Note the Trojans and the Greeks, which cluster around the Sun/Jupiter L4 and L5 points.
There is one Trojan asteroid that appears to move in such a pattern with Jupiter and the Sun.
Michael Nauenberg (UCSC) has found that in some cases these orbits are quasi-stable (don’t evolve into chaos).