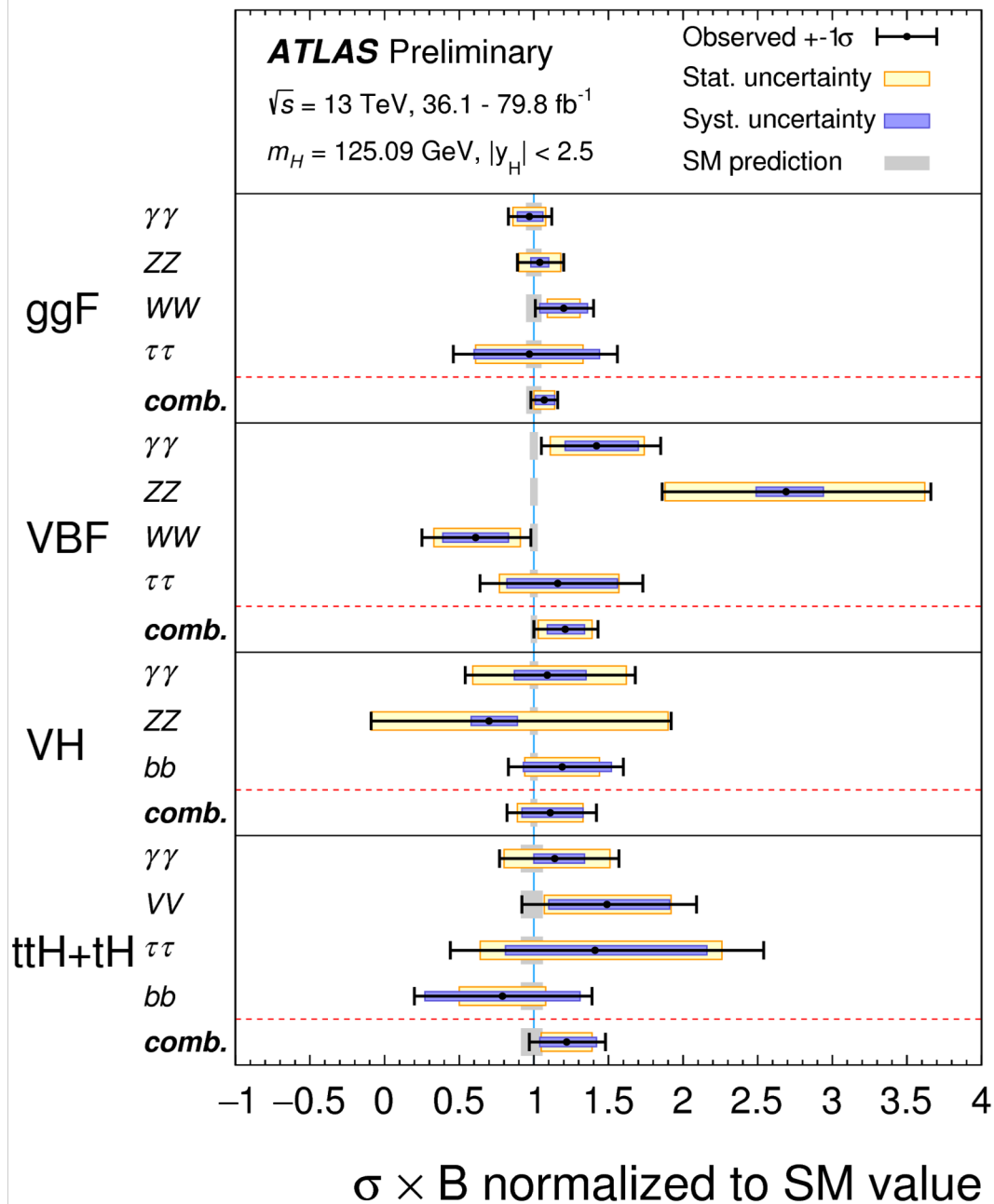
After the end of Run-1 of the LHC (2011—2013), the ATLAS and CMS Collaborations provided a combined analysis of the Higgs boson data.

The properties of the Higgs boson were consistent with Standard Model predictions (within the statistical power of the Higgs boson data).

The Higgs data taken at Run-2 of the LHC (2015—2016) have confirmed the Run-1 observations (with potential deviations from the Standard Model further reduced).

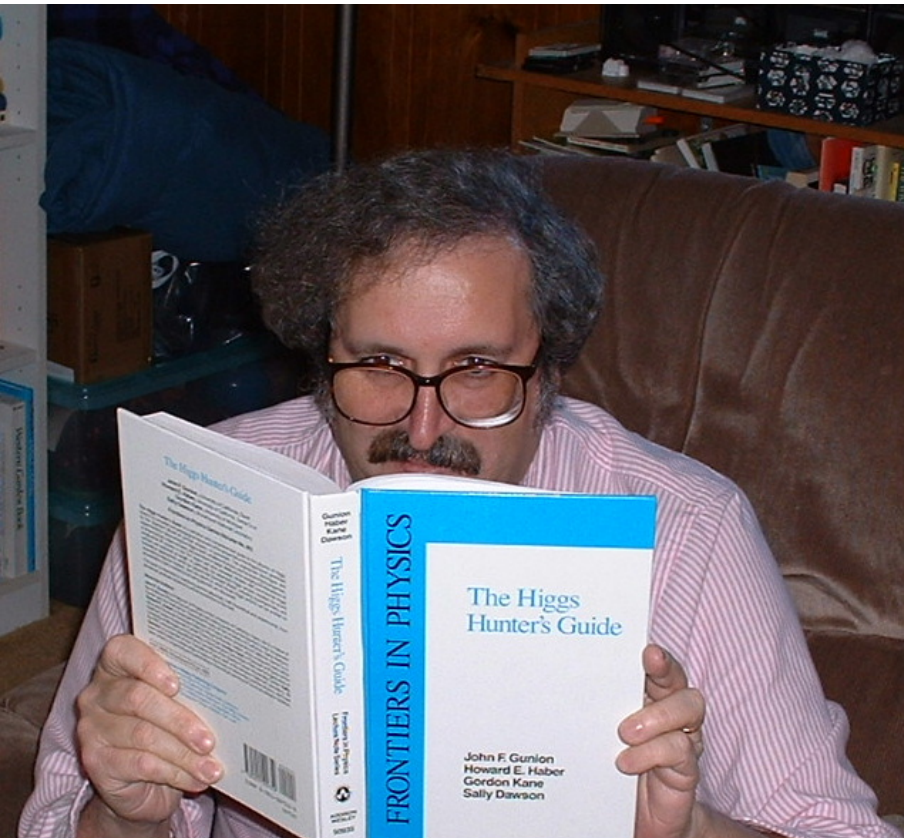


Taken from A.M. Sirunyan et al. [CMS Collaboration], arXiv:1809.10733.



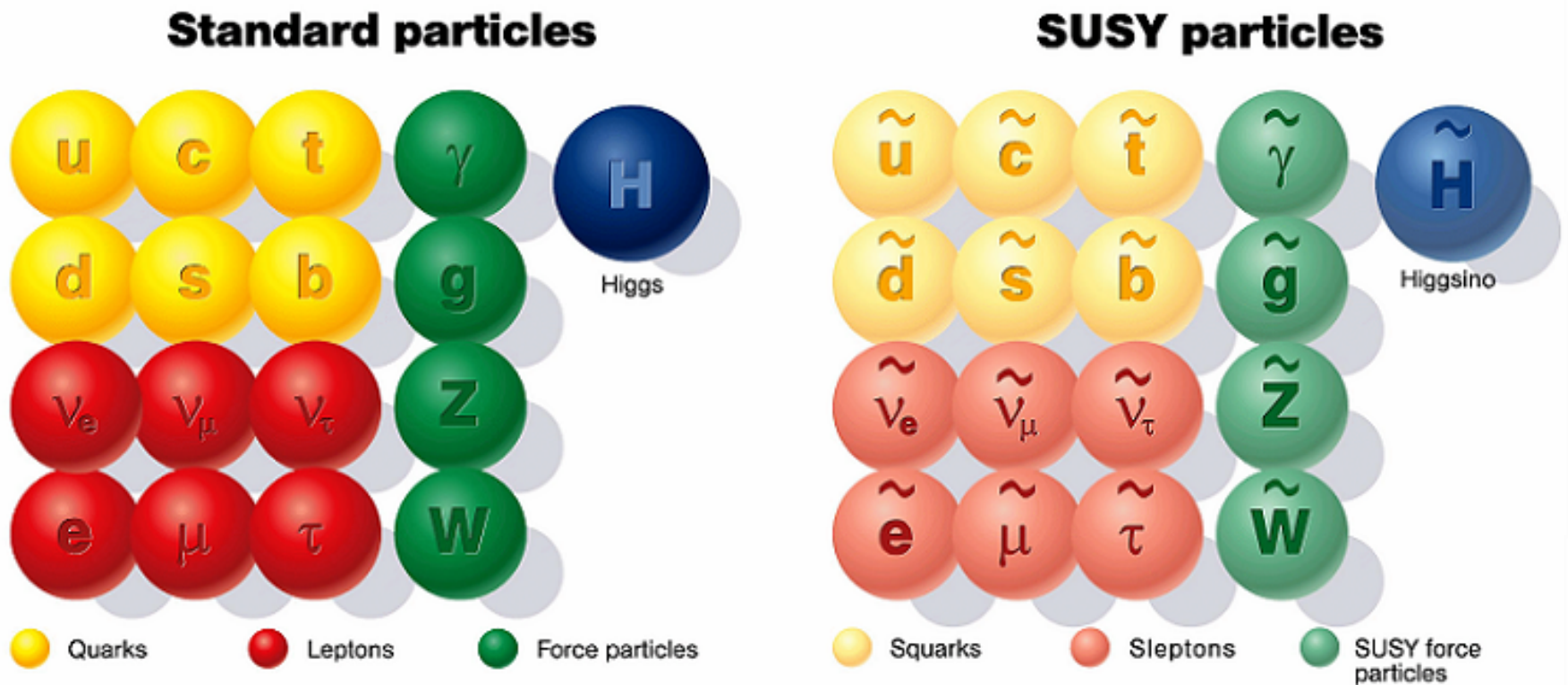
Taken from ATLAS collaboration,  
 ATLAS-CONF-2018-031,  
 presented at the  
 XXXIX International Conference  
 on High Energy Physics in  
 Seoul, Korea, 4—11 July 2018

# Research program 1: theory and phenomenology of Higgs bosons





# Research program 2: theory and phenomenology of TeV-scale supersymmetry (SUSY)



For a review, see H.E. Haber, *Supersymmetry Theory*, in M. Tanabashi et al. [Particle Data Group Collaboration], *Review of Particle Physics*, Phys. Rev. D **98**, 030001 (2018) pp. 790—806.

You may be alone now,  
but there *is* hope.



There is a theory that says  
that, for each one of you,  
there is a partner for you  
somewhere out there.



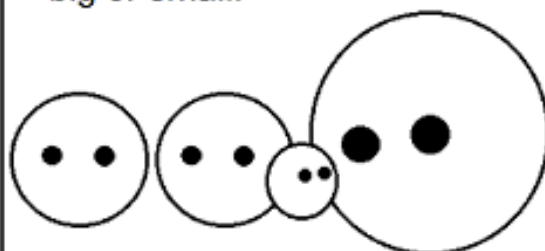
Your partner simply  
hasn't been found yet.



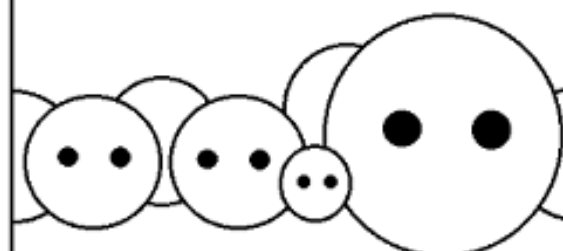
It doesn't matter what you look  
like; it doesn't matter whether  
you're attractive or not.



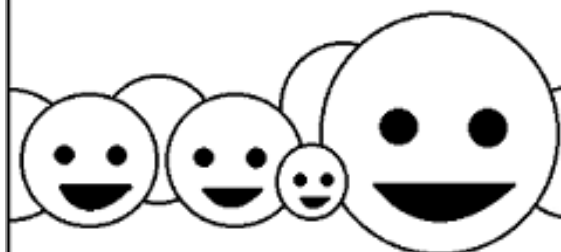
It doesn't matter how much  
you weigh; whether you're  
big or small.



It doesn't matter what your  
personality is like; whether  
you're charming or strange.



According to this theory, there is  
a partner out there for each and  
every one of you.



Unfortunately, there is no  
compelling evidence to  
support this theory yet.



So SUSY is probably wrong and  
you're all SOL.





# As a member of the Particle Data Group, I am the author of the biennial Supersymmetry Theory review

## PHYSICAL REVIEW D

Articles Published in AUGUST 2018  
D1  
PART A

*covering particles, fields,  
gravitation, and cosmology*

### Review of Particle Physics

M. Tanabashi *et al.* (Particle Data Group), Phys. Rev. D 98, 030001 (2018)



Published by  
AMERICAN PHYSICAL SOCIETY



Volume 98

Third Series

Number 3

## 790 109. Supersymmetry, part I (theory)

### 109. Supersymmetry, Part I (Theory)

Revised September 2017 by Howard E. Haber (UC Santa Cruz).

#### 109.1 Introduction

#### 109.2 Structure of the MSSM

109.2.1 R-parity and the lightest supersymmetric particle

109.2.2 The goldstino and gravitino

109.2.3 Hidden sectors and the structure of supersymmetry-breaking

109.2.4 Supersymmetry and extra dimensions

109.2.5 Split-supersymmetry

#### 109.3 Parameters of the MSSM

109.3.1 The supersymmetry-conserving parameters

109.3.2 The supersymmetry-breaking parameters

109.3.3 MSSM-124

#### 109.4 The supersymmetric-particle spectrum

109.4.1 The charginos and neutralinos

109.4.2 The squarks, sleptons and sneutrinos

#### 109.5 The supersymmetric Higgs sector

109.5.1 The tree-level Higgs sector

109.5.2 The radiatively-corrected Higgs sector

#### 109.6 Restricting the MSSM parameter freedom

109.6.1 Gaugino mass relations

109.6.2 The constrained MSSM: mSUGRA, CMSSM, ...

109.6.3 Gauge-mediated supersymmetry breaking

109.6.4 The phenomenological MSSM

109.6.5 Simplified Models

#### 109.7 Experimental data confronts the MSSM

109.7.1 Naturalness constraints and the little hierarchy

109.7.2 Constraints from virtual exchange of supersymmetric particles

#### 109.8 Massive neutrinos in weak-scale supersymmetry

109.8.1 The supersymmetric seesaw

109.8.2 R-parity-violating supersymmetry

#### 109.9 Extensions beyond the MSSM

#### 109.1. Introduction

Supersymmetry (SUSY) is a generalization of the space-time symmetries of quantum field theory that transforms fermions into bosons and vice versa [1]. The existence of such a non-trivial extension

electroweak symmetry breaking, provides a natural origin and the stability of the gauge hierarchy.

At present, there is no unambiguous prediction for the breakdown of the Standard Model at the TeV scale. The expectations for new TeV-scale physics are based primarily on three theoretical considerations: a theory with an elementary scalar field of strength  $\lambda$  (e.g., a quartic scalar self-coupling or the square of a Yukawa coupling) respect to quantum corrections requires a cutoff roughly of order  $(16\pi^2/\lambda)^{1/2}m$ , but must enter [14]. A significantly larger energy scale is an unnatural fine-tuning of parameters in the theory. Applying this argument to the Standard Model expectation of new physics at the TeV scale.

Second, the unification of the three Standard Model gauge couplings at a very high energy close to the Planck scale physics beyond the Standard Model (where the gauge couplings above the electroweak scale unify) minimal supersymmetric extension of the Standard Model where superpartner masses lie below a few TeV of successful gauge coupling unification [1].

Third, the existence of dark matter, which is one quarter of the energy density of the universe within the Standard Model of particle physics. Stable weakly-interacting massive particle (WIMP) interaction rate are governed by new physics at the TeV-scale can be consistent with the observed relic density (this is the so-called WIMP miracle, which is the lightest supersymmetric particle, if stable, is a natural candidate for the dark matter of dark matter can be found in Ref. 23).

#### 109.2. Structure of the MSSM

The minimal supersymmetric extension of the Standard Model consists of the fields of the two-Higgs-doublet Standard Model and the corresponding superpartners: a particle and its superpartner together form a supermultiplet. The field content of the supersymmetric extension is summarized in Table 1.

## Research program 3: explorations of the Terascale at present and future colliders (LHC and ILC)

- Studies of the non-minimal Higgs sector
- Precision measurements of new physics observables
- Distinguishing among different theoretical interpretations of new physics signals
- Employing the ILC as a precision Higgs factory
- Terascale footprints of lepton-number-violating physics (e.g. R-parity-violation or the SUSY seesaw)
- New sources for CP-violation (Higgs and/or SUSY mediated)

# 2018--19 Publications

## Symmetries and Mass Degeneracies in the Scalar Sector

H.E. Haber, O.M. Ogreid, Per Osland and M.N. Rebelo, JHEP **1901** (2019) 042.

## Heavy Higgs boson decays in the alignment limit of the 2HDM

B. Grzadkowski, H.E. Haber, O.M. Ogreid and Per Osland, JHEP **1812** (2018) 056.

## Multi-Higgs doublet models: the Higgs-fermion couplings and their sum rules

M.P. Bento, H.E. Haber, J.C. Romão and J.P. Silva, JHEP **1810** (2018) 143.

## Viewpoint: Higgs Decay into Bottom Quarks Seen at Last

H.E. Haber, APS Physics **11** (2018) 91.

## Approximate Higgs alignment without decoupling

H.E. Haber, in the Proceedings of the 53th Rencontres de Moriond, QCD Session, March 17—24, 2018, in La Thuile, Aosta Valley, Italy, edited by E. Augé, J. Dumarchez and J. Trân Thanh Vân (ARISF Publishers, France, 2018) pp. 139–142.

## Supersymmetric Theory and Models

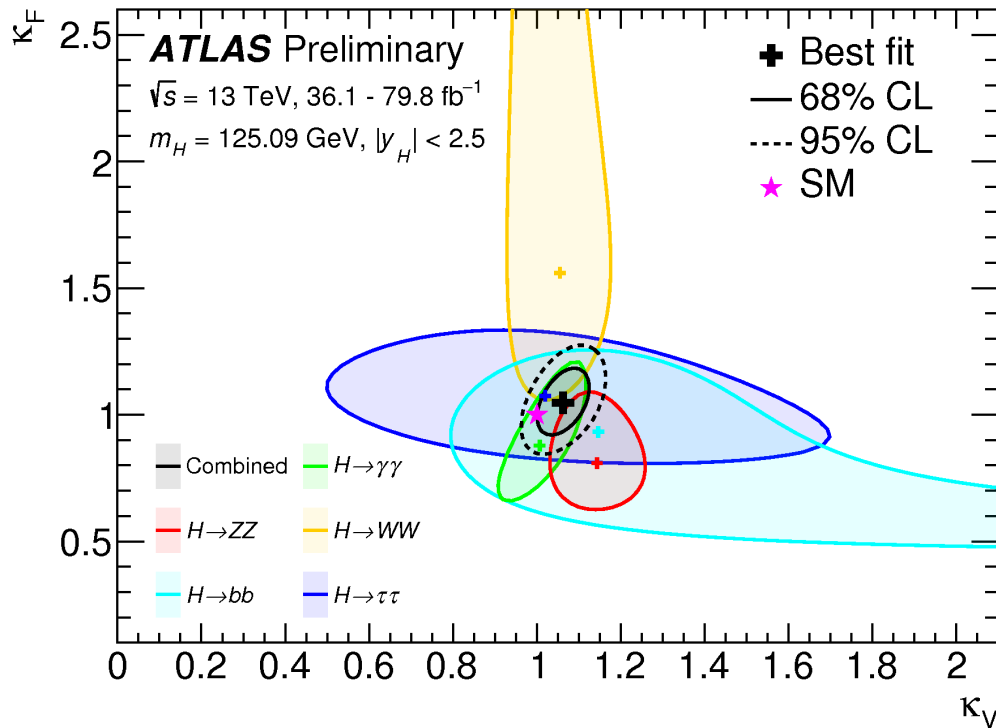
H.E. Haber and **L. Stephenson Haskins**, arXiv:1712.05926 [hep-ph], in Chapter 6 of [\*TASI 2016: Anticipating the Next Discoveries in Particle Physics\*](#), edited by Rouven Essig and Ian Low (World Scientific, Singapore, 2018) pp. 355--499.

UCSC graduate student authors in **red**.

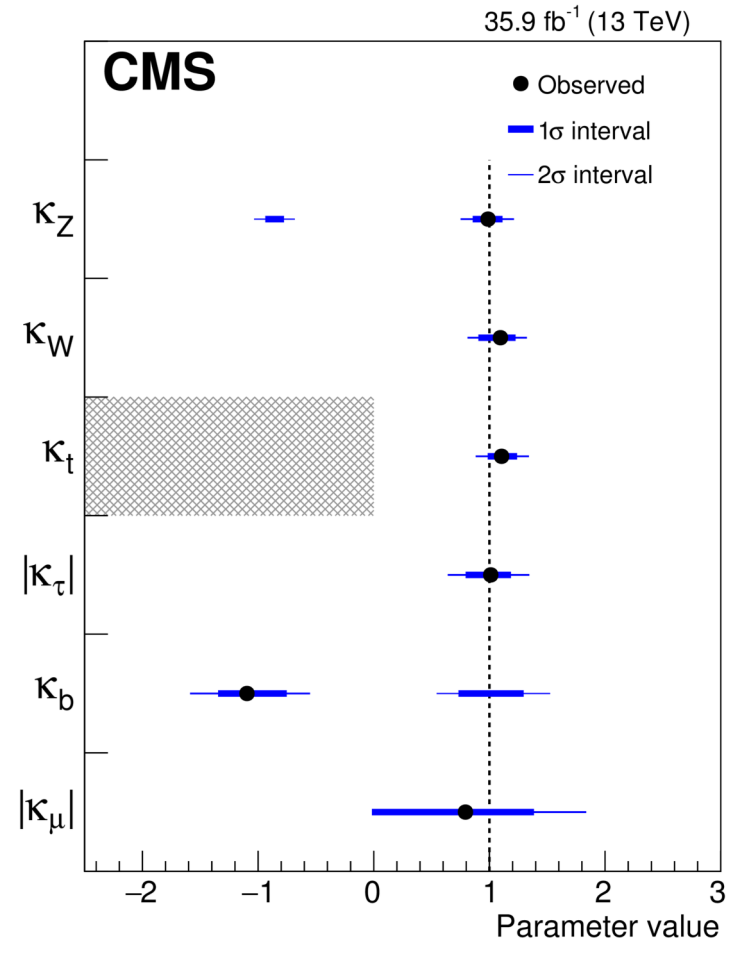
# Should we expect an extended Higgs sector beyond the SM?

- The fermion and gauge boson sectors of the SM are not of minimal form (“who ordered that?”). So, why should the spin-0 (scalar) sector be minimal?
- Adding new scalar states can alleviate the metastability of the vacuum, allowing the Higgs-sector-extended SM to be valid all the way up to the Planck scale.
- Extended Higgs sectors can provide a dark matter candidate.
- Extended Higgs sectors can provide new sources of CP violation (which may be useful in baryogenesis).
- Models of physics beyond the SM often require additional scalar Higgs states. E.g., two Higgs doublets are required in the minimal supersymmetric extension of the SM (MSSM).

# Search for deviations from SM-Higgs couplings



Negative log-likelihood contours at 68% and 95% CL in the  $(\kappa_F, \kappa_V)$  for the individual decay channels and the combined fit. The crosses indicate the best-fit values and the star the Standard Model prediction. Taken from ATLAS collaboration, ATLAS-CONF-2018-031.



Summary of the  $\kappa$  framework model assuming that there are no additional BSM contributions to the Higgs boson width, i.e.  $\text{BR}_{\text{BSM}} = 0$ . The points indicate the best fit values while the thick and thin horizontal bars show the 1σ and 2σ CL intervals, respectively. Taken from A.M. Sirunyan et al. [CMS Collaboration], arXiv:1809.10733.



# A tale of two alignment mechanisms

## 1. Higgs field alignment

In the limit in which one of the Higgs mass eigenstate fields is approximately aligned with the direction of the scalar doublet vacuum expectation value (vev) in field space, the tree-level properties of corresponding scalar mass eigenstate approximate those of the SM Higgs boson.

## 2. Flavor alignment

The quark mass matrices arise from the Higgs-fermion Yukawa couplings when the neutral Higgs fields acquire vevs. In the case of flavor alignment, the diagonalization of the quark mass matrices simultaneously diagonalize the neutral Higgs quark interactions, which implies the absence of tree-level Higgs-mediated FCNCs in hadron physics.



# Higgs field alignment with or without decoupling

## 1. The decoupling limit

Approximate Higgs field alignment is most naturally achieved in the decoupling limit, where there is a new mass parameter,  $M \gg v$ , such that all physical Higgs masses with one exception are of  $\mathcal{O}(M)$ . The Higgs boson, with  $m_h \sim \mathcal{O}(v)$ , is SM-like, due to approximate alignment.

## 2. Higgs field alignment without decoupling<sup>4</sup>

In models of alignment without decoupling (due to suppressed scalar mixing), the masses of all Higgs scalars (both SM-like and non-SM-like) can be of  $\mathcal{O}(v)$ . Hence, the non-SM Higgs scalars may be more easily accessible at the LHC. In some theories, this can be achieved by a symmetry (e.g., the inert doublet model). In most cases, approximate alignment is an accidental (fine-tuned?) region of the model parameter space.

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<sup>4</sup>J.F. Gunion and H.E. Haber, hep-ph/0207010; N. Craig, J. Galloway and S. Thomas, arXiv:1305.2424.

# Evidence for new physics beyond the SM in B decays to muon pairs?

Recent results from LHCb and CMS at the LHC yield the following branching ratios (BR):

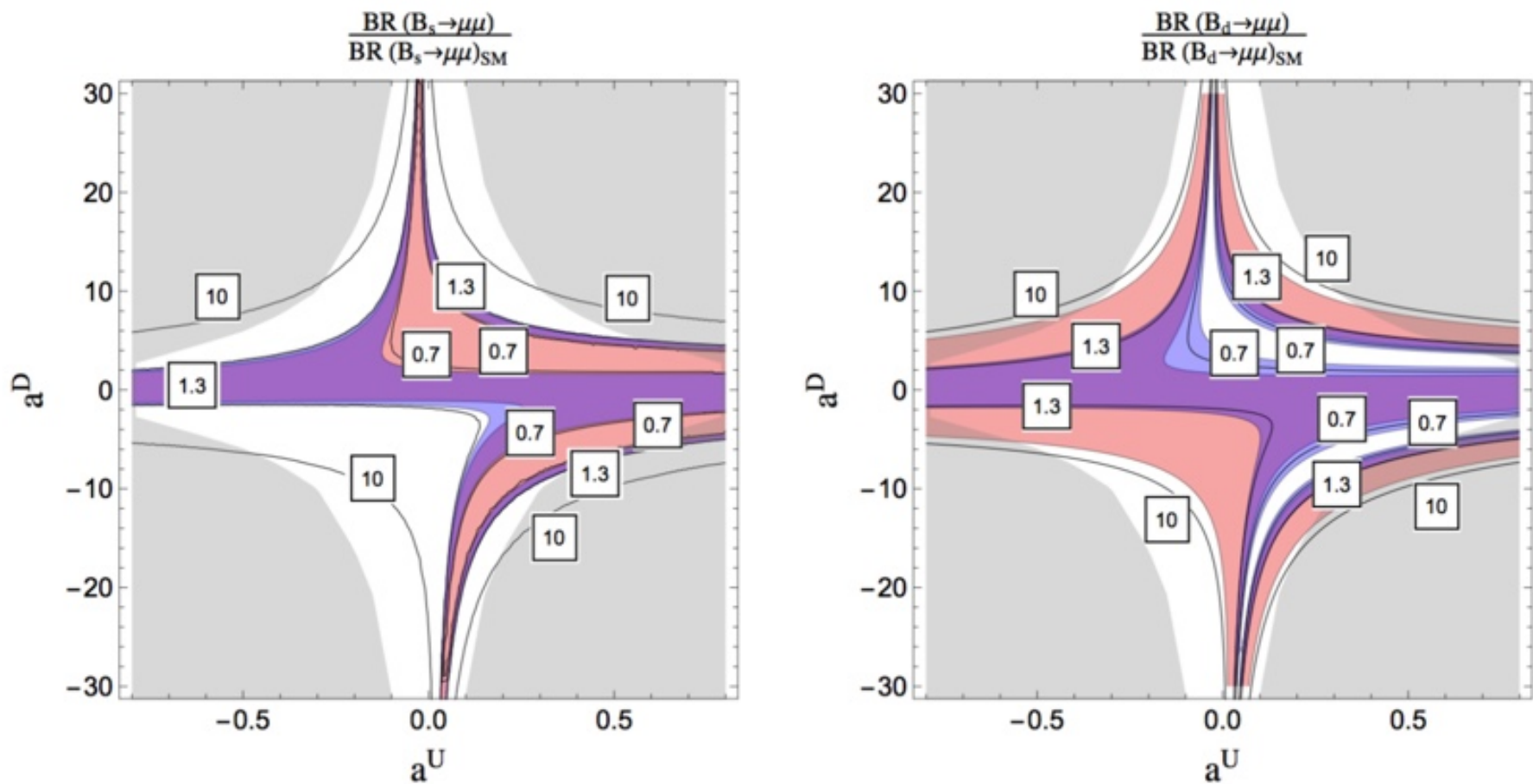
$$\begin{aligned} \text{BR}(B_s \rightarrow \mu^+ \mu^-)_{exp} &= (2.8_{-0.6}^{+0.7}) \times 10^{-9}, \\ \text{BR}(B_d \rightarrow \mu^+ \mu^-)_{exp} &= (3.9_{-1.4}^{+1.6}) \times 10^{-10} \end{aligned}$$

which should be compared with the SM predictions,

$$\begin{aligned} \text{BR}(B_s \rightarrow \mu^+ \mu^-)_{SM} &= (3.65 \pm 0.23) \times 10^{-9}, \\ \text{BR}(B_d \rightarrow \mu^+ \mu^-)_{SM} &= (1.06 \pm 0.09) \times 10^{-10}, \end{aligned}$$

In S. Gori, H.E. Haber and E. Santos, JHEP **1706** (2017) 110, new contributions to these decays were considered in the two Higgs doublet model (2HDM) where flavor alignment is imposed at very high energies. However, renormalization group running generates small flavor-changing neutral Higgs couplings that do not exist in the SM and can contribute to neutral B decays.

The present data already puts interesting constraints on the flavor alignment parameters  $a^U$  and  $a^D$  of our model.



**Figure 7.** Leading log prediction for the branching ratios for  $B_s \rightarrow \mu^+ \mu^-$  (left panel) and  $B_d \rightarrow \mu^+ \mu^-$  (right panel) relative the SM, as a function of  $a^U$  and  $a^D$ , with fixed  $\tan \beta = 10$ ,  $\cos(\beta - \alpha) = 0$ , and  $m_A = m_H = 400$  GeV. The regions in pink are allowed at the  $2\sigma$  level by the present measurements. The purple shaded regions are anticipated by the more precise HL-LHC measurements, assuming a measured central value equal to the SM prediction. The gray shaded regions produce Landau poles in the Yukawa couplings below  $M_P$ .

# Exploring some consequences of the Ivanov-Silva 3HDM

$$J_1 = Z_1, \quad (\text{A.71})$$

$$J_2 = Z_1 + 2Z_3, \quad (\text{A.72})$$

$$J_3 = Z_1 + 2Z_4, \quad (\text{A.73})$$

$$J_4 = Z_1^2 + 2Z_3^2 + 2Z_4^2 + 2Z_5^2, \quad (\text{A.74})$$

$$J_5 = Z_1^3 + 4Z_5^2 Z_1 + 2Z_3^3 + 6Z_3 Z_4^2 + 2Z_2 Z_5^2 + 4Z_5^2 \text{Re } Z_8, \quad (\text{A.75})$$

$$J_6 = Z_1^4 + 2Z_3^4 + 2Z_4^4 + 12Z_3^2 Z_4^2 + 4Z_5^4 + 2Z_5^2 (3Z_1^2 + 2Z_1 Z_2 + Z_2^2) + 8Z_5^2 [|Z_8|^2 + (Z_1 + Z_2) \text{Re } Z_8 + (\text{Im } Z_9)^2]. \quad (\text{A.76})$$

Using the first four invariant quantities above, one can show that  $Z_5$  can be expressed in terms of an invariant quantity.<sup>45</sup> In particular,

$$Z_5^2 = -J_1^2 + \frac{1}{2} J_1 (J_2 + J_3) - \frac{1}{4} (J_2^2 + J_3^2) + \frac{1}{2} J_4. \quad (\text{A.77})$$

Finally, we have discovered a remarkable invariant quantity,

$$\begin{aligned} \mathcal{N} = & 32Z_5^2 J_6 - 16J_5^2 + 8J_5(3J_{21}J_{31}^2 + K) - J_{31}^4(9J_{21}^2 + 4Z_5^2) - 6KJ_{21}J_{31}^2 - 24Z_5^2 J_{21}^2 J_{31}^2 \\ & - J_{21}^6 - 4Z_5^2 J_{21}^4 - 8J_1(J_1^2 + 2Z_5^2)J_{21}^3 - 16J_1^6 - 96Z_5^2 J_1^4 - 192Z_5^4 J_1^2 - 128Z_5^6, \end{aligned} \quad (\text{A.78})$$

where  $J_{ij} \equiv J_i - J_j$ , the invariant quantity  $Z_5^2$  is given by Eq. (A.77) and

$$K \equiv 4J_1^3 + 8Z_5^2 J_1 + J_{21}^3. \quad (\text{A.79})$$

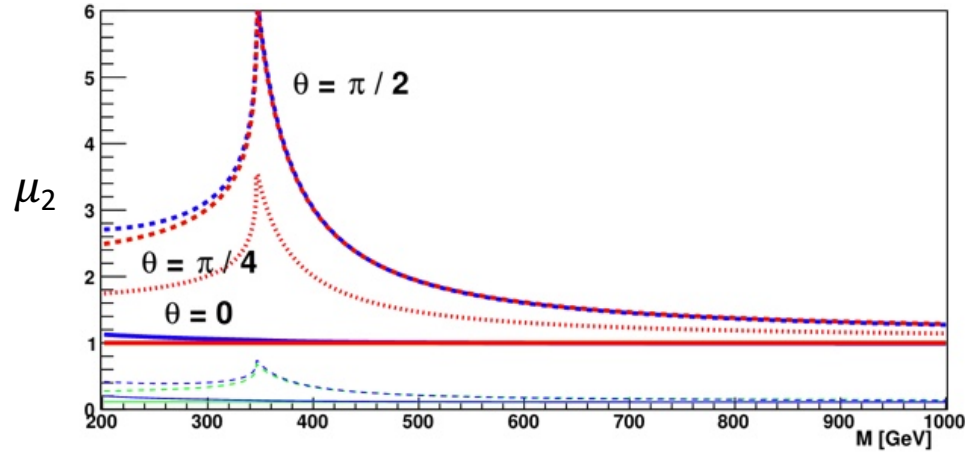
Plugging in the expressions for  $J_1, \dots, J_6$  given above, we find

$$\mathcal{N} = 256Z_5^4 [(\text{Im } Z_8)^2 + (\text{Im } Z_9)^2]. \quad (\text{A.80})$$

The physical consequence of the non-vanishing of this invariant quantity is the existence of a coupling of  $Z$  to four mass-degenerate inert scalars. For more details, see H.E. Haber, O.M. Ogreid, Per Osland and M.N. Rebelo, JHEP **1901** (2019) 042.



# Exploring heavy Higgs boson decays in the alignment limit of the 2HDM



**Figure 1.** Cross section ratios  $\mu_2$  for  $gg$  production of  $H_2$  for  $\bar{\rho}^q$  defined by eq. (4.38). Here, for illustration we assume that phases of  $\hat{\rho}^q$  are the same for up- and down-type quarks, so  $\theta_u = \theta_d = \theta$ . Red, heavy: general model with  $|\hat{\rho}^u| = |\hat{\rho}^d| = 1$  with (solid)  $\theta = 0$ , (dotted)  $\theta = \pi/4$  and (dashed)  $\theta = \pi/2$ . Blue (green) heavy solid: Type II (Type I) for  $\tan \beta = 1$  with  $\alpha_3 = 0$  (so  $H_3 = A$ ). Dashed, same with  $\alpha_3 = \pi/2$  (so  $H_2 = A$ ). Thin (blue and green) Type I and Type II with  $\tan \beta = 3$ . (The green curves, for Type I, are partly covered by the red and blue ones.) The spike at  $M = 2m_t$  originates from the function  $\text{Re } B$  of eq. (F.2) describing the pseudoscalar coupling.

To illustrate effects of generic Yukawa couplings in the production of  $H_{2,3}$  we define

$$\mu_\alpha \equiv \frac{\sigma_\alpha}{\sigma_{\text{SM}}} = \frac{X_\alpha^2}{|A|_{\text{SM}}^2}, \quad (5.4)$$

where  $\alpha = 2, 3$ ,  $\sigma_\alpha$  is the  $pp \rightarrow H_\alpha$   $gg$  cross section in the 2HDM,  $\sigma_{\text{SM}}$  is the corresponding SM cross section, and  $X_2^2$  is given by eq. (5.2). Here,  $A_{\text{SM}}$  refers to the function (F.1), summed over  $t$  and  $b$ -quark loops. In figure 1 we plot this quantity for  $\alpha = 2$ .

# My recent Ph.D. students and their thesis projects

John Mason (2008): Hard Supersymmetry-Breaking “Wrong-Higgs” Couplings of the MSSM

Deva O’Neil (2009): Phenomenology of the Basis-Independent CP-Violating Two-Higgs Doublet Model (2HDM)

Laura Fava (2015): Precision Measurement of UED Coupling Constants Using Like-Sign Leptons at the LHC

Edward Santos (2015): Renormalization Group Constraints on the Two-Higgs Doublet Model

## Where are they now?

J. Mason – following a three-year post doctoral research associate in particle theory at Harvard University, John accepted a position as an associate professor of physics at Western State College of Colorado

D. O’Neil – associate professor of physics at Bridgewater College (in Virginia)

L. Fava and E. Santos – participated in the Insight Data Science Fellows Program; initially found employment in Silicon Valley.

E. Santos – presently works for Google (will give Physics Colloquium next month)



# Recent Ph.D. student (co-advised with Michael Dine) and her thesis project

Laurel Stephenson Haskins (2017): Supersymmetry , Inflation and Dark Matter

## Current position

Post Doctoral Research Associate at the Racah Institute of Physics at the Hebrew University of Jerusalem

We collaborated on two projects:

1. M. Dine, P. Draper, H.E. Haber and L. S. Haskins, *Perturbation Theory in Supersymmetric QED: Infrared Divergences and Gauge Invariance*, Phys. Rev. D **94**, 095003 (2016).
2. H.E. Haber and L. Stephenson Haskins, *Supersymmetric Theory and Models*, arXiv:1712.05926 [hep-ph], in Chapter 6 of *TASI 2016: Anticipating the Next Discoveries in Particle Physics*, edited by Rouven Essig and Ian Low (World Scientific, Singapore, 2018) pp. 355--499.

# Supersymmetric Theory and Models

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In these introductory lectures, we review the theoretical tools used in constructing supersymmetric field theories and their application to physical models. We first introduce the technology of two-component spinors, which is convenient for describing spin- $\frac{1}{2}$  fermions. After motivating why a theory of nature may be supersymmetric at the TeV energy scale, we show how supersymmetry (SUSY) arises as an extension of the Poincaré algebra of spacetime symmetries. We then obtain the representations of the SUSY algebra and discuss its simplest realization in the Wess-Zumino model. In order to have a systematic approach for obtaining supersymmetric Lagrangians, we introduce the formalism of superspace and superfields and recover the Wess-Zumino Lagrangian. These methods are then extended to encompass supersymmetric abelian and non-abelian gauge theories coupled to supermatter. Since supersymmetry is not an exact symmetry of nature, it must ultimately be broken. We discuss several mechanisms of SUSY-breaking (both spontaneous and explicit) and briefly survey various proposals for realizing SUSY-breaking in nature. Finally, we construct the Minimal Supersymmetric extension of the Standard Model (MSSM), and consider the implications for the future of SUSY in particle physics.

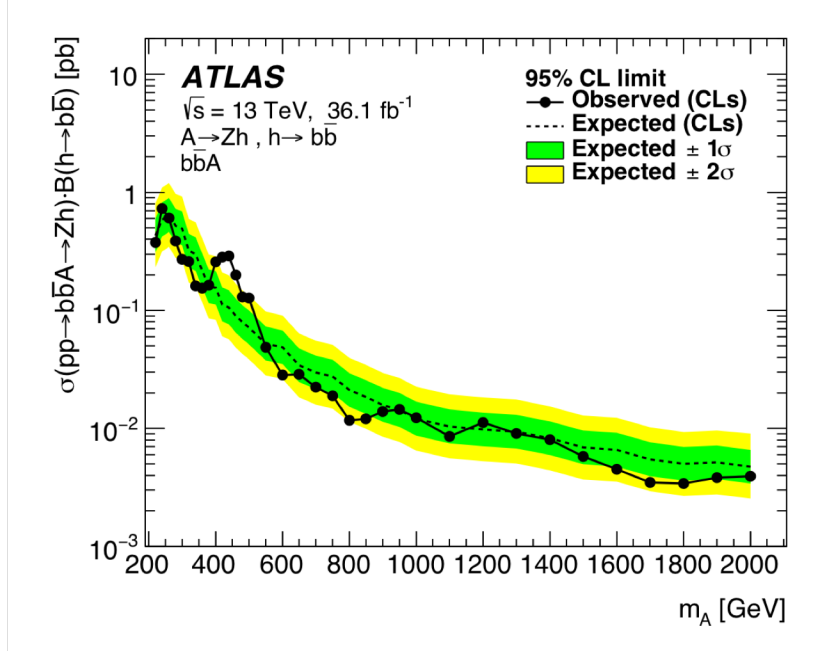
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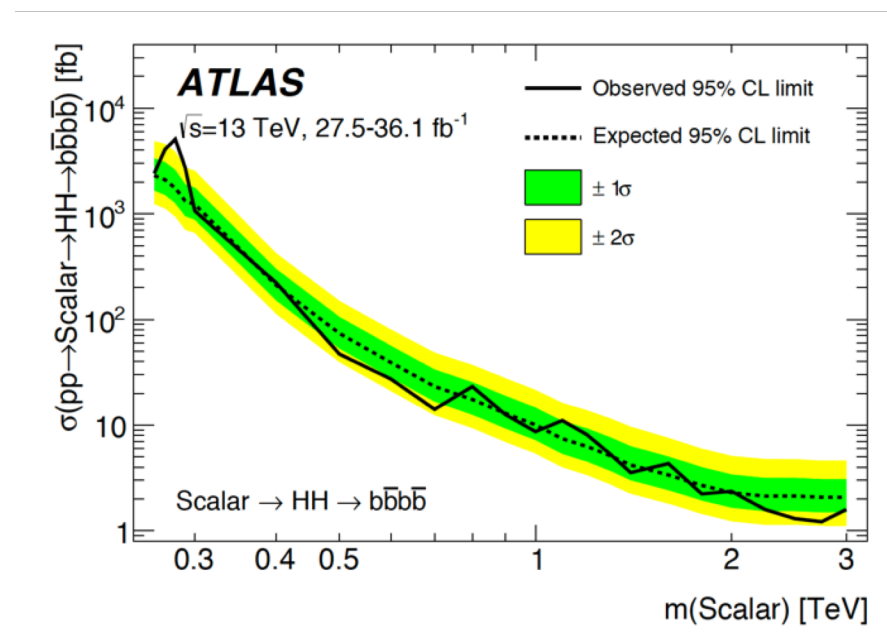
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# My current Ph.D. students and their projects

- 2HDM high energy flavor alignment (with S. Gori and E. Shahly)
  - Neutral Higgs-mediated flavor violation in the lepton sector.
- Phenomenological aspects of more general 2HDMs (with J. Connell and P. Ferreira)
  - Exploring some (local)  $3\sigma$  deviations in ATLAS searches for new Higgs bosons, with implications for the flavor-aligned 2HDM.



ATLAS Collaboration, JHEP **1803** (2018) 174



ATLAS Collaboration, arXiv:1804.06174

# Other Ongoing and Future Activities

- Natural alignment without decoupling (with P. Draper,...)
  - Achieving a SM-like Higgs boson without fine-tuning.
- Theoretical studies of the CP-violating 2HDM (with J.P. Silva,...)
- Basis-invariant treatment of the 3HDM (with V. Keus)
- P-even CP-violating signals in scalar-mediated processes (with V. Keus, T. Stefaniak and S. Thomas)
- Higgs alignment at one loop (with S.J.D. King and S. Moretti)
- Higgs alignment in 2HDM effective field theory (with A. Dedes and J. Rosiek,...)
- Higgs alignment in the Georgi-Machacek model (with P. Ferreira, H. Logan and Y. Wu)

Various other projects are waiting for the right Ph.D. student...