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An Introduction to Particle Dark Matter Lecture 3

3rd José Plínio Baptista School on Cosmology

25-30 September 2016

Pedra Azul, ES, Brazil

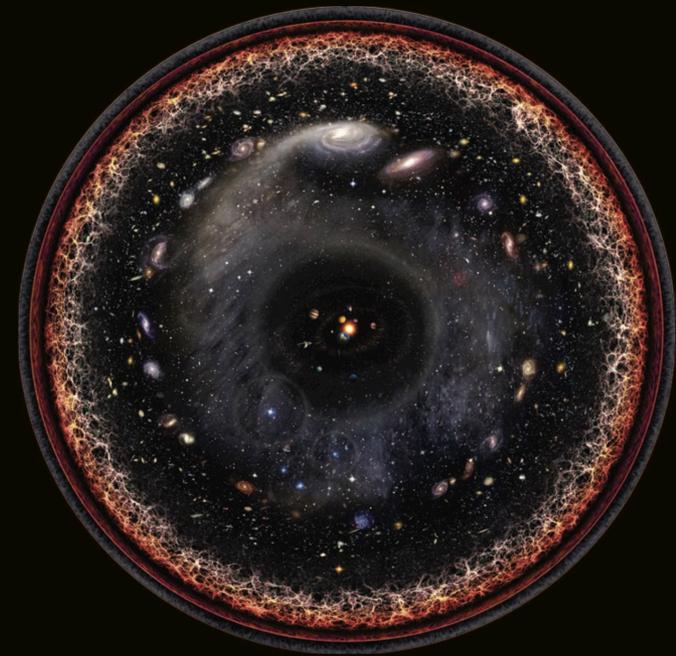


Key ideas from last lecture

- ✓ Cold relic density: **Boltzmann** equation, still $\Omega \sim 1/\sigma$, but potentially with **caveats** (resonances, coannihilation, thresholds)
- ✓ Modified **expansion rate** at DM freeze-out = big deal!
- ✓ Following chemical decoupling, **kinetic decoupling** sets the **cutoff** to the matter power spectrum
- ✓ Cut off **tiny** for cold relics, **too big** for hot relics, ~OK for warm
- ✓ DM doesn't need to be **coupled** to **ordinary matter** (other than gravitationally) but if thermal relic works, then it is
- ✓ **Direct detection** hard, but possible; keV-scale energy deposited, GeV-scale DM masses

AN INTRODUCTION TO PARTICLE DARK MATTER

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AN INTRODUCTION TO PARTICLE DARK MATTER

The paradigm of dark matter has been one of the key developments at the interface between cosmology and elementary particle physics in the past century, and one of the foundational blocks of the Standard Cosmological Model. This book offers a brand new perspective within this complex field: building and testing particle physics models for cosmological dark matter.

Chapters are organized to give a clear understanding of key research directions and methods within the field. The discussion is interspersed with several suggested problems, which question understanding and provide first-hand experience in transferring knowledge into practice. Appendices are also provided to summarize physical principles, in order to enable the building of a quantitative and well-founded understanding of particle models for dark matter. Rather than a review, key facts and findings are presented from the bottom up, separated and broken down into approachable sections and classroom-based discussions.

This is essential reading for anyone interested in the quest for understanding the microscopic nature of dark matter as it manifests itself in particle physics experiments, cosmological observations, and high-energy astrophysical phenomena. This highly interdisciplinary book is a primer for cosmologists and astrophysicists interested in building an understanding of particle models for dark matter, as well as for particle physicists interested in early-universe cosmology and high-energy astrophysics.

Front cover photo credit:
Observable universe logarithmic
Pablo Carlos Budassi

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 **World Scientific**

* to appear end of 2016/beginning 2017

Direct detection **event rates**

$$\frac{dR}{dE_R} = N_T n_\chi \left\langle v_\chi \frac{d\sigma}{dE_R} \right\rangle$$

$$E_R = \frac{q^2}{2m_T} = \frac{\mu_T^2}{m_T} v_\chi^2 (1 - \cos \theta)$$

$$dE_R = (d \cos \theta) (\mu_T^2 / m_T) v^2$$

$$\frac{dR}{dE_R} = N_T \frac{\rho_{DM} m_T}{m_\chi \mu_T^2} \int_{v_{\min}}^{v_{\text{esc}}} d^3 v \frac{f(v)}{v} \frac{d\sigma}{d \cos \theta}$$

How do we calculate the scattering **cross section**?

Non-relativistic limit, the scattering **matrix element** is the Fourier transform of WIMP-nucleus potential

$$\mathcal{M}(q^2) \sim \int \langle f | V(\vec{r}) | i \rangle e^{i\vec{q} \cdot \vec{r}} d\vec{r},$$

to the lowest order in velocity, the potential is just a **contact interaction** of spin-independent and axial terms

$$V(\vec{r}) = \sum_{\text{nucleons } n} (G_s^n + G_a^n \vec{\sigma}_\chi \cdot \vec{\sigma}_n) \delta(\vec{r} - \vec{r}_n).$$

where the **G**'s are the effective DM-nucleon couplings for **scalar** and **axial** interactions

Coherence requires the nucleus size to be much smaller than the momentum transfer wavelength ($1/q$)

$$qR_{\text{nucleus}} \ll 1$$

Loss of coherence is phenomenologically accounted for by introducing **form factors** describing the nucleus response

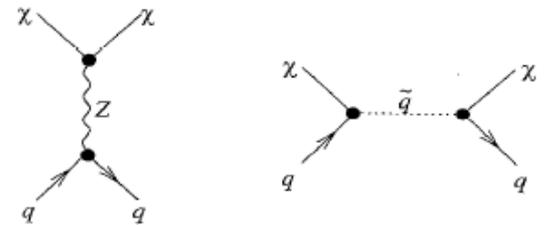
$$\mathcal{M}(q^2) = T(0)F(q^2)$$

Given a **microscopic** theory of dark matter,
how does one get to the **DM-nucleus cross section**?

An interesting **multi-layered** problem in **effective field theory**!

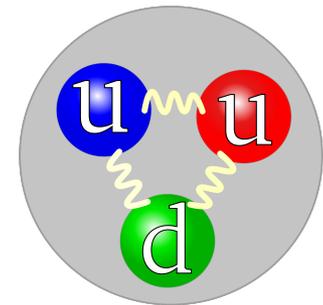
Low-energy EFT

Dark Matter-quark



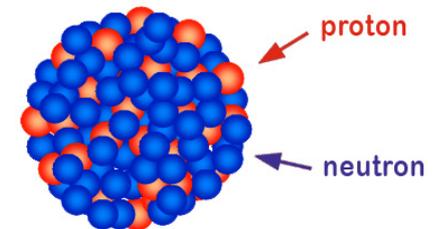
Nucleon matrix elements

Dark Matter-nucleon



Form factors

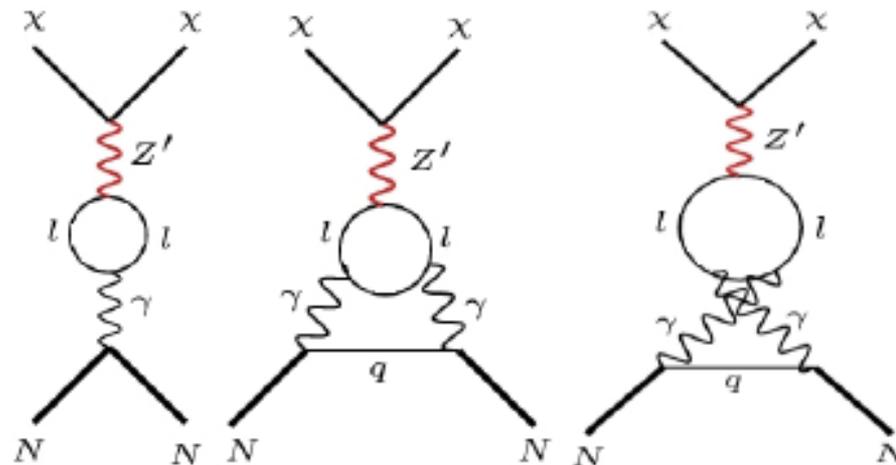
Dark Matter-nucleus

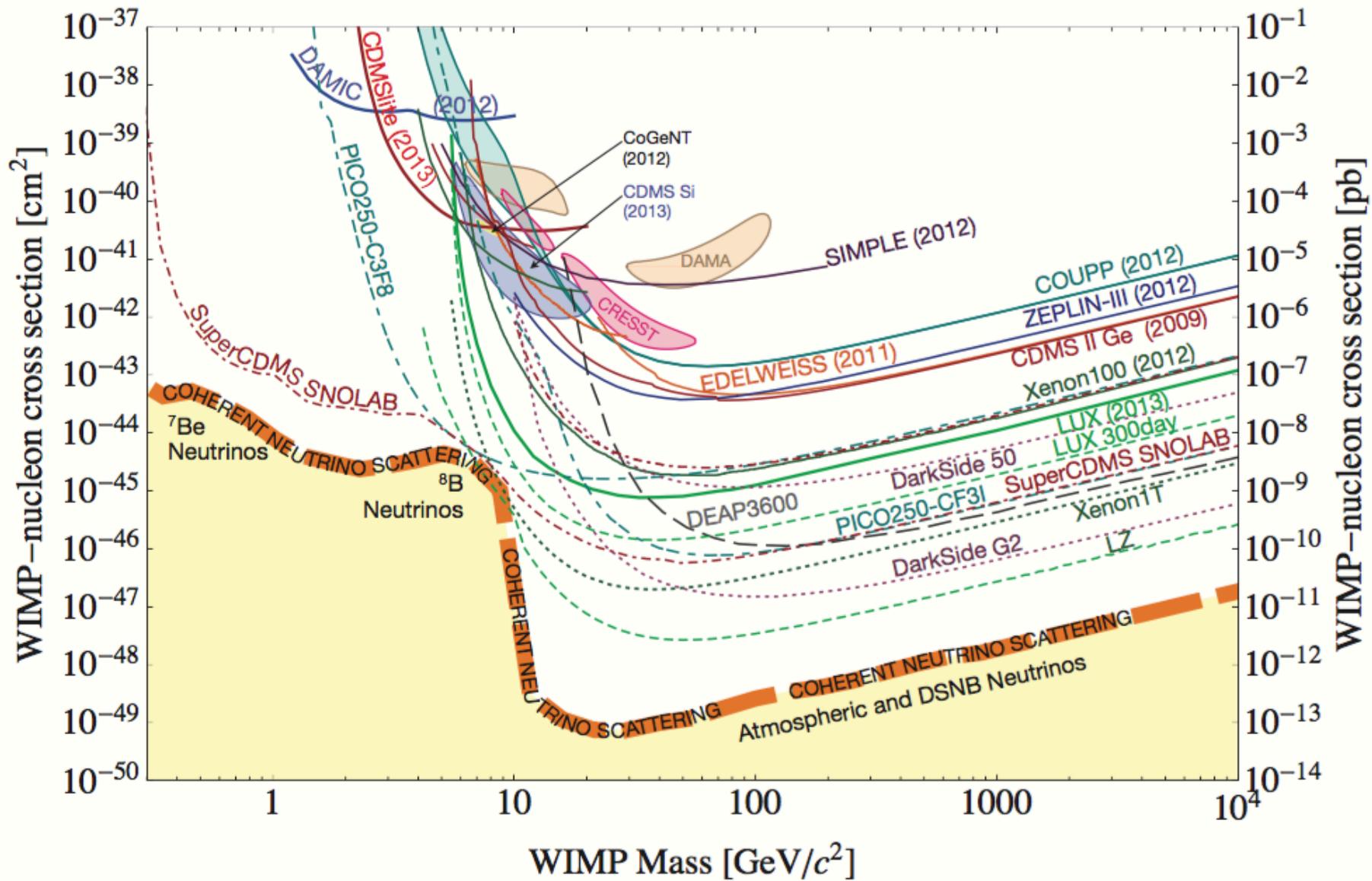


Sometimes life is simpler, e.g. if DM is (**milli-electric-**)**charged**

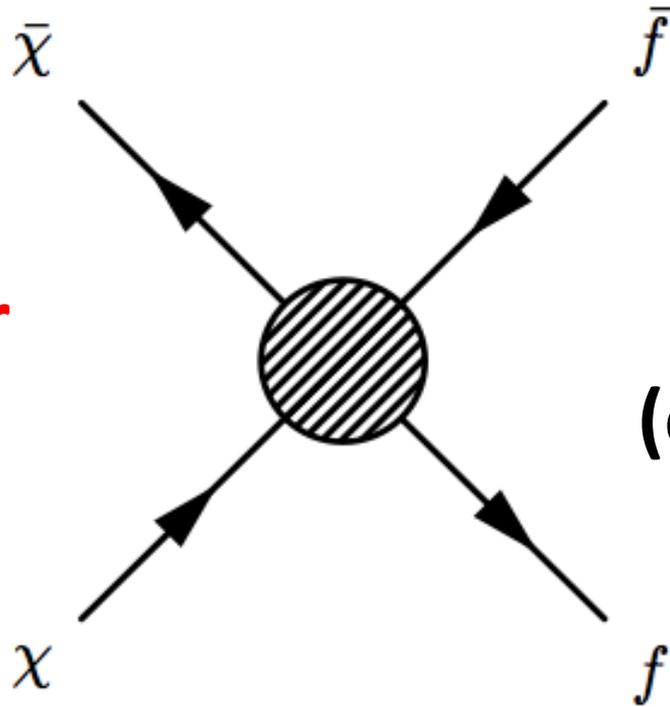
$$\sigma_N = \frac{16\pi\alpha^2\epsilon^2 Z^2 \mu_N^2}{q^4}$$

Sometimes life is nastier, e.g. if DM is **lepto-philic**

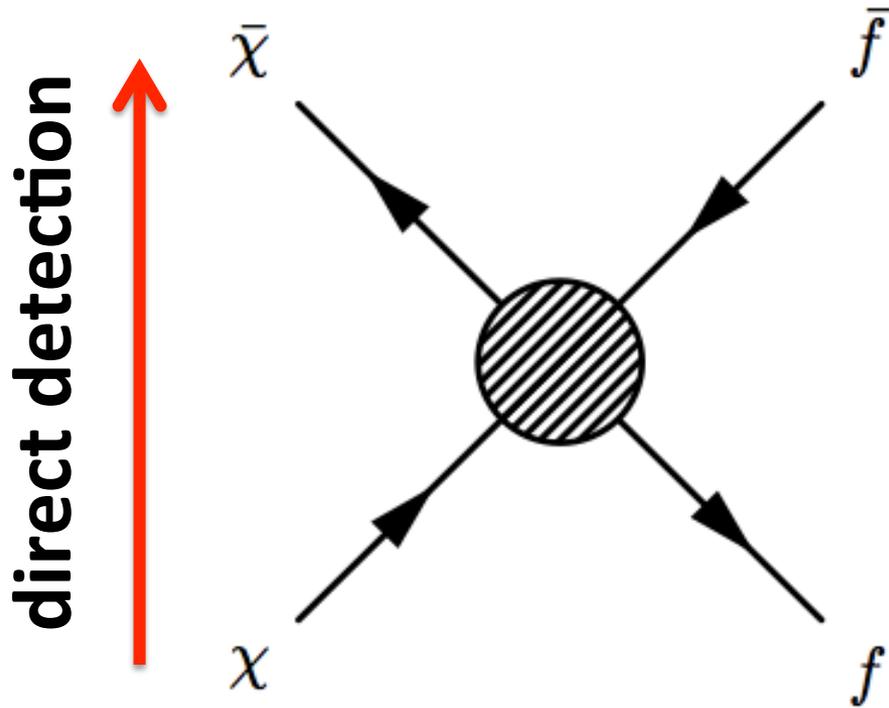




**Dark Matter
Particles**



**Standard Model
(ordinary) Particles**



direct detection

thermal equilibrium

[pair annihilation, “indirect” detection]

Idea: use the **debris** of DM **pair-annihilation**
(likely large if thermal relic) or **decay**

$$\Gamma_{\text{SM, ann}} \sim \left(\int_V \frac{\rho_{\text{DM}}^2}{m_\chi^2} dV \right) \times (\sigma v) \times (N_{\text{SM, ann}}),$$
$$\Gamma_{\text{SM, dec}} \sim \left(\int_V \frac{\rho_{\text{DM}}}{m_\chi} dV \right) \times \left(\frac{1}{\tau_{\text{dec}}} \right) \times (N_{\text{SM, dec}})$$

What do we know about these **rates**?
 σv from **thermal production** (with caveats!)

How about **decay rate**?

Suppose DM decay mediated by **high-scale** physics at scale **M**

$$\Gamma_5 \sim \frac{1}{M^2} m_\chi^3$$

$$\tau_5 \sim 1 \text{ s} \left(\frac{1 \text{ TeV}}{m_\chi} \right)^3 \left(\frac{M}{10^{16} \text{ GeV}} \right)^2$$

Dimension-5 operator doesn't work – would be too **short lived!**

$$\Gamma_6 \sim \frac{1}{M^4} m_\chi^5,$$

Interesting, well motivated!

$$\tau_6 \sim 10^{27} \text{ s} \left(\frac{1 \text{ TeV}}{m_\chi} \right)^5 \left(\frac{M}{10^{16} \text{ GeV}} \right)^4$$

What about annihilation **final state**?

Very **model-dependent**

1. if DM belongs to an SU(2) **multiplet**, then well-defined combination of ZZ, WW final states...

2. In UED, DM is KK-1 mode of **hypercharge gauge boson**, thus

$$|M|^2 \propto |Y_f|^4 \quad [Y_{u_L} = 4/3, \quad Y_{e_R} = 2]$$

3. Special "**selection rule**", e.g. helicity suppression for Majorana fermion (analogous to charged pion decay)

$$|M|^2 \propto m_f^2$$

Annihilation (or decay) of DM can be **detected**
or **constrained** in a variety of ways

Here's one possible **classification**:

1. **Very Indirect**: effects induced by dark matter on **astrophysical objects** or on **cosmological observations**
2. **Pretty Indirect**: probes that don't "trace back" to the annihilation event, as their trajectories are bent as the particles propagate: **charged cosmic rays**
3. **Not-so-indirect**: **neutrinos** and **gamma rays**, with the great added advantage of traveling in straight lines

Very indirect probes include e.g.

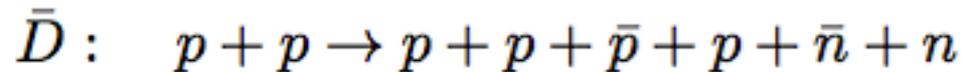
- **Solar Physics** (dark matter can affect the Sun's core temperature, the sound speed inside the Sun,...)
- **Neutron Star Capture**, possibly leading to the formation of black holes (notably e.g. in the context of asymmetric dark matter)
- **Supernova** and **Star** cooling
- **Protostars** (e.g. WIMP-fueled population-III stars)
- **Planets warming**
- **Big Bang Nucleosynthesis**, on the **cosmic microwave background**, on **reionization**, on **structure formation**...

Pretty Indirect Probes: **charged cosmic rays**

Good idea is to use **rare** cosmic rays, such as **anti-matter**

antiprotons, positrons relatively abundant
(mostly from inelastic processes CR p on ISM p)

Interesting probe: **antideuterons** (or even **anti-³He** !!)



large energy **threshold** (~17 GeV), so typically large momentum, while from DM produced at very low momentum! Select **low-energy antideuterons**

positrons (and in part antiprotons) have attracted attention because of "**anomalies**" reported by PAMELA, AMS-02

general scheme for Galactic CR's: **diffusion** (leaky-box) models

$$\frac{dn}{dE} = \psi(\vec{x}, E, t)$$

$$\frac{\partial}{\partial t} \psi = D(E) \Delta \psi + \frac{\partial}{\partial E} (b(E) \psi) + Q(\vec{x}, E, t)$$

Things can be made arbitrarily more **complicated/sophisticated**:

- *Cosmic-ray convection*; recipe: add: $\frac{\partial}{\partial z} (v_c \cdot \psi)$;
- *Diffusive re-acceleration*; recipe: add: $\frac{\partial}{\partial p} p^2 D_{pp} \frac{\partial}{\partial p} \frac{1}{p^2} \psi$;
- *Fragmentation and decays*; recipe: add: $-\frac{1}{\tau_{f,d}} \psi$.

Boundary conditions:

$$R \sim \mathcal{O}(1) \times 10 \text{ kpc},$$

$$h \sim \mathcal{O}(1) \times 1 \text{ kpc}.$$

$$D(E) \sim D_0 \left(\frac{E}{E_0} \right)^\delta$$

Useful to **simplify** the diffusion equation assuming steady-state, using typical diffusion and energy loss **time-scales**, defined by

$$\tau_{\text{diff}} \sim \frac{R^2}{D_0} \cdot E^{-\delta}, \quad \tau_{\text{loss}} \sim \frac{E}{b(E)}$$

Diff. Eq. then looks like $0 = -\frac{\psi}{\tau_{\text{diff}}} - \frac{\psi}{\tau_{\text{loss}}} + Q$.

with **solution** $\psi \sim Q \cdot \min[\tau_{\text{diff}}, \tau_{\text{loss}}]$.

If the source is cosmic rays accelerated via a **Fermi mechanism**,

$$Q \sim E^{-2} \longrightarrow \psi \sim E^{-2} \cdot E^{-\delta} \sim E^{-2.7}$$

...in agreement with **CR protons** (where en. losses are irrelevant)

For CR **electrons**, energy losses are efficient above a certain **energy**,

$$b_e(E) \simeq b_{\text{IC}}^0 \left(\frac{u_{\text{ph}}}{1 \text{ eV/cm}^3} \right) \cdot E^2 + b_{\text{sync}}^0 \left(\frac{B}{1 \mu\text{G}} \right)^2 \cdot E^2$$

$$b_{\text{IC}}^0 \simeq 0.76, \quad b_{\text{sync}}^0 \simeq 0.025 \cdot 10^{-16} \text{ GeV/s}$$

Therefore (as observed) we expect a **broken power-law**

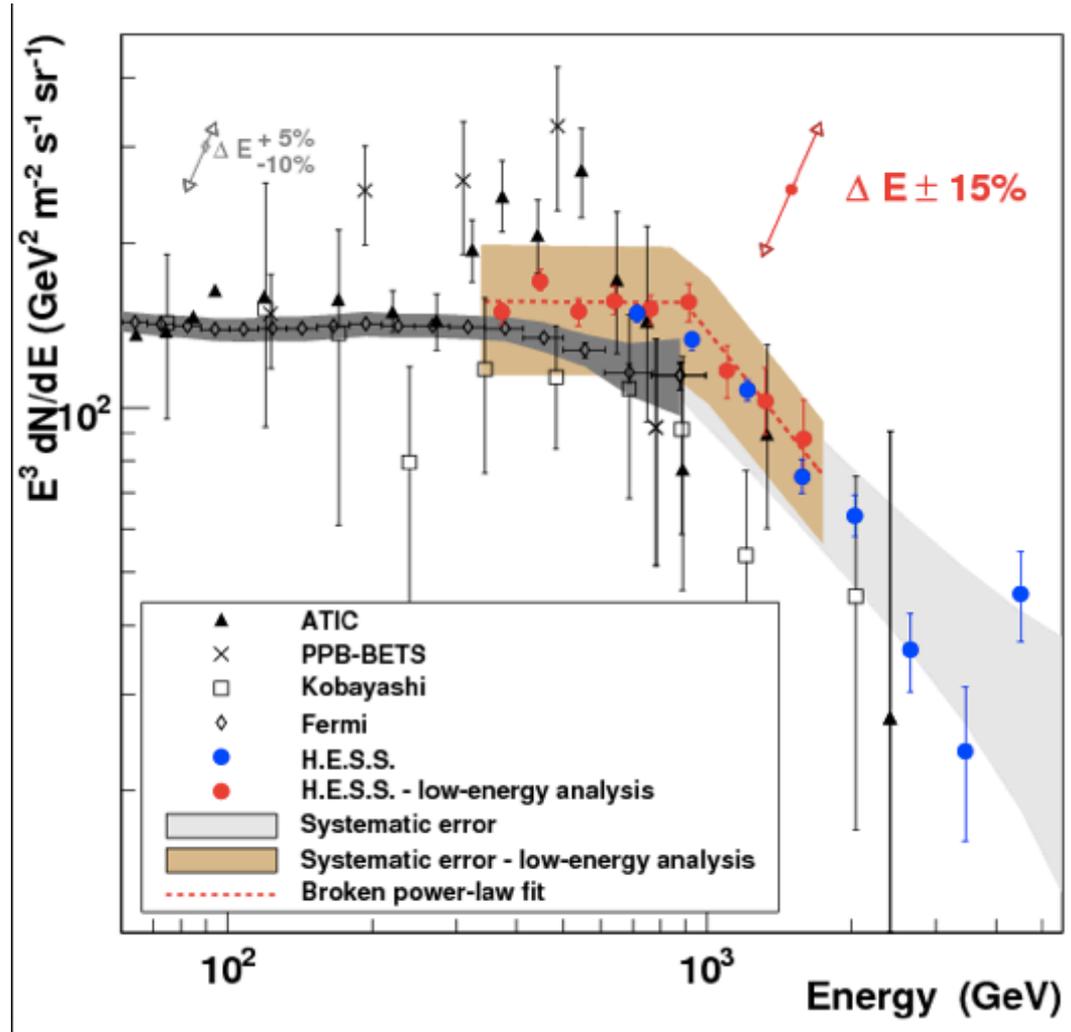
$$\psi_{\text{primary, low-energy}} \sim Q \cdot \tau_{\text{diff}} \sim E^{-2} \cdot E^{-\delta} \sim E^{-2.7}$$

$$\psi_{\text{primary, high-energy}} \sim Q \cdot \tau_{\text{loss}} \sim E^{-1} \cdot \frac{E}{E^2} \sim E^{-3}$$

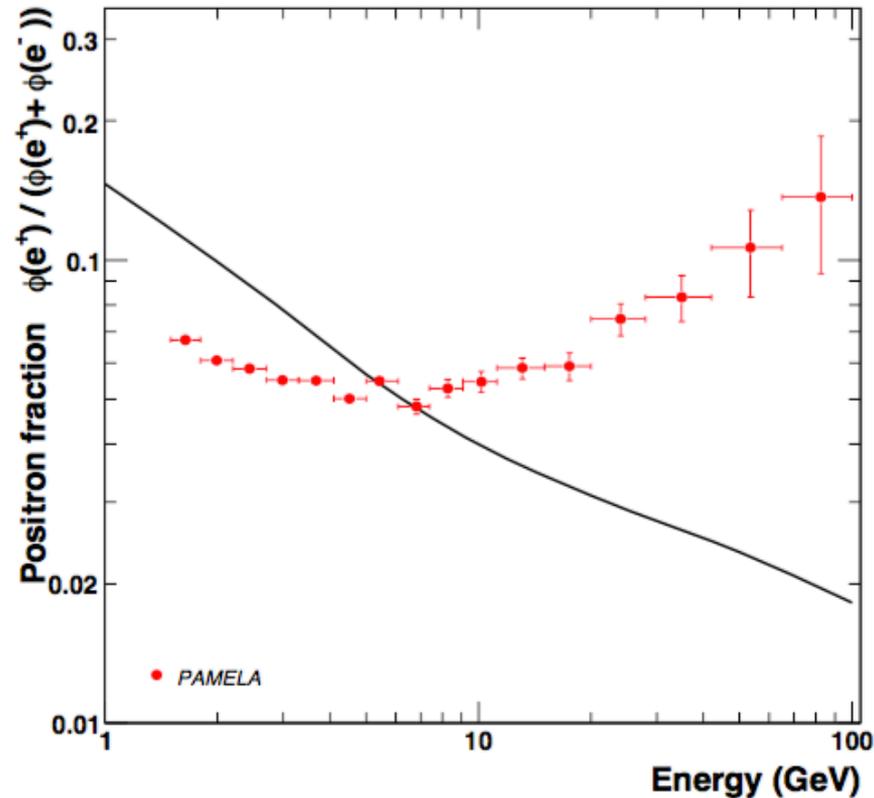
Also, **secondary-to-primary** ratios are generically

$$\frac{\psi_{e^+}}{\psi_{e^-}} \sim E^{-\delta}.$$

Electron spectrum looks pretty good



but the **secondary-to-primary ratio** prediction is at **odds** with observed rising positron fraction



Much **hype** about this possibly being from **DM** – but very **problematic**

- No excess **anitprotons** – must be "leptophilic" (possible but not generic)
- No observed **secondary radiation** from brems or IC
- Needed **pair-annihilation rate** very large for thermal production, leads to unseen gamma-ray or radio emission

$$\langle\sigma v\rangle \sim 10^{-24} \frac{\text{cm}^3}{\text{s}} \cdot \left(\frac{m_\chi}{100 \text{ GeV}}\right)^{1.5}$$

Alternate explanation: nearby **point source**
 injecting a burst of **positrons** (a.k.a. Green's function, a.k.a. **PSR**)

$$\psi \propto Q \cdot \exp \left(- \left(\frac{r}{r_{\text{diff}}} \right)^2 \right)$$

Estimate **Age** and **Distance** of putative source

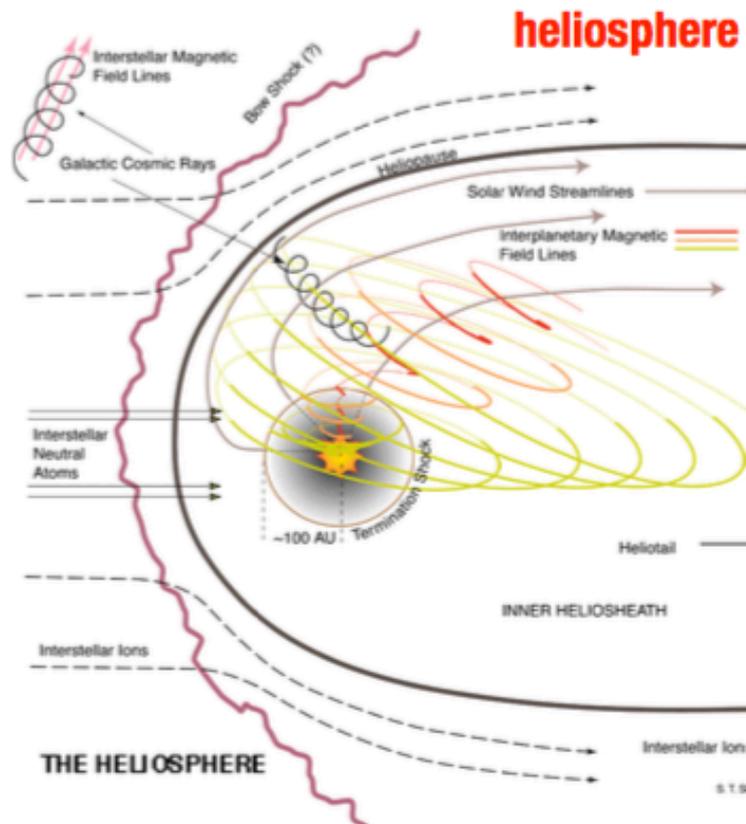
$$t_{\text{psr}} \ll \tau_{\text{loss}} = \frac{E}{b(E)}; \text{ for } E = 100 \text{ GeV}, \tau_{\text{loss}} \sim \frac{100}{10^{-16} \cdot 100^2} \text{ s} \sim 10^{14} \text{ s} \sim 3 \text{ Myr.}$$

$$r_{\text{diff}} \simeq \sqrt{D(E) \cdot t.}$$

$$\sqrt{D(E) \cdot t_{\text{psr}}} \gg \text{distance} \rightarrow \text{distance} \ll (3 \times 10^{28} \cdot 100^{0.7} \cdot 10^{14})^{1/2} \text{ cm} \sim 10^{22} \text{ cm} \sim 3 \text{ kpc.}$$

One possible way to **disentangle** PSR from DM: **anisotropy**

Complication: Larmor radius for **heliospheric** magnetic fields $B \sim nT$, is of the order of the **solar system size** (exercise)



Not-so-indirect DM detection: **neutrinos!**

Only **two** observed astrophysical sources of neutrinos!

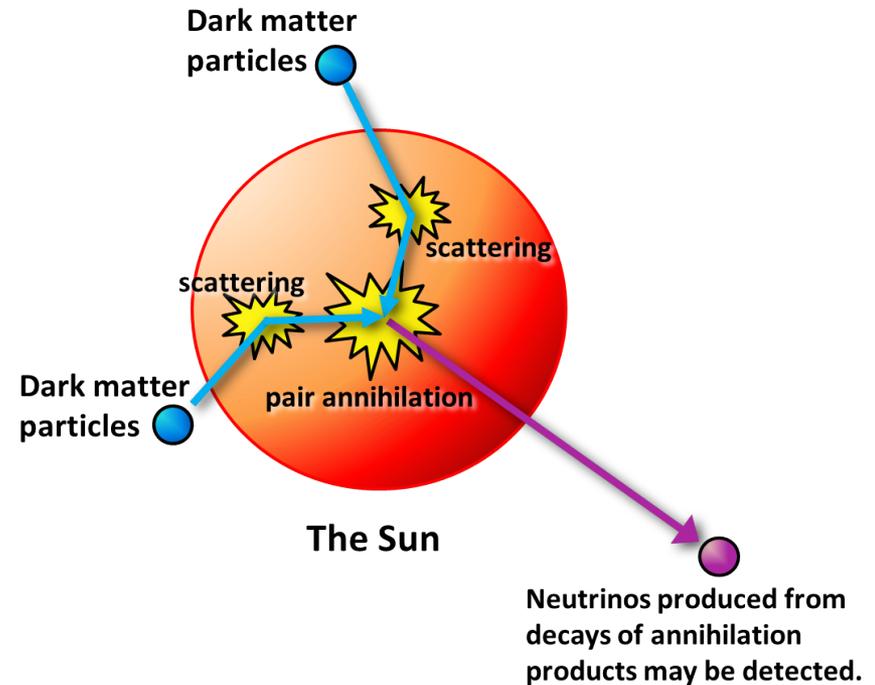
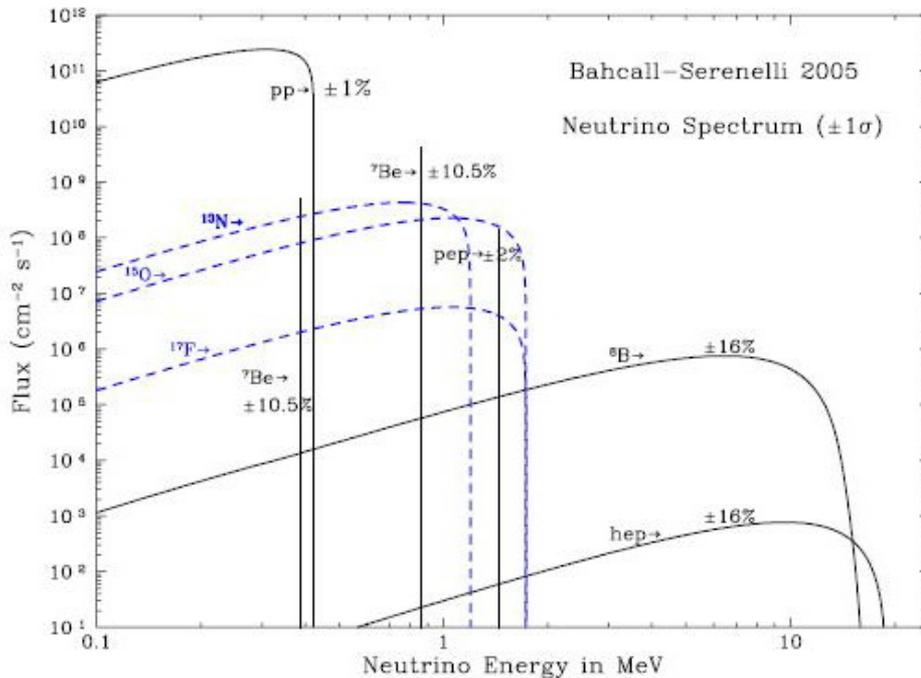
Hard (but not impossible) to detect particles

flip side: neutrinos have very **long mean free paths** in matter!

idea: DM can be **captured** in celestial bodies, **accrete** in sizable densities, start pair-annihilating

if the process of capture and annihilation is in **equilibrium**, large **fluxes** of neutrino can escape

best target: **Sun!** Large, **nearby**, **low-E** neutrino emission



Estimate the process **quantitatively!**

First: **capture rate**

$$C_{\odot} \sim \phi_{\chi} \cdot \left(\frac{M_{\odot}}{m_p} \right) \cdot \sigma_{\chi-p}, \quad \phi_{\chi} \sim n_{\chi} \cdot v_{\text{DM}} = \frac{\rho_{\text{DM}}}{m_{\chi}} \cdot v_{\text{DM}}$$

$$\begin{aligned} \sigma_{\chi-p}^{\text{spin dependent}} &\lesssim 10^{-39} \text{ cm}^2, \\ \sigma_{\chi-p}^{\text{spin independent}} &\lesssim 10^{-44} \text{ cm}^2. \end{aligned}$$

$$C_{\odot} \sim \frac{10^{23}}{\text{s}} \left(\frac{\rho_{\text{DM}}}{0.3 \text{ GeV/cm}^3} \right) \cdot \left(\frac{v_{\text{DM}}}{300 \text{ km/s}} \right) \cdot \left(\frac{100 \text{ GeV}}{m_{\chi}} \right) \cdot \left(\frac{\sigma_{\chi-p}}{10^{-39} \text{ cm}^2} \right)$$

Number of **accreted DM particles** N

$$\frac{dN}{dt} = C^\odot - A^\odot [N(t)]^2 - E^\odot N(t).$$

$$A^\odot \simeq \frac{\langle \sigma v \rangle}{V_{\text{eff}}} \quad \frac{m_\chi \phi_{\text{grav}}(R_{\text{eff}})}{T^\odot} \simeq 1$$

$$V_{\text{eff}} \sim 10^{28} \text{ cm}^3 \left(\frac{m_\chi}{100 \text{ GeV}} \right)^{3/2}$$

$$\Gamma_A = \frac{1}{2} A^\odot [N(t^\odot)]^2 = \frac{C^\odot}{2} \left[\tanh(\sqrt{C^\odot A^\odot} t^\odot) \right]^2.$$

$$t^\odot \sim 4.5 \text{ Byr} \sim 10^{17} \text{ s}$$

$$t^{\text{eq}} \equiv \frac{1}{\sqrt{C^\odot A^\odot}} \ll t^\odot \qquad C^\odot \sim 10^{23} \text{ s}^{-1} \left(\frac{\sigma_{\chi-p}}{10^{-39} \text{ cm}^2} \right)$$

$$A_{\text{eq}}^\odot \gg \frac{1}{(t^\odot)^2 C^\odot} = \frac{1}{10^{34} \cdot 10^{23} \text{ s}} \sim 10^{-57} \text{ s}^{-1}$$

$$A^\odot = 3 \times 10^{-54} \text{ s}^{-1} \left(\frac{\langle \sigma v \rangle}{3 \times 10^{-26} \text{ cm}^3/\text{s}} \right)$$

So yes thermal DM is in **equilibration** as long as
WIMP-nucleon cross section is **larger** than 10^{-41} cm^2

With **equilibration**, flux of neutrinos only depends on **capture rate**!

$$\Gamma_A = \frac{1}{2} A^\odot [N(t^\odot)]^2 = \frac{C^\odot}{2} \left[\tanh(\sqrt{C^\odot A^\odot} t^\odot) \right]^2 \quad \Gamma_A \simeq \frac{C^\odot}{2}$$

flux of **neutrinos** is then
$$\frac{dN_{\nu_f}}{dE_{\nu_f}} = \frac{C^\odot}{8\pi(D^\odot)^2} \left(\frac{dN_{\nu_f}}{dE_{\nu_f}} \right)_{\text{inj}}$$

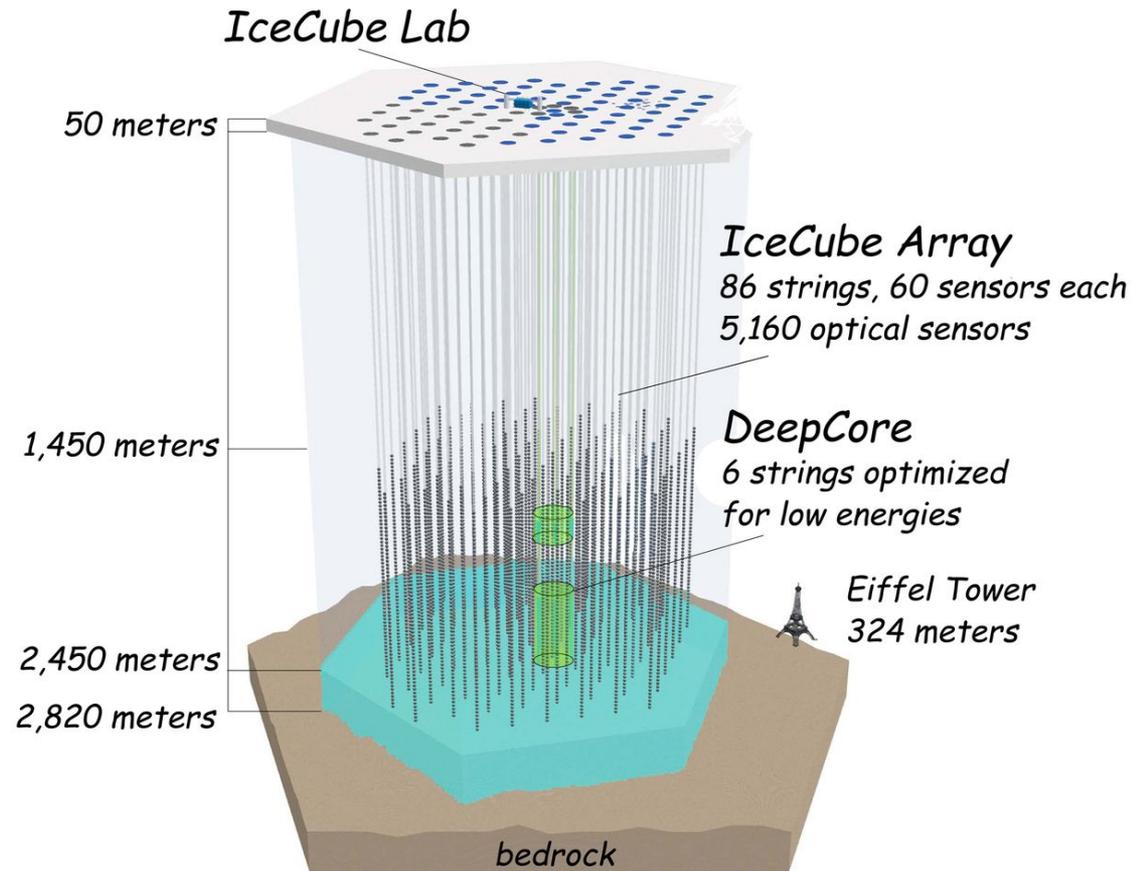
...and the number of **events** at **IceCube**

$$N_{\text{events}} = \int dE_{\nu_\mu} \int dy \left(A_{\text{eff}} \cdot \frac{dN_{\nu_\mu}}{dE_{\nu_\mu}} \cdot \frac{d\sigma}{dy}(E_{\nu_\mu}, y) \cdot (R_\mu(E_{\nu_\mu})) \right)$$

Best **final states**: WW, ZZ, or leptophilic

So far **no anomalous events** from Sun observed; **Earth** less promising

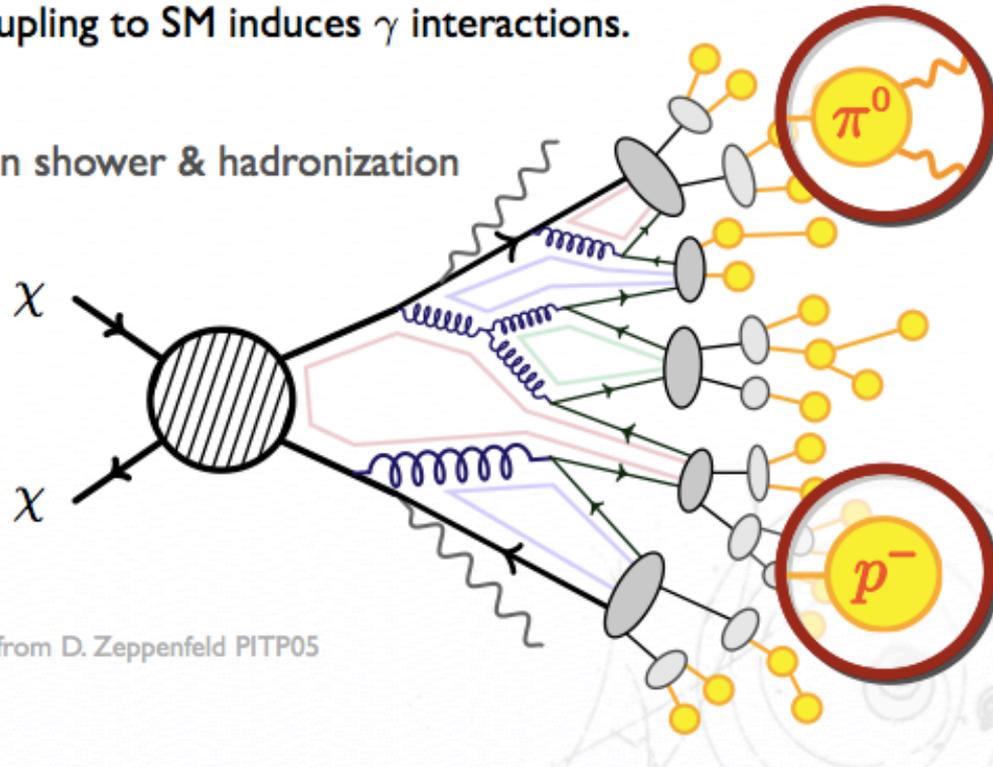
Opportunities with
lower-energy
threshold sub-detectors
DeepCore, PINGU



Light from dark matter!

DM coupling to SM induces γ interactions.

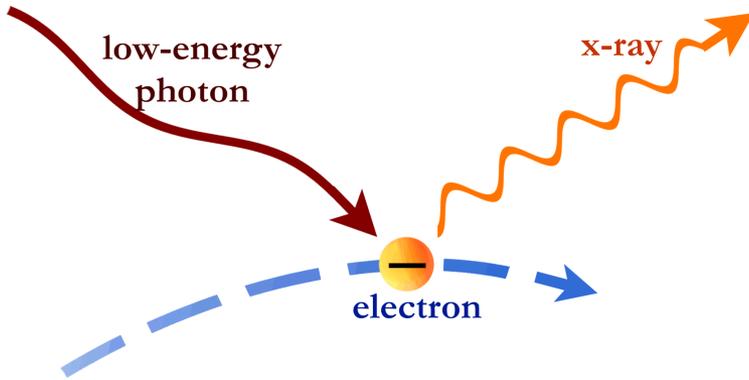
Parton shower & hadronization



Adapted from D. Zeppenfeld PITP05

Primary photons: prompt, or internal brems; just run Pythia (if you can!)

Secondary photons: IC, synchrotron



$$\langle E'_0 \rangle \sim \frac{4}{3} \gamma_e^2 E_0.$$

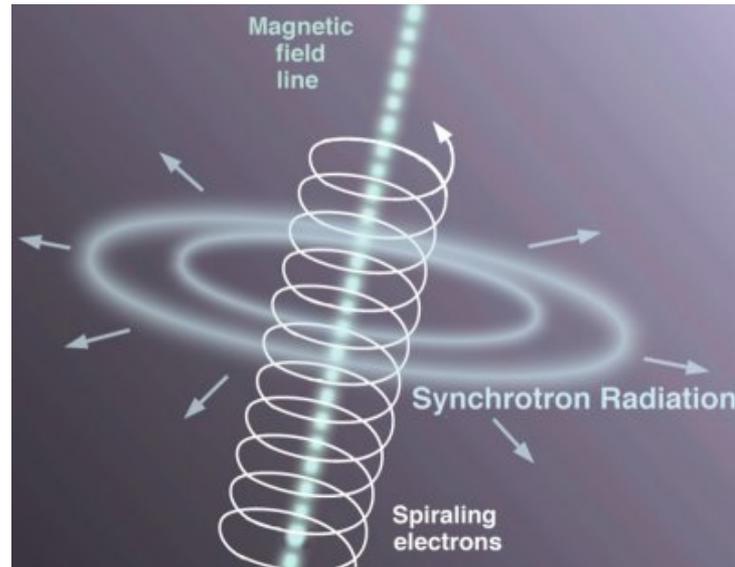
CMB : $E_0 \sim 2 \times 10^{-4}$ eV

starlight : $E_0 \sim 1$ eV

dust : $E_0 \sim 0.01$ eV

$$E_e \sim \frac{m_\chi}{10} \rightarrow \gamma_e \sim 2 \times 10^4 \left(\frac{m_\chi}{100 \text{ GeV}} \right)$$

$$E'_{\text{CMB}} \sim 10^5 \text{ eV} \left(\frac{m_\chi}{100 \text{ GeV}} \right)^2$$



$$\frac{\nu_{\text{sync}}}{\text{MHz}} \simeq 10 \cdot \left(\frac{E_e}{\text{GeV}} \right)^2 \left(\frac{B}{\mu\text{G}} \right) \simeq 2.8 \cdot \left(\frac{\gamma_e}{1000} \right)^2 \left(\frac{B}{\mu\text{G}} \right)$$

Prompt emission simply depends on **annihilation** final state, and **target** of choice

$$\phi_\gamma = \frac{\Delta\Omega}{4\pi} \left\{ \frac{1}{\Delta\Omega} \int d\Omega \int dl(\psi) (\rho_{\text{DM}})^2 \right\} \frac{\langle\sigma v\rangle}{2m_\chi^2} \frac{dN_\gamma}{dE_\gamma}$$

$$\frac{dN_\gamma}{dE_\gamma} = \sum_f \frac{dN_\gamma^f}{dE_\gamma}$$

Angular region varies from 1 degree, to 0.1 degrees (10^{-3} , 10^{-5} sr, resp)

1. Dwarf Spheroidal Galaxies

- Draco, $J \sim 10^{19} \text{ GeV}^2/\text{cm}^5$, \pm a factor 1.5;
- Ursa Minor, $J \sim 10^{19} \text{ GeV}^2/\text{cm}^5$, \pm a factor 1.5;
- Segue, $J \sim 10^{20} \text{ GeV}^2/\text{cm}^5$, \pm a factor 3

2. Local Milky-Way-like galaxies

- M31, $J \sim 10^{20} \text{ GeV}^2/\text{cm}^5$

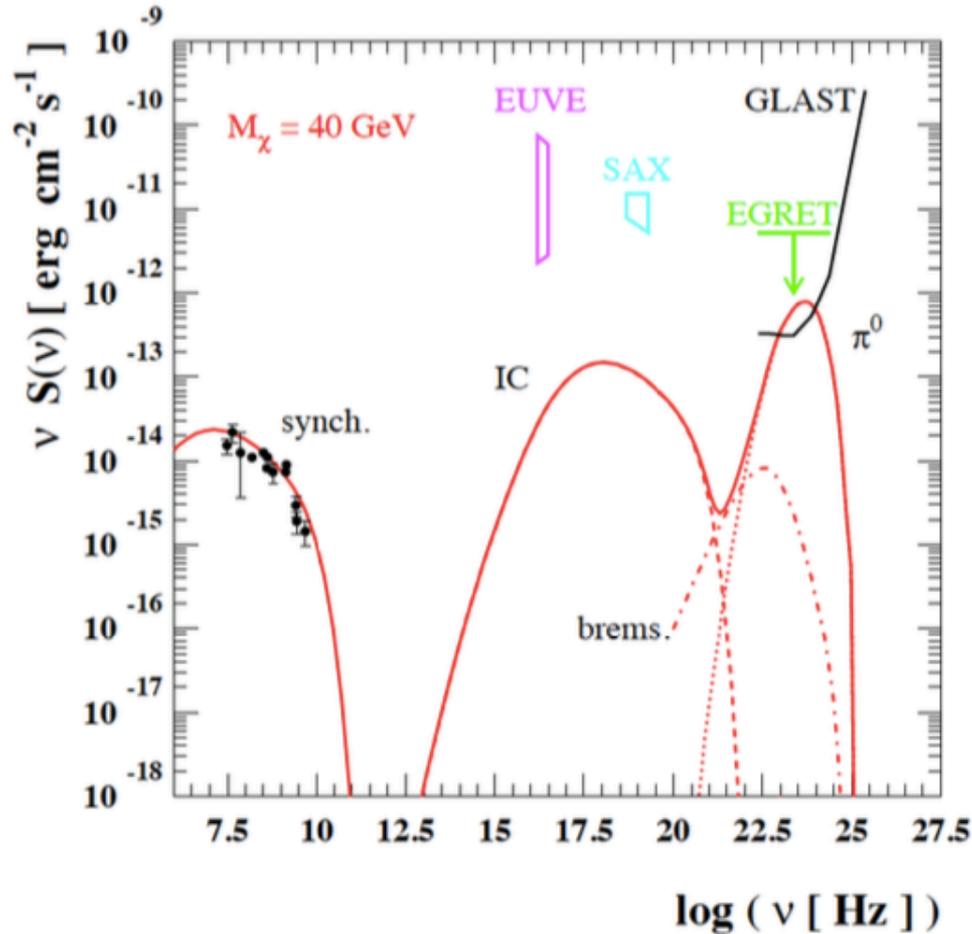
3. Local clusters of galaxies

- Fornax, $J \sim 10^{18} \text{ GeV}^2/\text{cm}^5$
- Coma, $J \sim 10^{17} \text{ GeV}^2/\text{cm}^5$
- Bullet, $J \sim 10^{14} \text{ GeV}^2/\text{cm}^5$

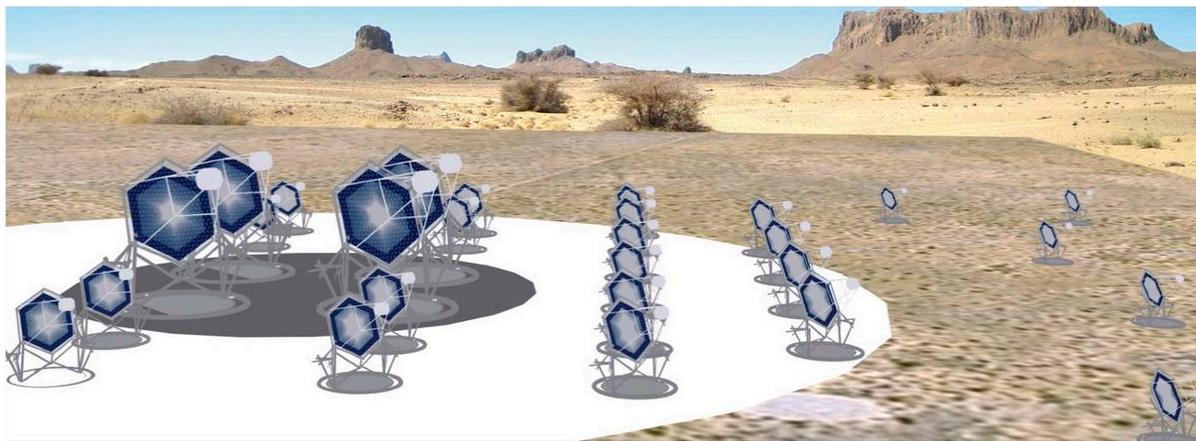
4. Galactic center

- 0.1° : $J \sim 10^{22} \dots 10^{25} \text{ GeV}^2/\text{cm}^5$
- 1° : $J \sim 10^{22} \dots 10^{24} \text{ GeV}^2/\text{cm}^5$

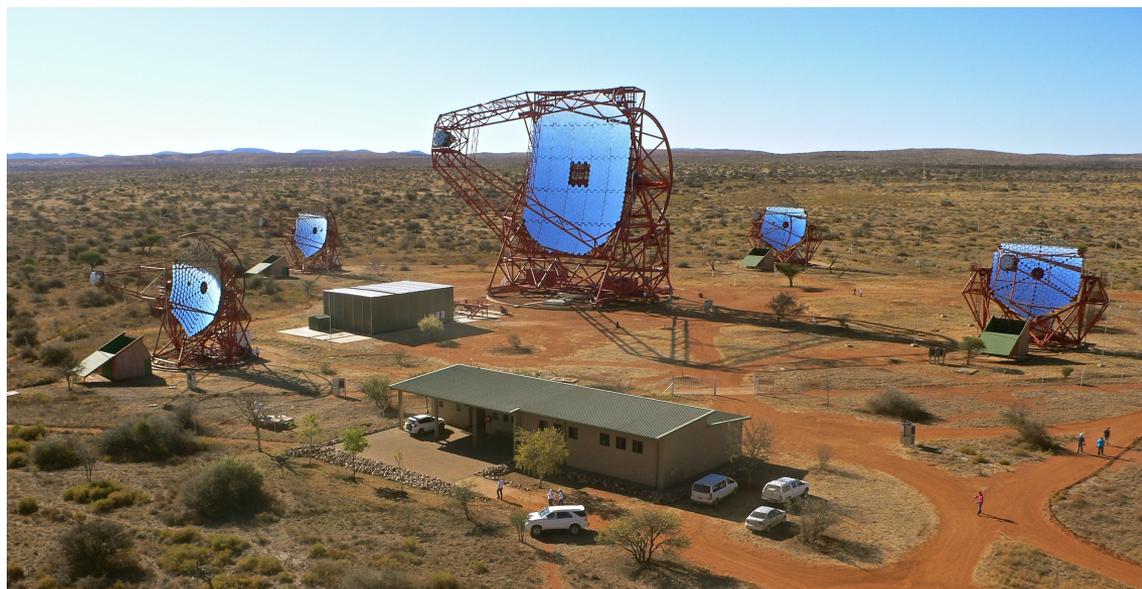
Overall **emission** looks like this, e.g. in a **cluster** of galaxies



here, **normalization** chosen to fit radio emission



	Fermi-LAT	H.E.S.S.	CTA
E_γ range	0.1 to 300 GeV	0.1 to 10 TeV	10 GeV to 10 TeV
A_{eff}	$\sim 1 \text{ m}^2$	$\sim 10^5 \text{ m}^2$	$\sim 10^6 \text{ m}^2$
T_{obs}	$\sim 10^8 \text{ s}$	$\sim 10^6 \text{ s}$	$\sim 10^6 \text{ s}$



to have a **detection**: collect **some photons**, beat **background** (S/N>>1)

$$\int dE_\gamma \frac{dN_\gamma}{dE_\gamma} \sim \frac{m_\chi}{\text{GeV}}$$

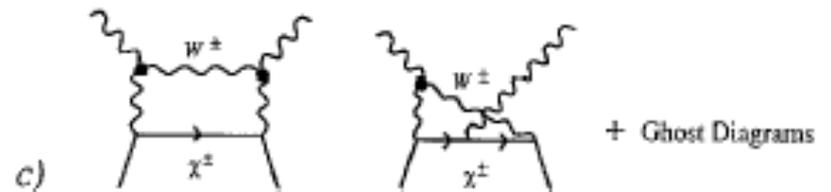
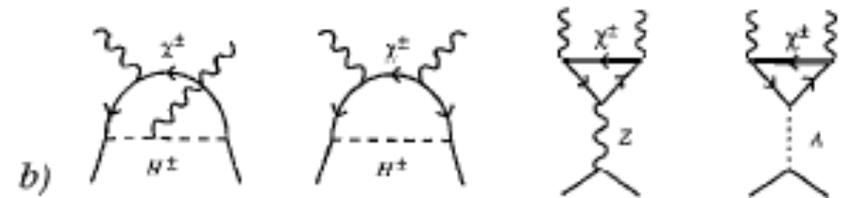
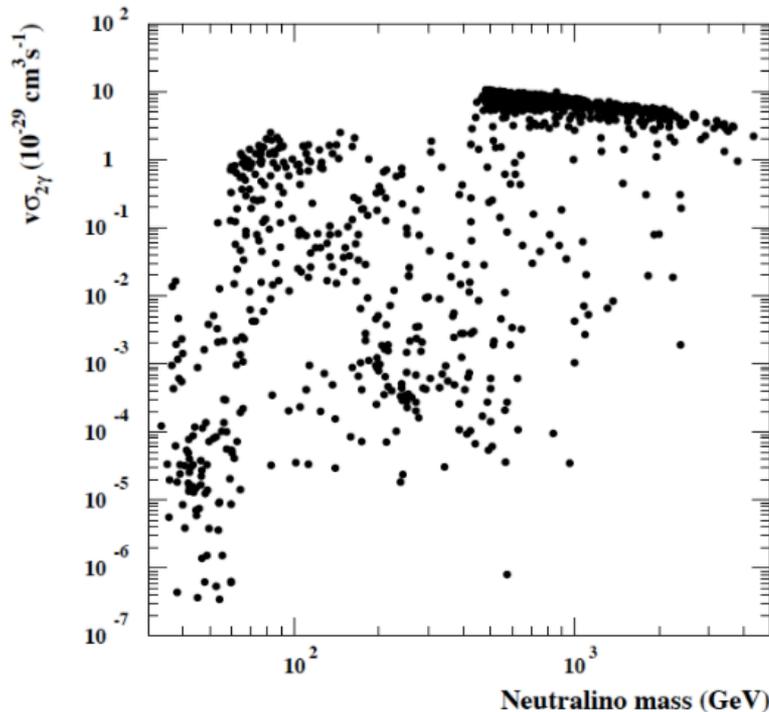
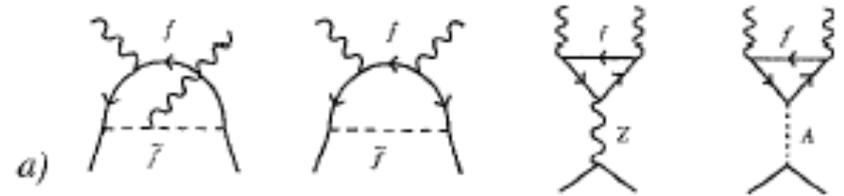
$$\phi_\gamma = (\Delta\Omega \cdot J) \frac{1}{8\pi} \frac{\langle\sigma v\rangle}{m_\chi^2} \cdot m_\chi \sim 10^{-32} \frac{1}{\text{cm}^2 \text{ s}} \left(\frac{J}{\text{GeV}^2/\text{cm}^5} \right)$$

$$N_\gamma \sim A_{\text{eff}} \cdot T_{\text{obs}} \cdot \phi_\gamma \sim 10^{-20} \frac{J}{\text{GeV}^2/\text{cm}^5}$$

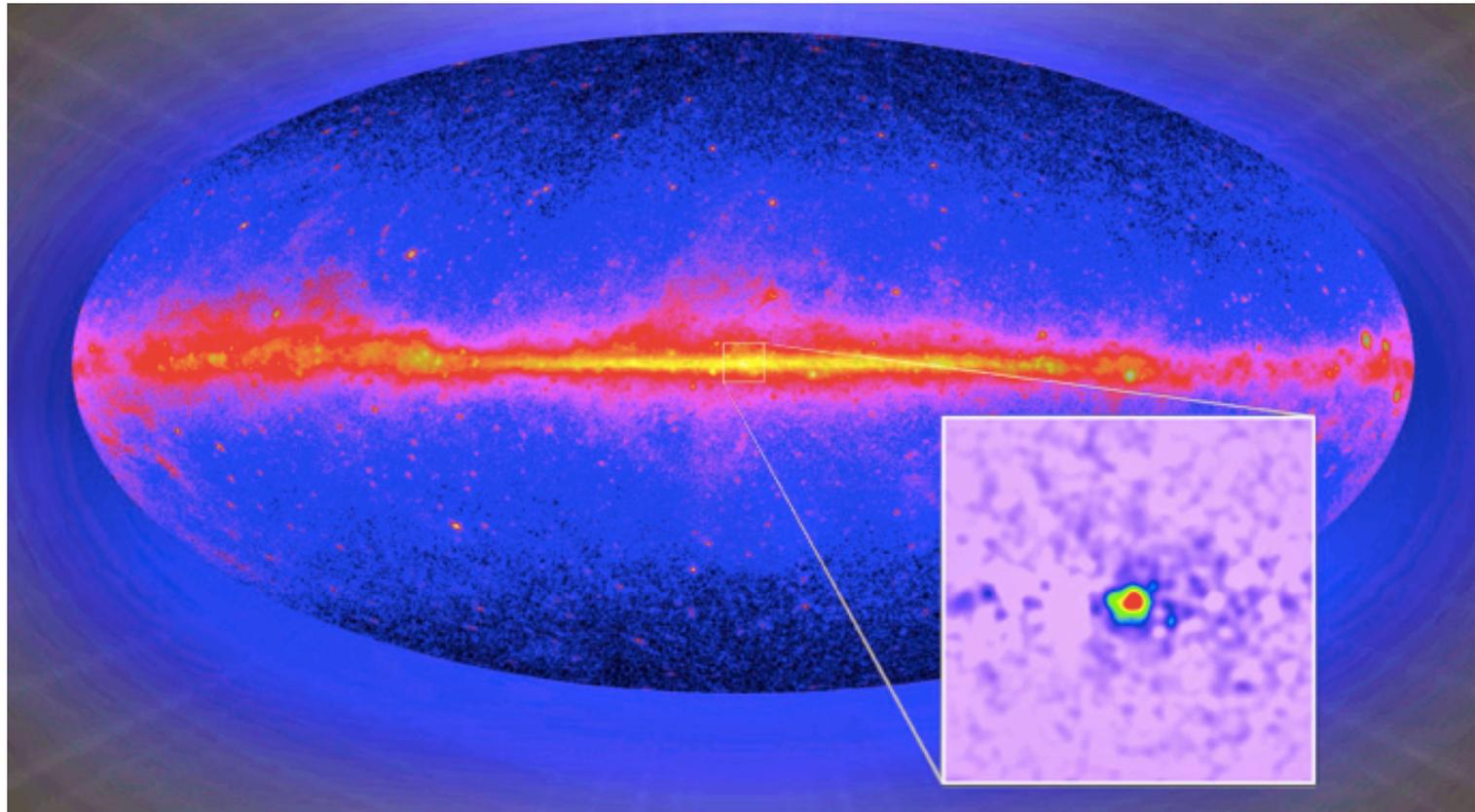
$$J^{\text{tot}} \sim \text{few} \times 10^{20} \text{ GeV}^2/\text{cm}^5, \quad \langle\sigma v\rangle_{\text{lim}} \sim 3 \times 10^{-26} \frac{\text{cm}^3}{\text{s}} \left(\frac{30 \text{ GeV}}{m_\chi} \right)$$

In addition, **monochromatic** photons $\chi\chi \rightarrow \gamma\gamma$

$$\frac{\langle\sigma v\rangle_{\gamma\gamma}}{\langle\sigma v\rangle_{\text{tot}}} \sim \frac{\alpha^2}{16\pi^2}$$



After early reports (primarily by Hooper et al) **Galactic Center Excess** reported independently, and with a variety of different assumptions for background etc, by Daylan et al (Harvard+MIT+Fermilab); Abazijian et al (UCI); Macias and Gordon (NZ)



What **produces** the Galactic Center **excess**?

Fitting the excess with
Dark Matter Annihilation not problematic

- ✓ **Morphology** ~OK
- ✓ **Spectrum** ~OK
- ✓ **Constraints from dSph, radio, CMB**
~sort of OK

What **produces** the Galactic Center **excess**?

Most obvious astrophysical counterpart
(unresolved **pulsars**) **does not work**

- ✓ **Morphology NOT OK**
- ✓ **Spectrum NOT OK**
- ✓ **Not enough!**

What **produces** the Galactic Center **excess**?

WRONG QUESTION!

Rather: **is the excess** indeed **there**?

Are models of **diffuse** emission
adequate to current **data**?